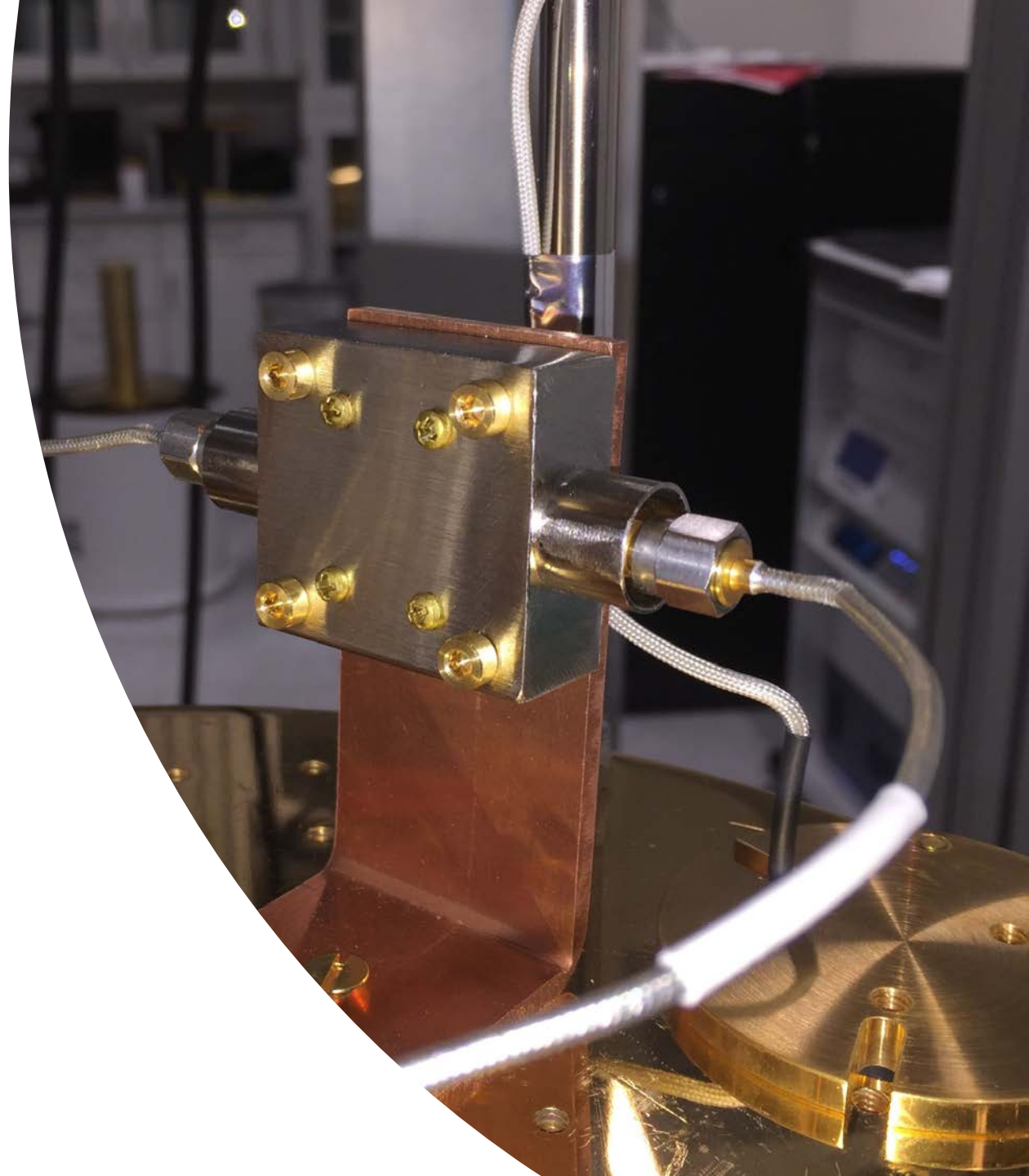


# Summer Research Summary

10/17/2019

Yuxiang Pei

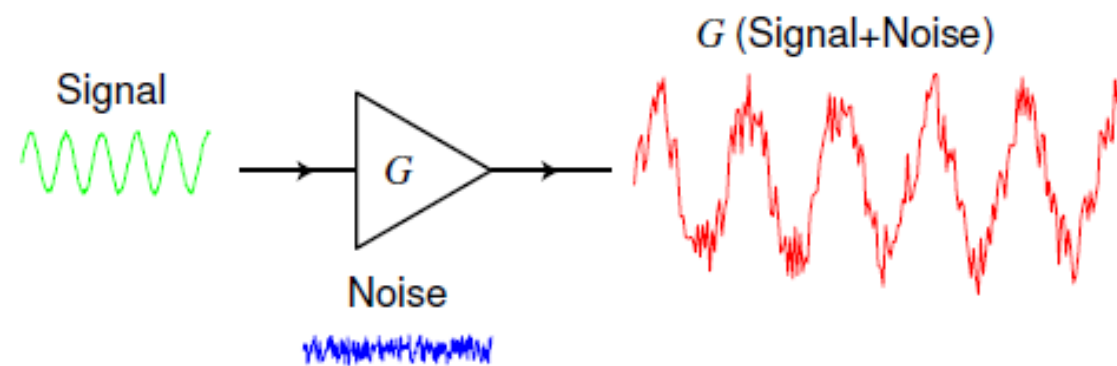
- Characterization of TWPA
- Enhancing sensitivity of EPR
- Setting up of HEMT





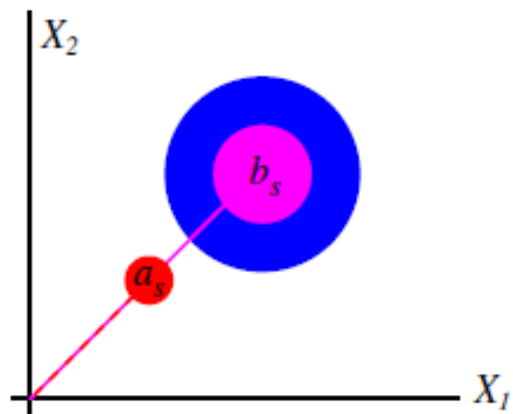
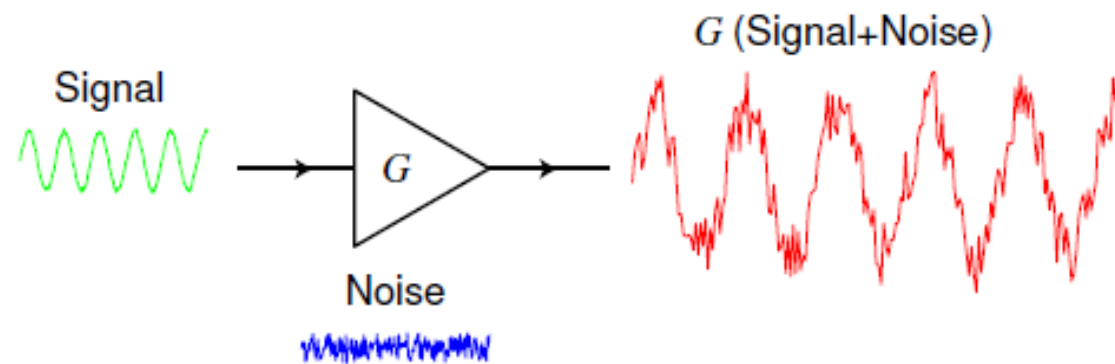


