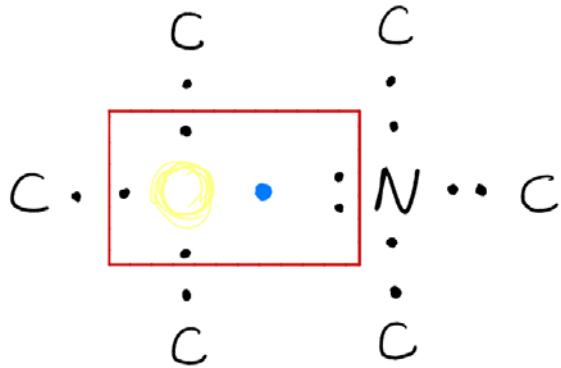
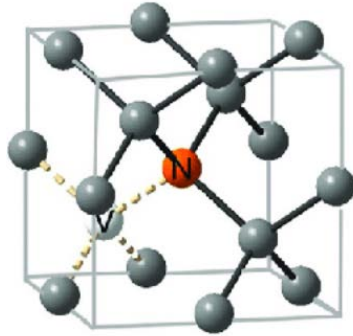


NV center electronic state

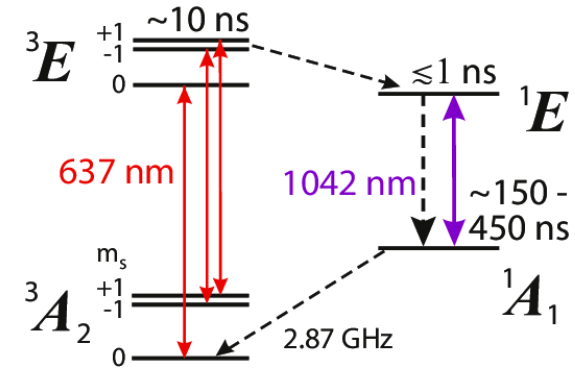
NV center
(sensor)