# Motivation





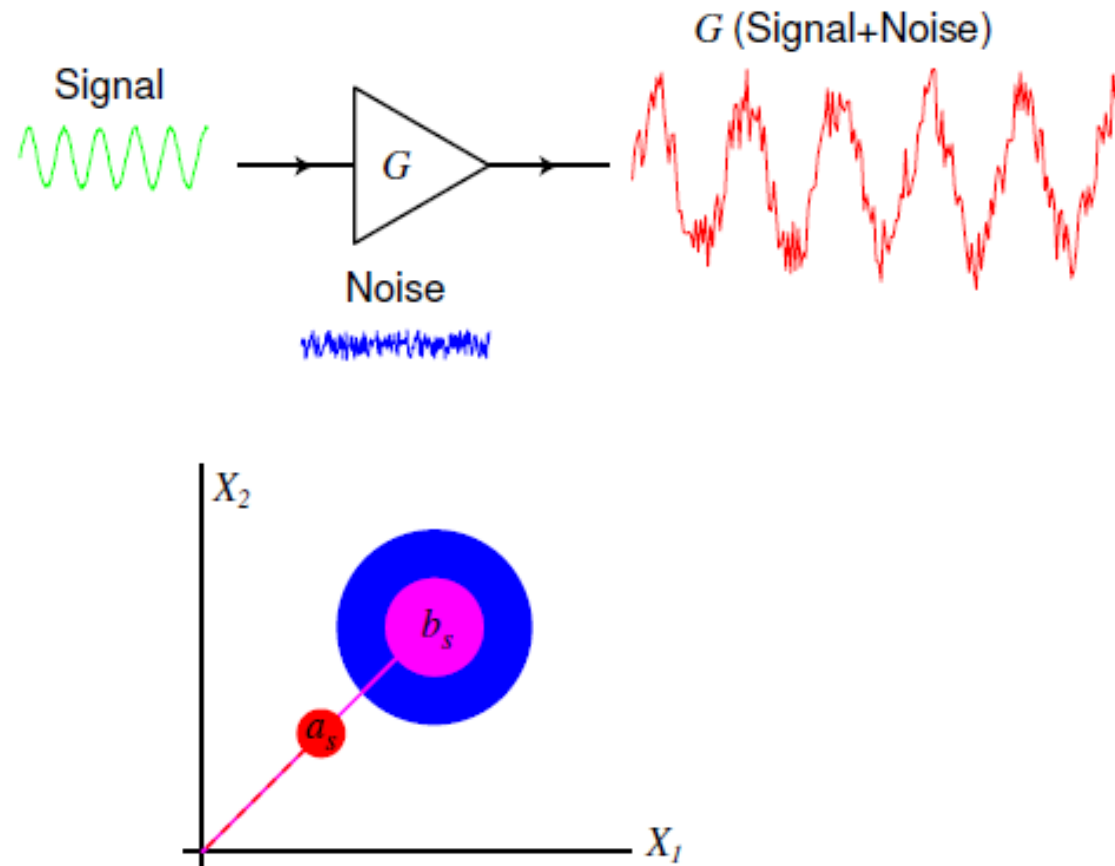
# Motivation



Quantum limit of amplification:

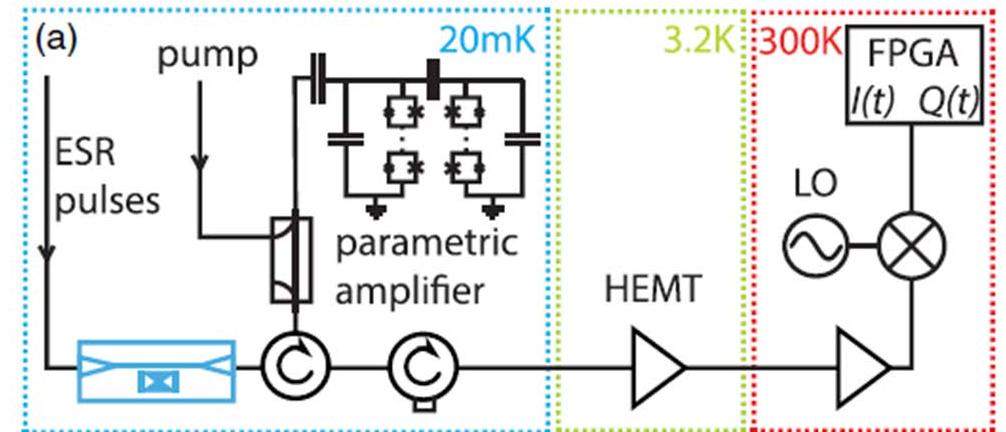
minimum amount of added noise to quadratures

# Motivation



Quantum limit of amplification:

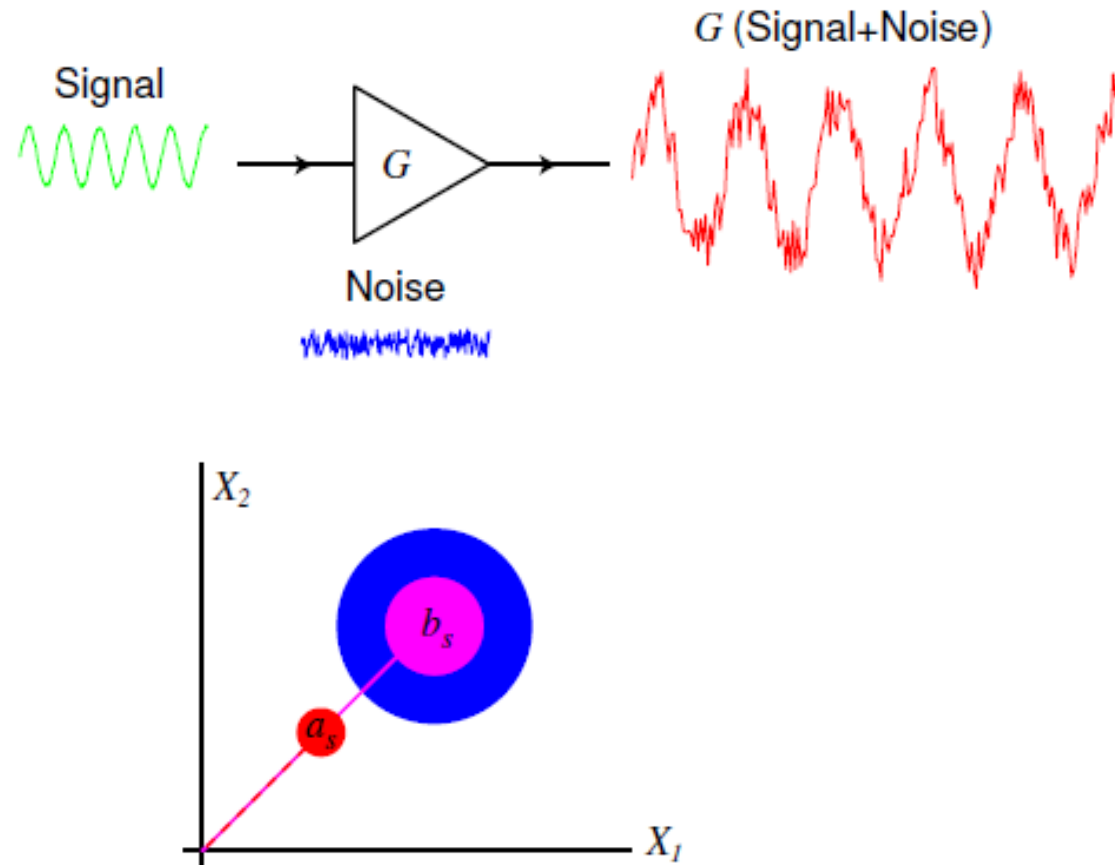
minimum amount of added noise to quadratures



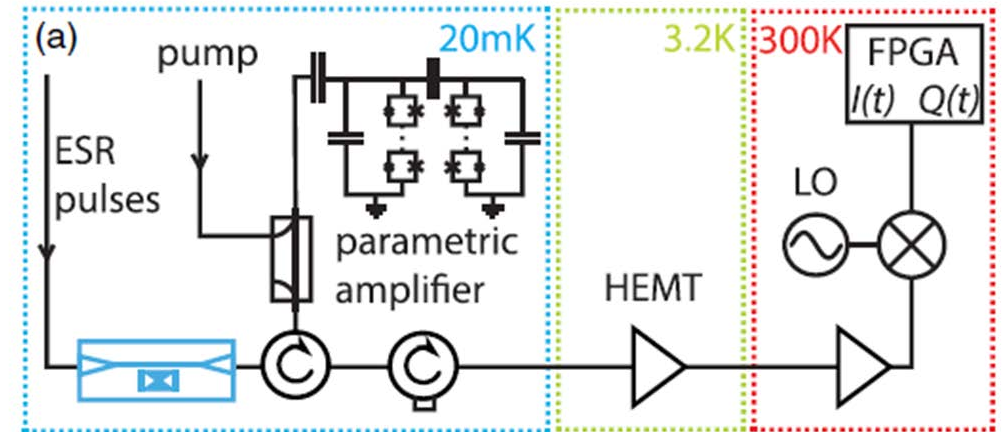
Sensitive measurements



# Motivation



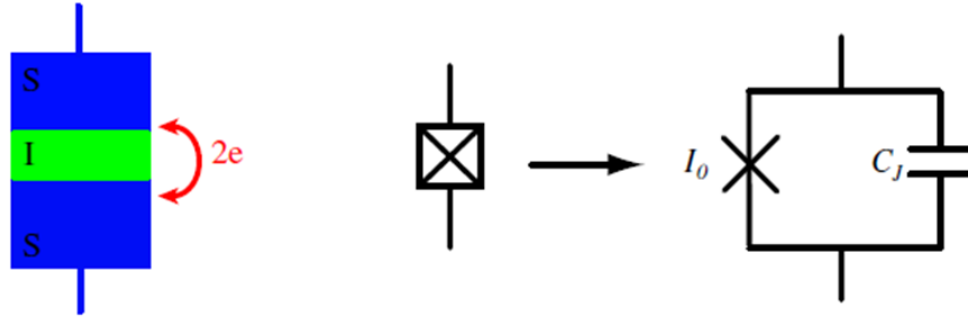
Quantum limit of amplification:  
minimum amount of added noise to quadratures



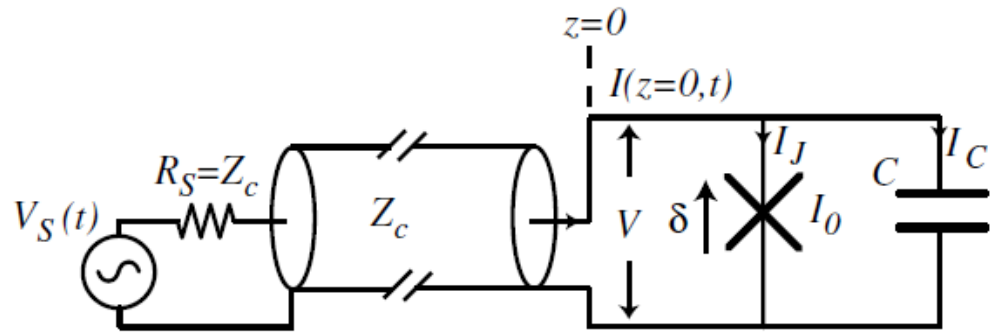
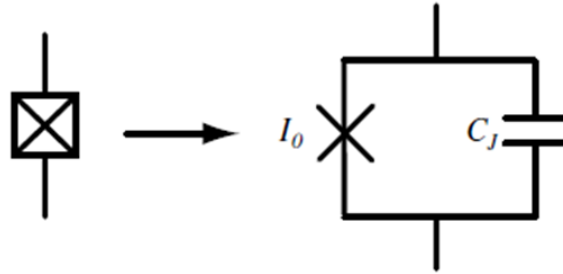
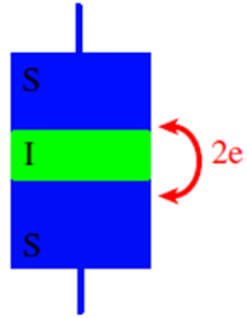
Sensitive measurements

Traditional JPA:  
single frequency measurements  
low bandwidth and saturation power