Structure of NV^-

○ vacancy

• additional electron



Energy level diagram of NV^-

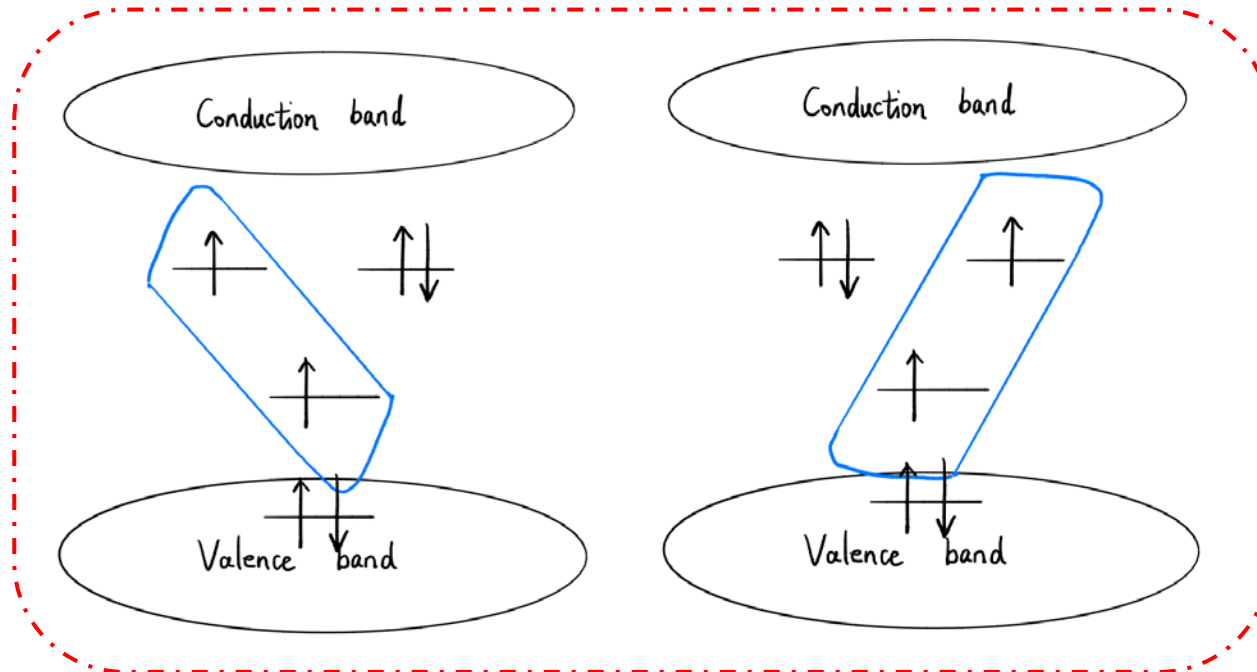
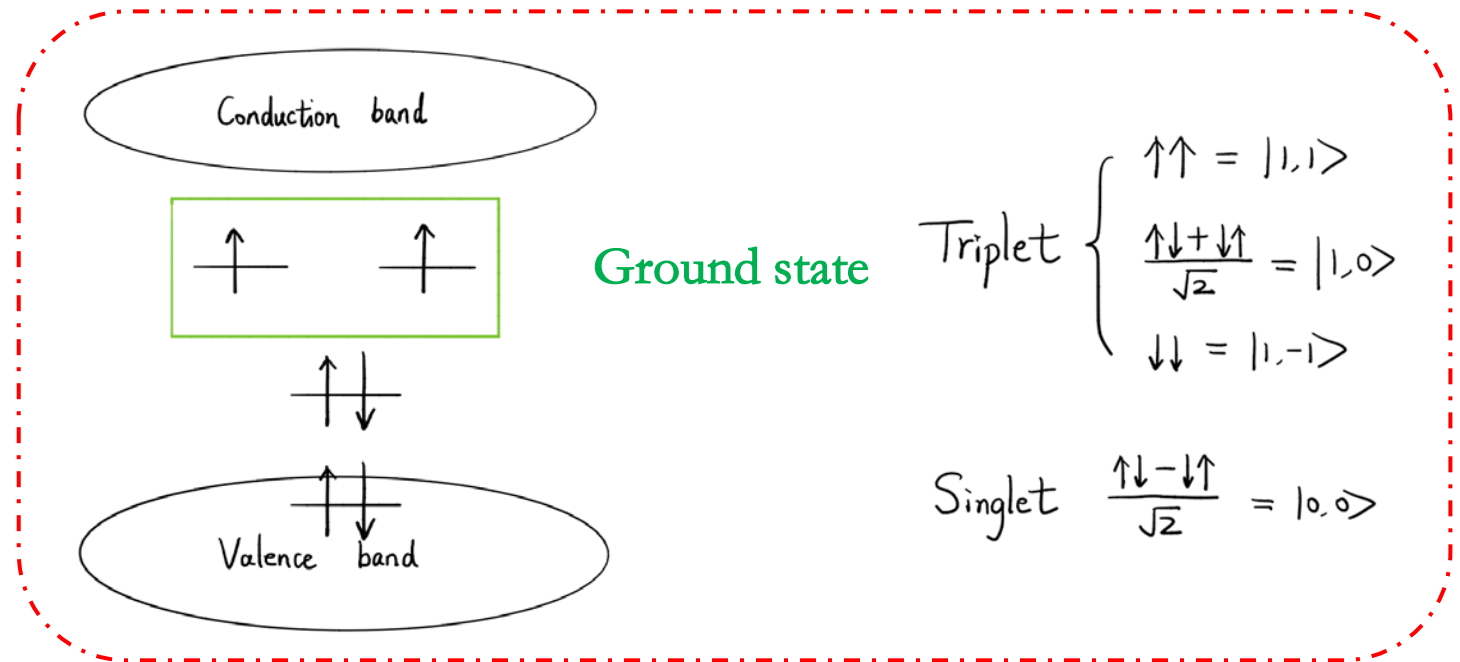
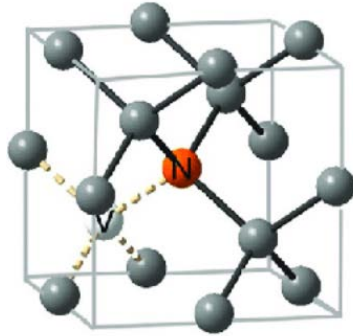
negative NV^- : $S = 1$

neutral NV^0 : $S = \frac{1}{2}$

positive NV^+ : $S = 0$

NV center electronic state

NV center
(sensor)



NV center electronic state

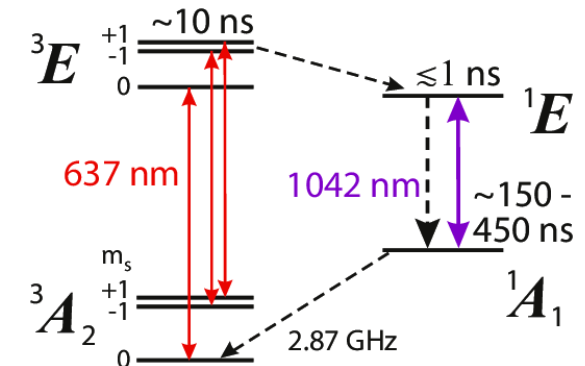
Zero-field H: SOC & spin-spin interaction

$$\begin{aligned}
 H_g &= \frac{1}{\hbar} (\vec{S} \cdot \vec{D} \cdot \vec{S}) \quad \text{Zero field splitting tensor} \quad \vec{D} = \begin{pmatrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{zy} & D_{zz} \end{pmatrix} \\
 &= \frac{1}{\hbar} (S_x D_{xx} S_x + S_y D_{yy} S_y + S_z D_{zz} S_z) \\
 &= \frac{1}{\hbar} (D_x S_x^2 + D_y S_y^2 + D_z S_z^2) \quad S_x^2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad S_x^+ = \begin{pmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{pmatrix} \quad S_y^2 = \begin{pmatrix} \frac{1}{2} & -\frac{1}{2} \\ -\frac{1}{2} & \frac{1}{2} \end{pmatrix} \\
 &\xrightarrow[D \text{ traceless}]{D = \frac{3}{2} D_z, E = \frac{D_x - D_y}{2}} \quad = \hbar \begin{pmatrix} \frac{D}{3} & & E \\ & -\frac{2}{3}D & \\ E & & \frac{D}{3} \end{pmatrix} = \hbar \left\{ D \left[\hat{S}_z^2 - \frac{S(S+1)}{3} \right] + E \frac{(\hat{S}_+^2 + \hat{S}_-^2)}{2(S_x^2 - S_y^2)} \right\}
 \end{aligned}$$

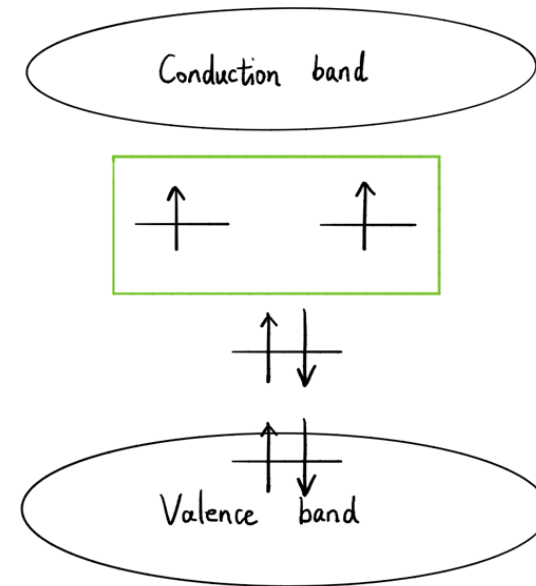
Ground state longitudinal and transverse zero-field splittings D_{GS} and E_{GS}

With energy & states:

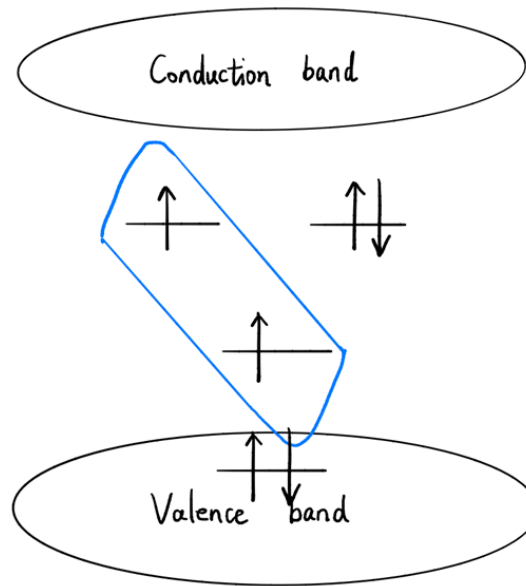
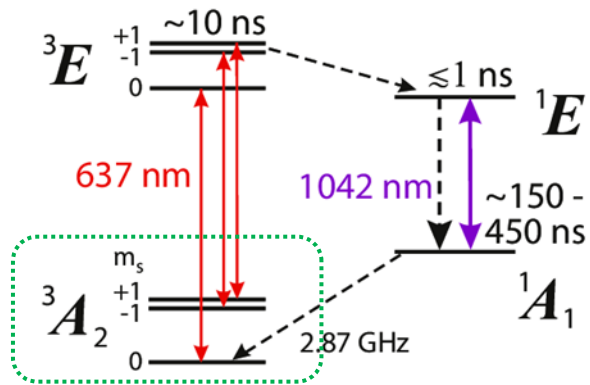
$$\begin{aligned}
 &-\frac{2}{3} D \hbar, \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}; \quad \left(\frac{D}{3} - E \right) \hbar, \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}; \quad \left(\frac{D}{3} + E \right) \hbar, \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}; \\
 &|m_s = 0\rangle \quad \quad \quad |-\rangle \quad \quad \quad |+\rangle
 \end{aligned}$$