# Non-linear nature of Josephson junctions

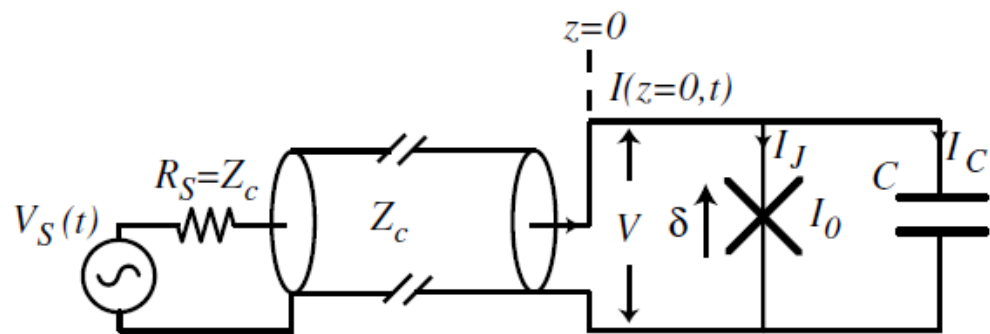
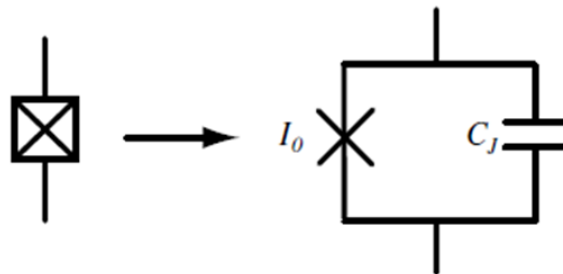
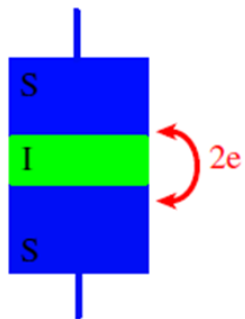


# Non-linear nature of Josephson junctions



$$C\varphi_0 \frac{d^2\delta(t)}{dt^2} + \frac{\varphi_0}{Z_c} \frac{d\delta(t)}{dt} + I_0 \sin(\delta(t)) = I_S(t)$$

# Non-linear nature of Josephson junctions

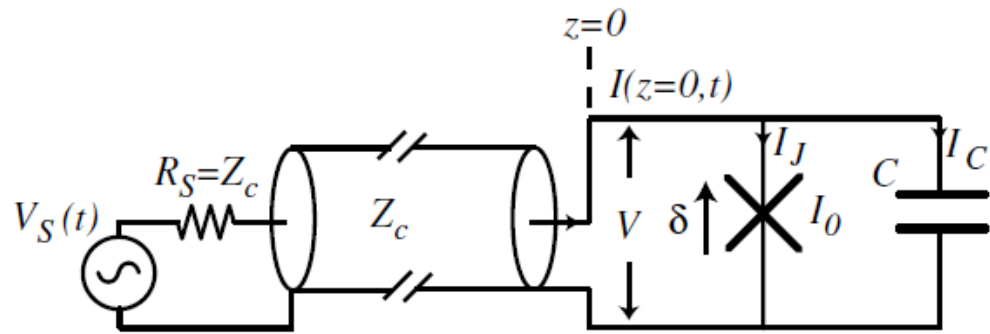
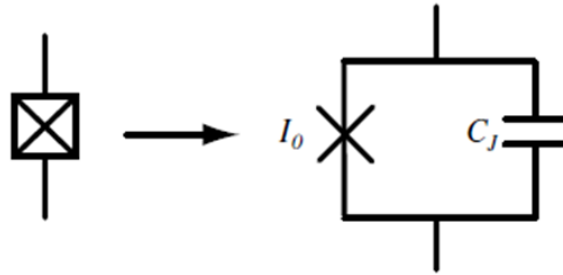
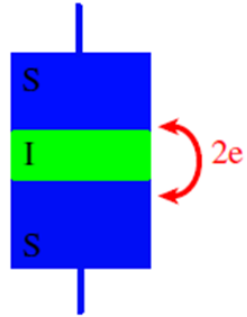


$$C\varphi_0 \frac{d^2\delta(t)}{dt^2} + \frac{\varphi_0}{Z_c} \frac{d\delta(t)}{dt} + I_0 \sin(\delta(t)) = I_S(t)$$

$$\frac{d^2\delta(t)}{dt^2} + 2\gamma \frac{d\delta(t)}{dt} + \omega_0^2 \left( \delta(t) - \frac{\delta^3(t)}{6} \right) - \omega_0^2 \frac{I_p}{I_0} \cos(\omega_p t) = \frac{2}{C\varphi_0 Z_c} v_s^{in}(t)$$