Energy level diagram of NV⁻



Coherent manipulation of NV center



(Optical pump)

$$|m_s = 0\rangle \longrightarrow \frac{|0\rangle + |+\rangle}{\sqrt{2}}$$

(MW) $\frac{\pi}{2}$ pulse

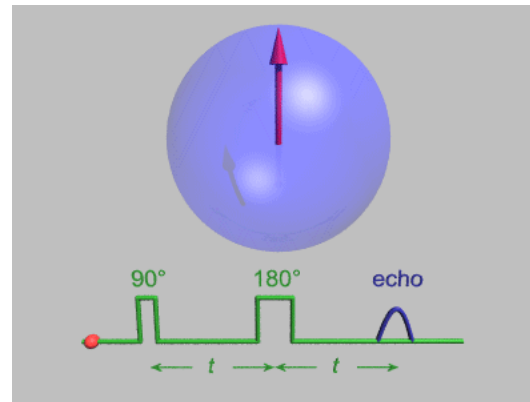
$$H_{MW} = \gamma_e B_{AC} S_x \cos(\omega t)$$

evolution

Governed by time-dependant \vec{B}

$$\frac{1}{\sqrt{2}} \left(|0\rangle + e^{-i\phi} |+\rangle \right)$$

projection: fluorescence



coherence is mapped by another $\pi/2$ pulse into a population difference

Echo amplitude \sim
polarization difference

simplest form of dynamical decoupling

Traditional Nuclear Quadrupole Resonance (NQR)



non-spherical nuclear charge
distributions for $I \geq 1$ nuclei

^{14}N , ^{17}O , ^{35}Cl , ^{63}Cu ...

Interact with EFG:
electric field gradient
(crystal field?)

Transition frequency for axial symmetry

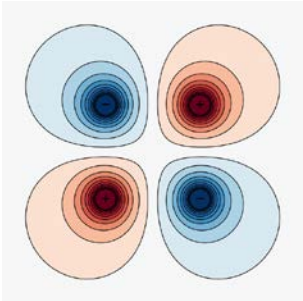
Specific frequency
for a given system

$$\nu_Q = \frac{3e^2 \textcolor{red}{qQ}}{4I(2I-1)h}$$

Q: nuclear quadrupole moment

q ~ largest principal component of the
EFG tensor at the nucleus

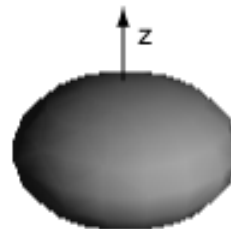
I: nuclear spin



Charge = 0
Dipole moment = 0
Q ≠ 0



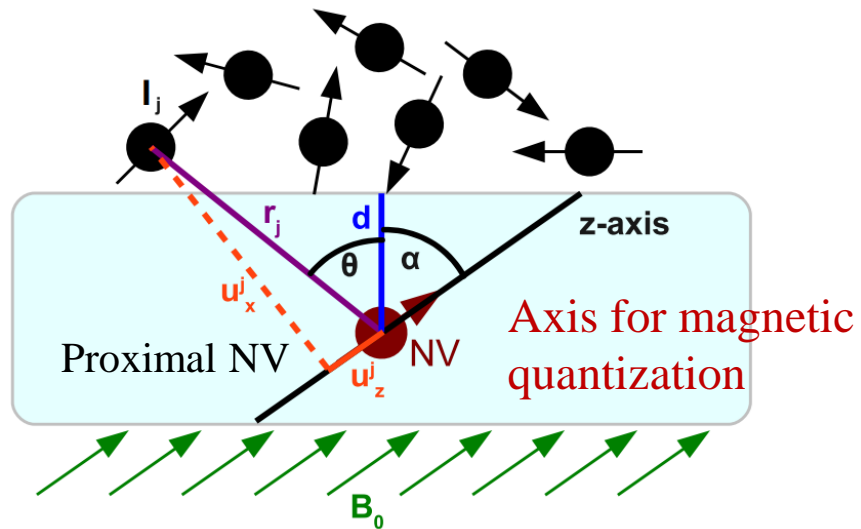
Q > 0
Prolate



Q < 0
Oblate

*B. H. Suits, Handbook of Applied
Solid State Spectroscopy
(Springer, New York, USA, 2006).*

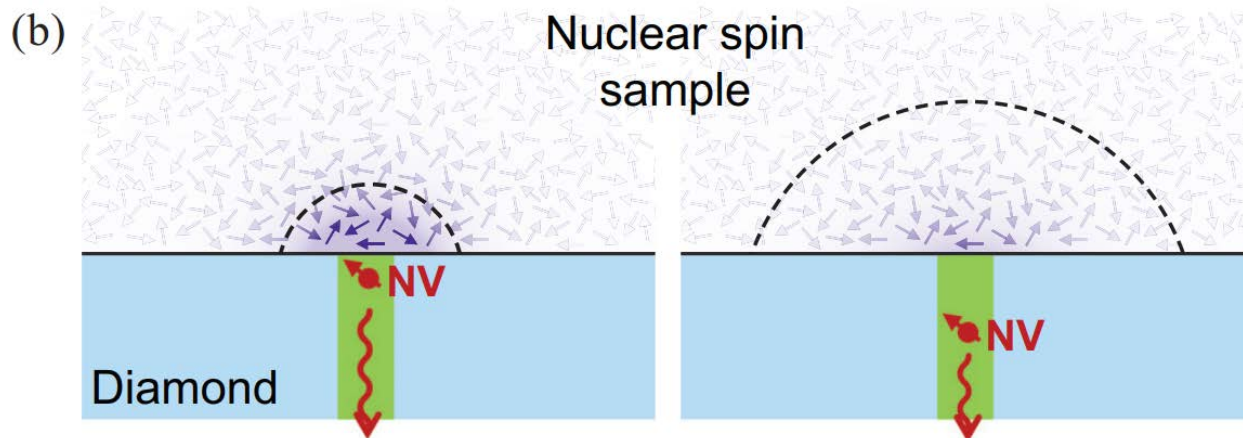
NV center as a nanoscale NQR spectrometer



Measure statistical fluctuations of the spin polarization $\sim \sqrt{N}$
(independent of the applied field)

N : number of nuclear spins
in the sensing volume

High sensitivity and small sensing volume:
ability to probe atomically thin layers