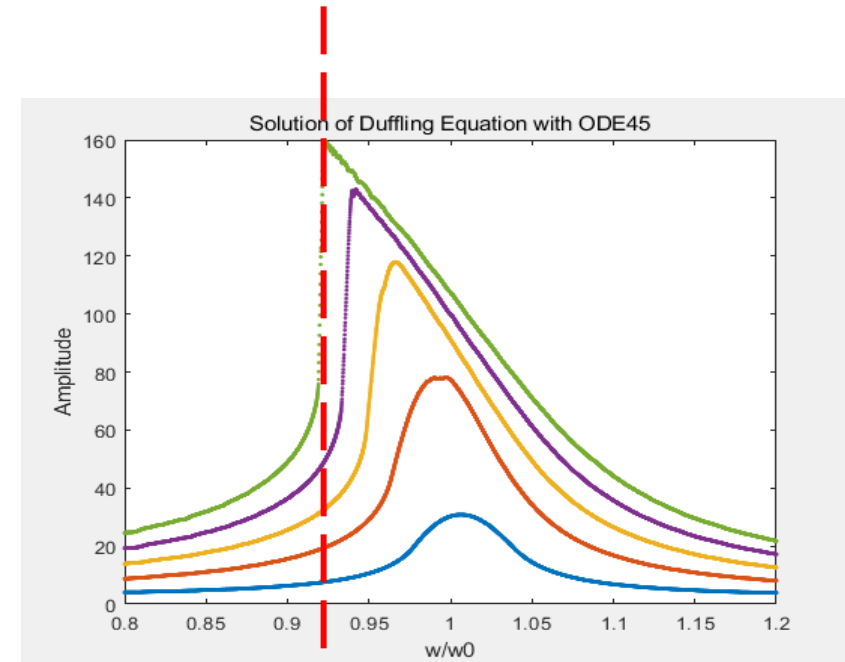


# Non-linear nature of Josephson junctions



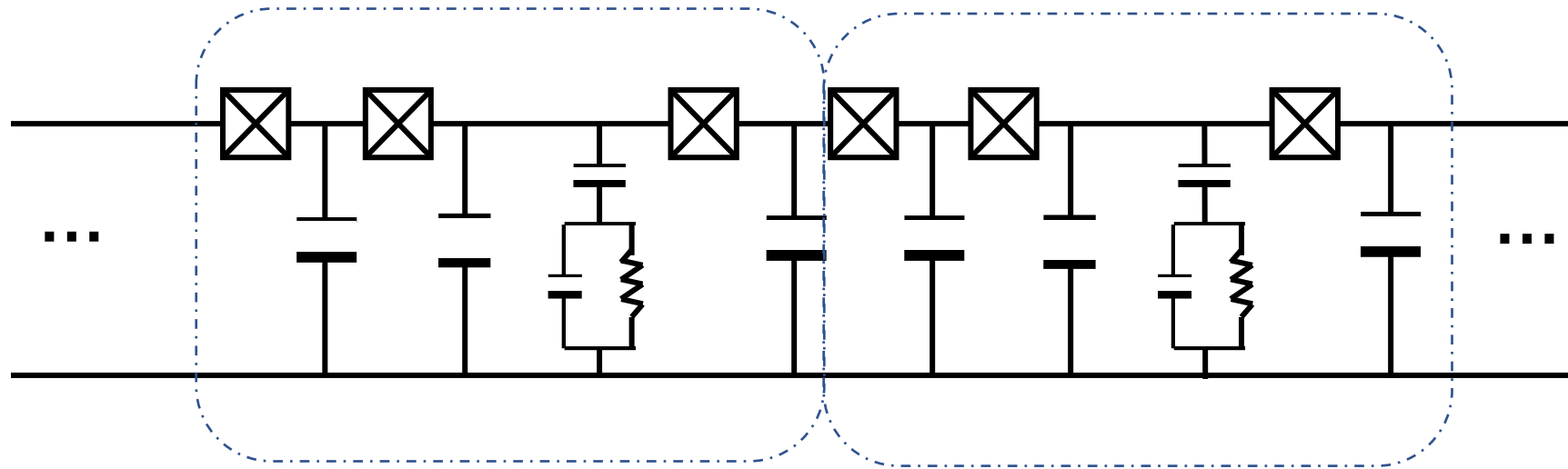
$$C\varphi_0 \frac{d^2\delta(t)}{dt^2} + \frac{\varphi_0}{Z_c} \frac{d\delta(t)}{dt} + I_0 \sin(\delta(t)) = I_S(t)$$

$$\frac{d^2\delta(t)}{dt^2} + 2\gamma \frac{d\delta(t)}{dt} + \omega_0^2 \left( \delta(t) - \frac{\delta^3(t)}{6} \right) - \omega_0^2 \frac{I_p}{I_0} \cos(\omega_p t) = \frac{2}{C\varphi_0 Z_c} v_s^{in}(t)$$



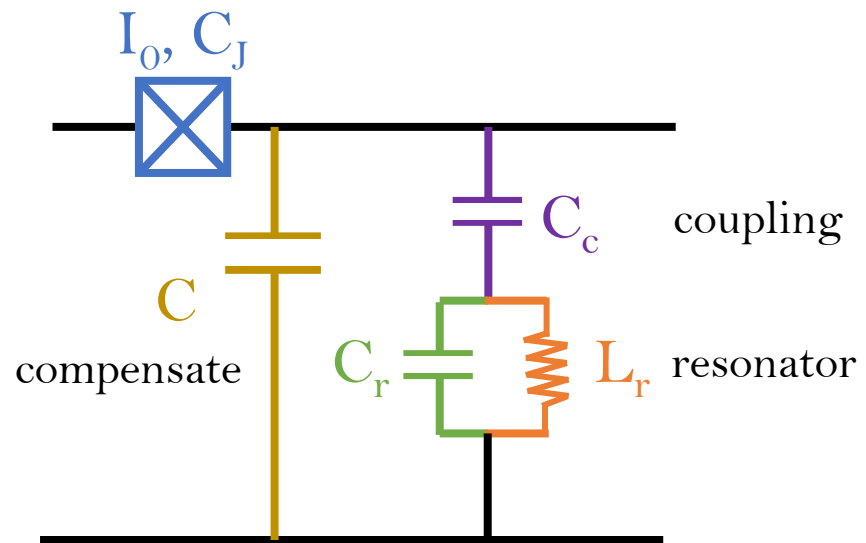
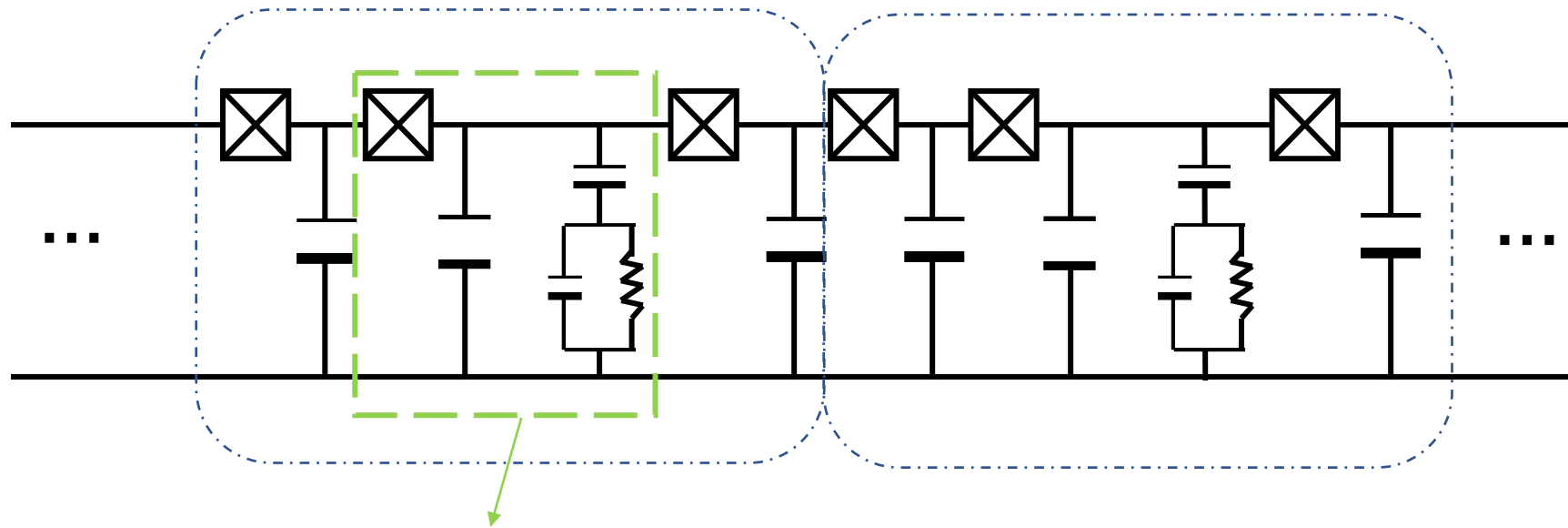