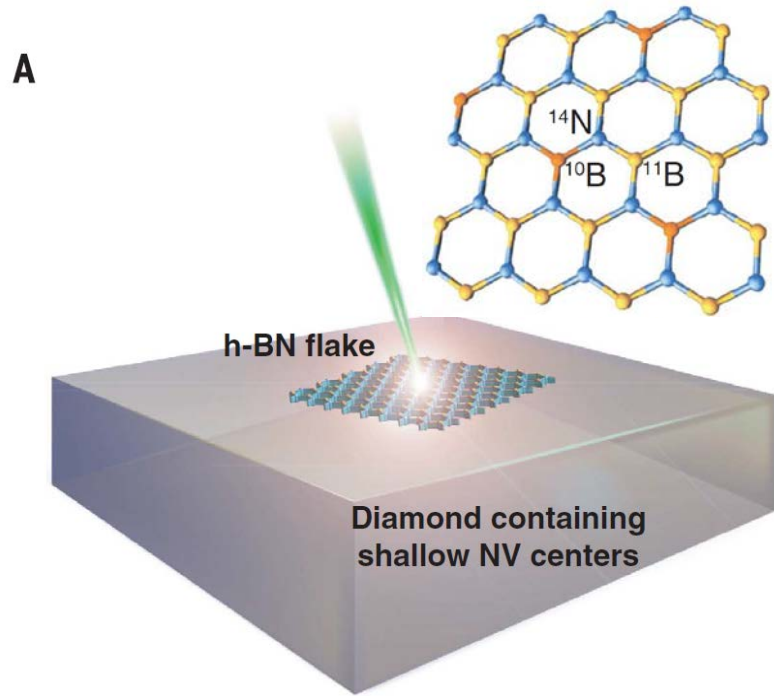


Depth: 6.8 ± 0.1 nm

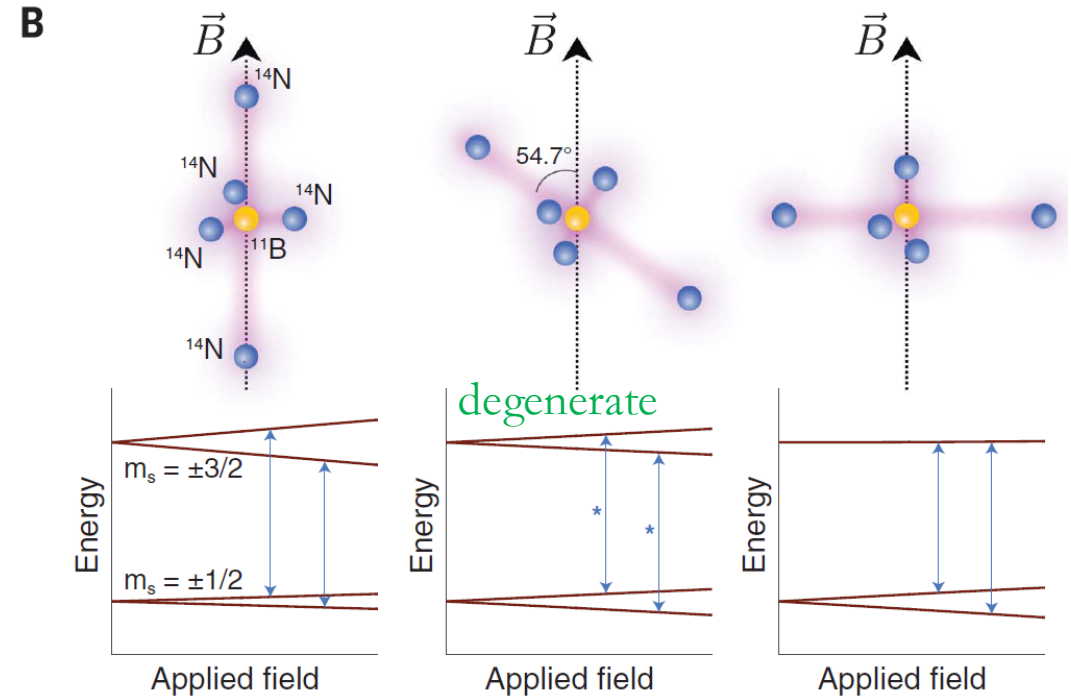
Due to dipolar coupling, a shallow NV center experiences a significantly stronger magnetic field from a smaller nuclear spin sample volume than a deep NV center experiences.

NMR technique for determining the depth of shallow nitrogen-vacancy centers in diamond
Linh M. Pham, Stephen J. DeVience et al

Special case: h-BN flake



$I = 3/2$ $I = 3$
 (80% ^{11}B , 20% ^{10}B)
 (close to 100% ^{14}N) $I = 1$
 honeycomb layered structure



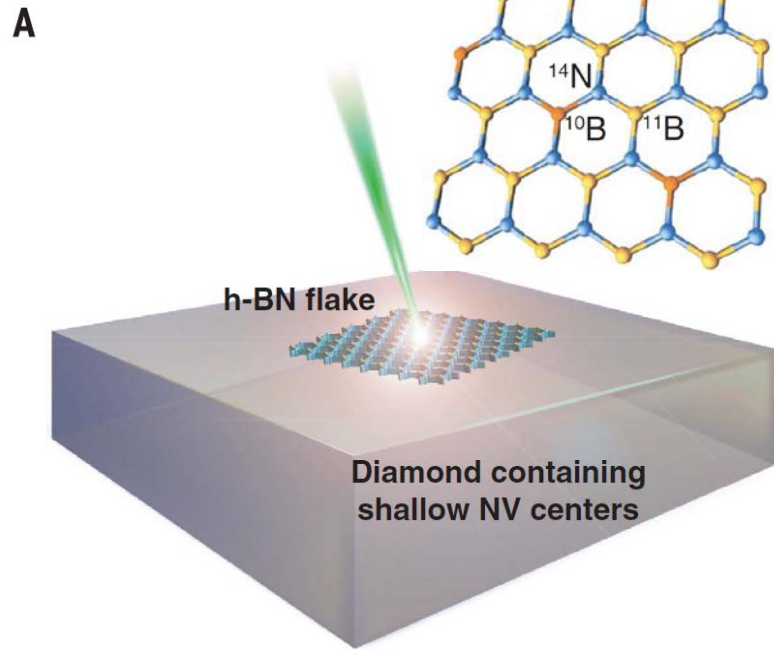
$$m_I = -I, -I+1, \dots, I-1, I$$

$$E_{\pm 3/2} = h\nu_Q \left(1 + \frac{\eta^2}{3} \right)^{1/2},$$

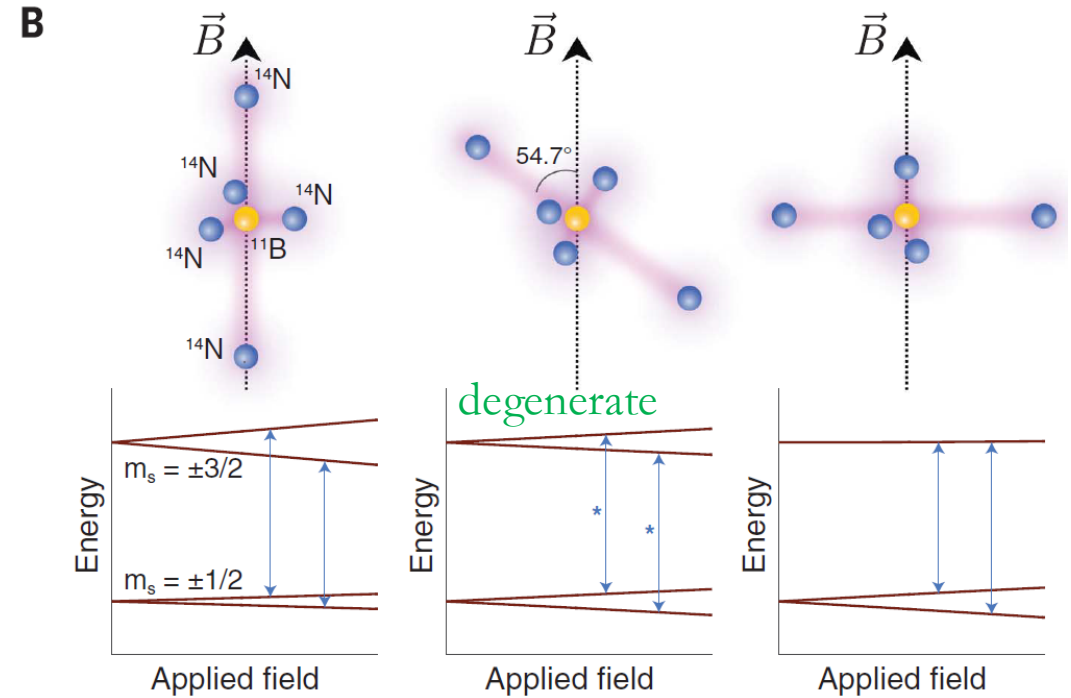
$$E_{\pm 1/2} = -h\nu_Q \left(1 + \frac{\eta^2}{3} \right)^{1/2}$$

B. H. Suits, Handbook of Applied Solid State Spectroscopy (Springer, New York, USA, 2006).

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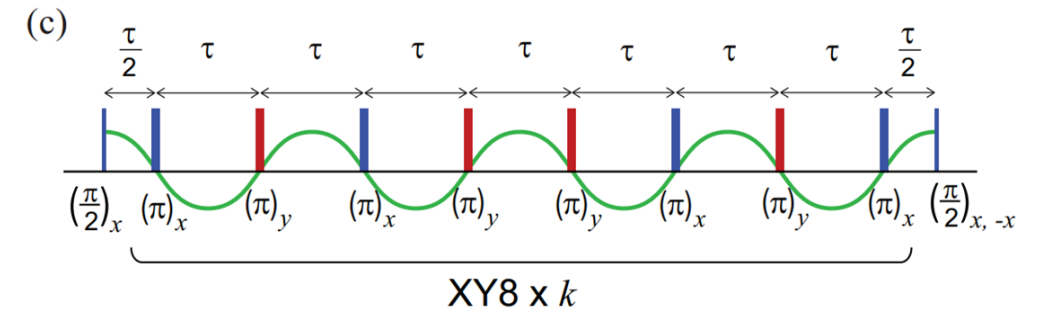
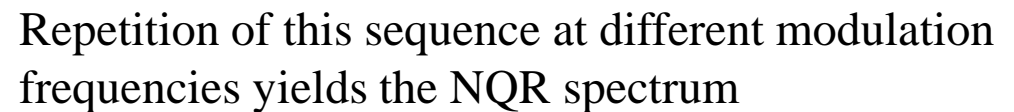
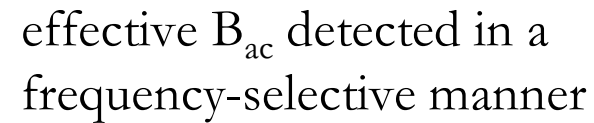
$$E_{\pm 3/2} = \frac{\hbar \nu_Q \rho}{2} \pm \frac{\hbar \nu_0}{2\rho} \left[(\rho - 1 + \eta)^2 c_x^2 + (\rho - 1 - \eta)^2 c_y^2 + (2 + \rho)^2 c_z^2 \right]^{1/2}$$