## Resonant phase matching



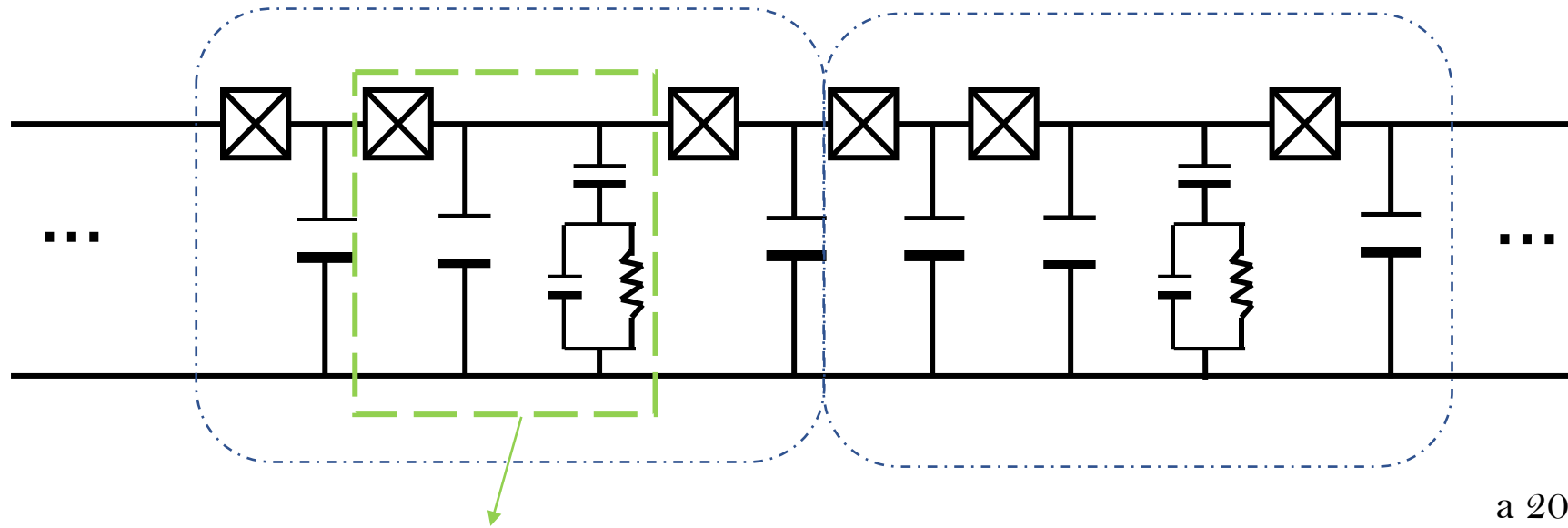


# Resonant phase matching

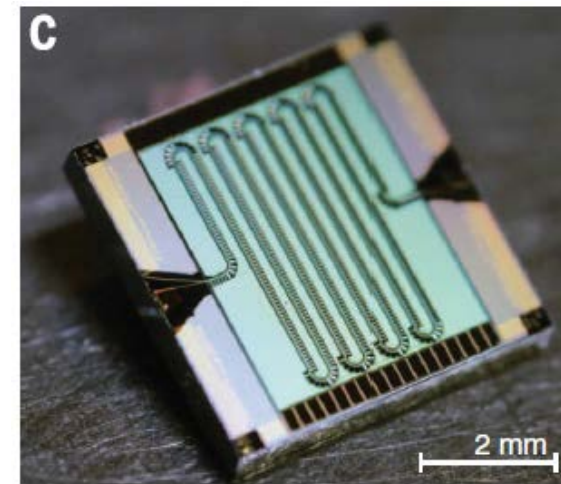
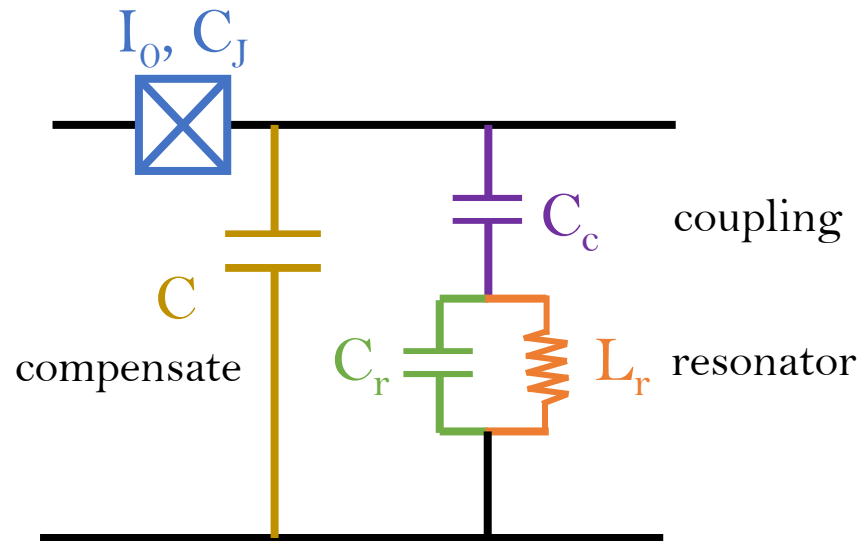




# Resonant phase matching



a 2037 junction JTWPA



*A near-quantum-limited Josephson traveling-wave parametric amplifier C. Macklin et al.*



## Resonant phase matching

$$\frac{\partial a_s}{\partial x} - i\kappa_s a_i^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$