$$E_{\pm 1/2} = -\frac{\hbar \nu_Q \rho}{2} \pm \frac{\hbar \nu_0}{2\rho} \left[(\rho + 1 - \eta)^2 c_x^2 + (\rho + 1 + \eta)^2 c_y^2 + (2 - \rho)^2 c_z^2 \right]^{1/2}$$

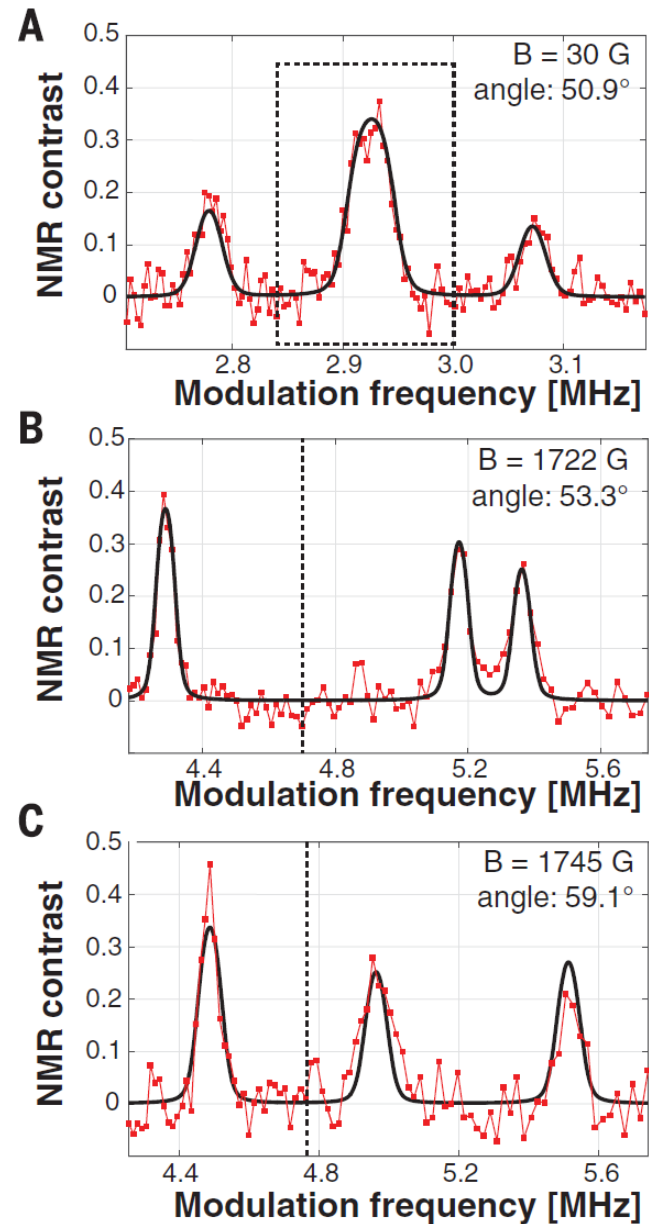
B. H. Suits, Handbook of Applied Solid State Spectroscopy (Springer, New York, USA, 2006).

measure individual Fourier components of NMR

modified XY8-371, 251...



NQR spectroscopy of h-BN



Satellite peaks: dipole-forbidden transitions become weakly allowed due to mixing by the **B** component perpendicular to the h-BN principal axis