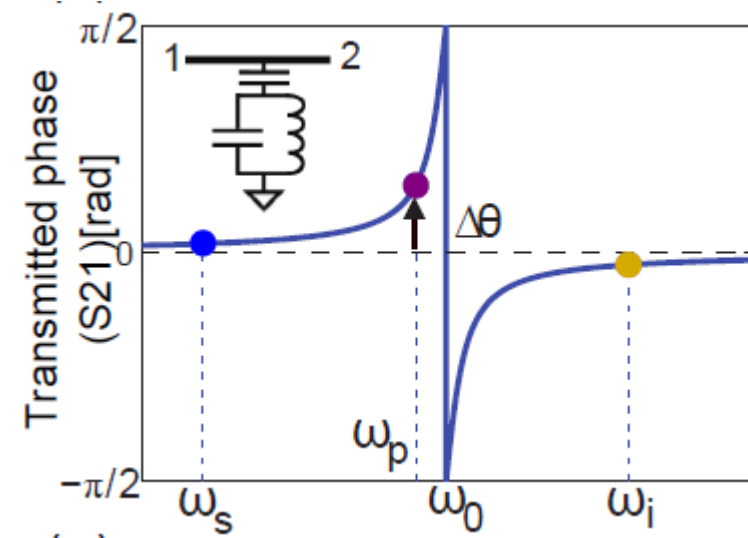
$$\frac{\partial a_i}{\partial x} - i\kappa_i a_s^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$



## Resonant phase matching

$$\frac{\partial a_s}{\partial x} - i\kappa_s a_i^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$

$$\frac{\partial a_i}{\partial x} - i\kappa_i a_s^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$

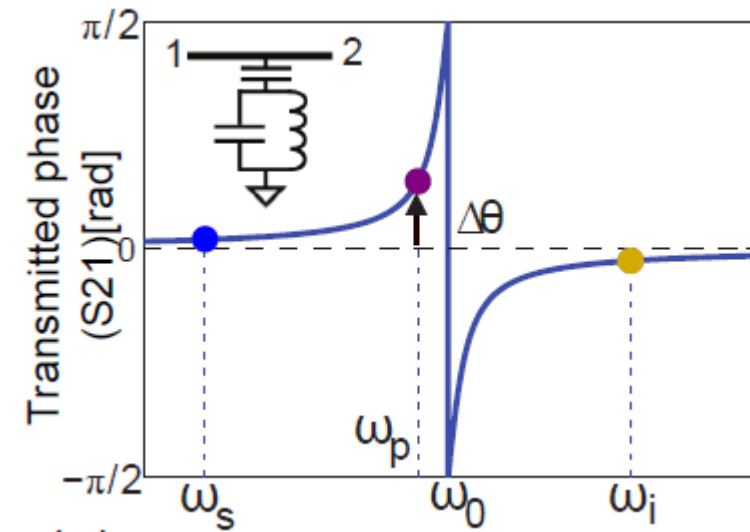


Phase shift due to a shunt resonator to ground

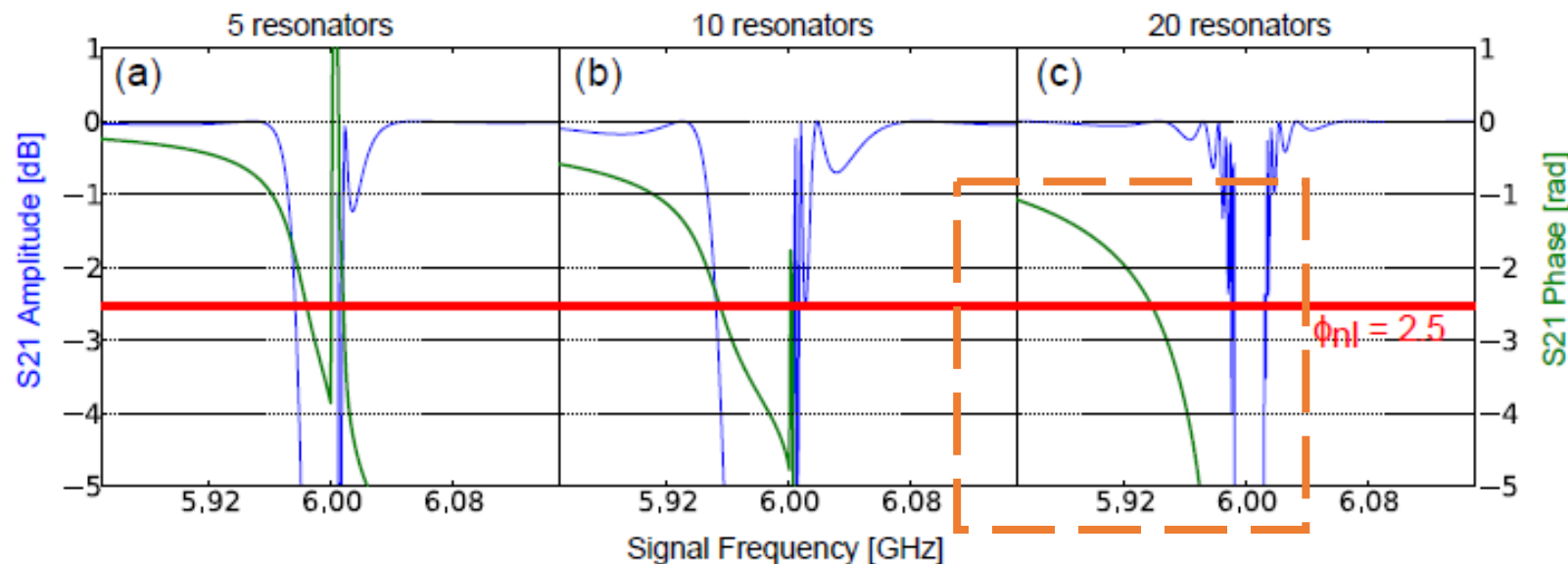
## Resonant phase matching

$$\frac{\partial a_s}{\partial x} - i\kappa_s a_i^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$

$$\frac{\partial a_i}{\partial x} - i\kappa_i a_s^* e^{i(\Delta k_L + 2\alpha_p - \alpha_s - \alpha_i)x} = 0$$



Phase shift due to a shunt resonator to ground



**simulated signal phase and A vs f  
for different numbers of resonators**

*Traveling wave parametric amplifier with  
Josephson junctions using minimal resonator  
phase matching T.C. White et al.*



TWPA gain

## TWPA gain

$$G_s = \cosh^2(gz) + \left(\frac{\kappa}{2g}\right)^2 \sinh^2(gz)$$

$$g = \sqrt{\frac{k_s k_i}{k_p^2} (\gamma k_p)^2 - (\kappa/2)^2}$$

$$\kappa = 2\gamma k_p + k_s + k_i - 2k_p$$

$z$ : the length along the transmission line

$\gamma$ : nonlinearity, the ratio of drive current to junction critical current

$\kappa$ : effective dispersion

$\Delta k$ : difference in wave vectors, phase mismatch

## TWPA gain

- linear superconducting transmission line

$$G_s = 1 + (\gamma k_p z)^2 = 1 + \phi_{nl}^2$$



nonlinear phase shift of the pump

$$G_s = \cosh^2(gz) + \left(\frac{\kappa}{2g}\right)^2 \sinh^2(gz)$$

$$g = \sqrt{\frac{k_s k_i}{k_p^2} (\gamma k_p)^2 - (\kappa/2)^2}$$

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## TWPA gain

- linear superconducting transmission line

$$G_s = 1 + (\gamma k_p z)^2 = 1 + \phi_{nl}^2$$



nonlinear phase shift of the pump

- Proper phase matching ( $\kappa=0$ )

$$G_s = \cosh^2(\gamma k_p z) \approx \frac{\exp(2\phi_{nl})}{4}$$

$$G_s = \cosh^2(gz) + \left(\frac{\kappa}{2g}\right)^2 \sinh^2(gz)$$

$$g = \sqrt{\frac{k_s k_i}{k_p^2} (\gamma k_p)^2 - (\kappa/2)^2}$$

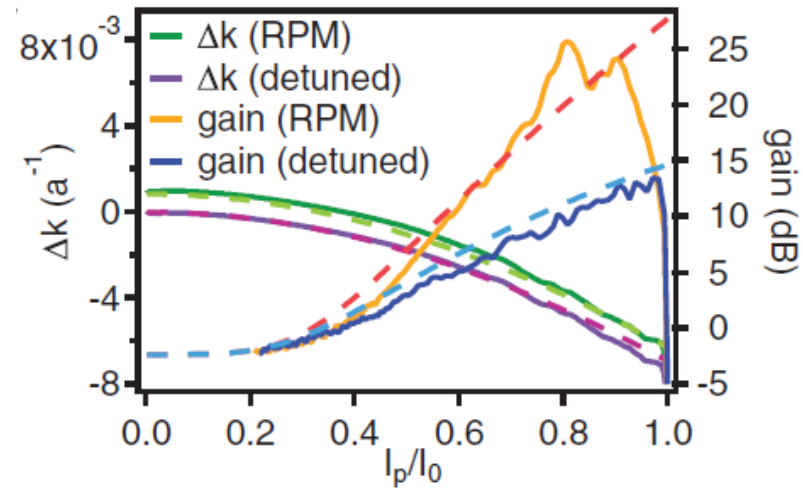
$$\kappa = 2\gamma k_p + k_s + k_i - 2k_p$$

$z$ : the length along the transmission line

$\gamma$ : nonlinearity, the ratio of drive current to junction critical current

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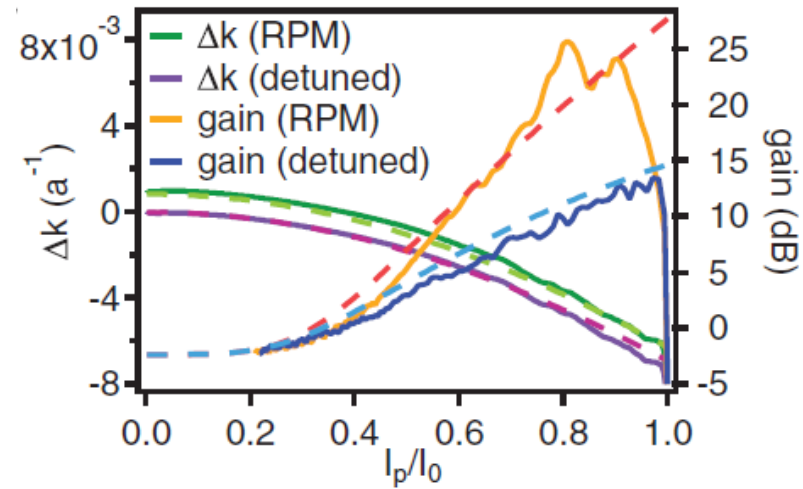
$\Delta k$ : difference in wave vectors, phase mismatch



### Phase mismatch and gain.

7.157 GHz and 6.5 GHz versus pump power, with a signal at 6.584 GHz.

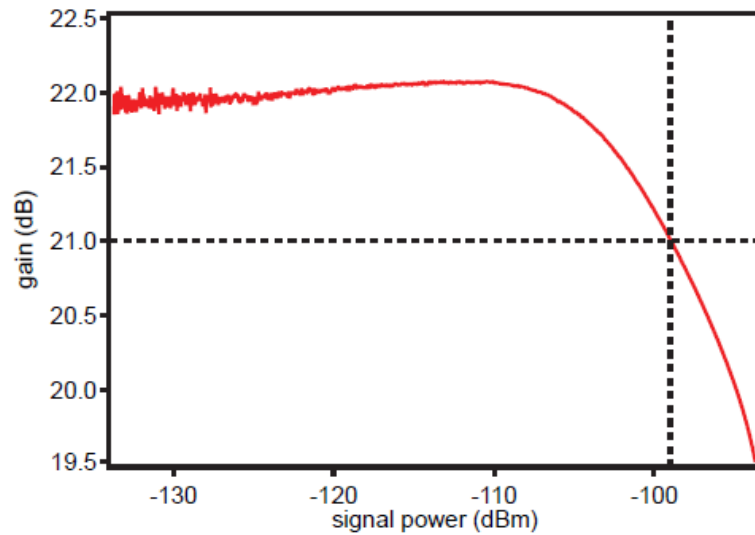
*A near-quantum-limited Josephson traveling-wave parametric amplifier C. Macklin et al.*



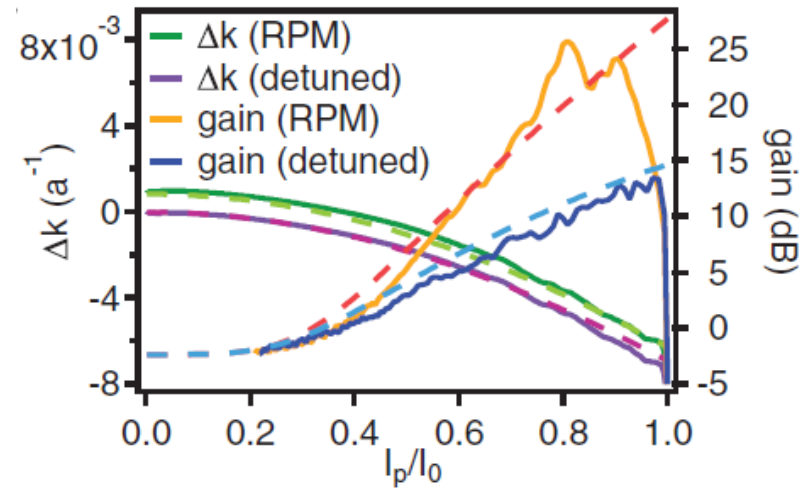
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7.157 GHz and 6.5 GHz versus pump power, with a signal at 6.584 GHz.

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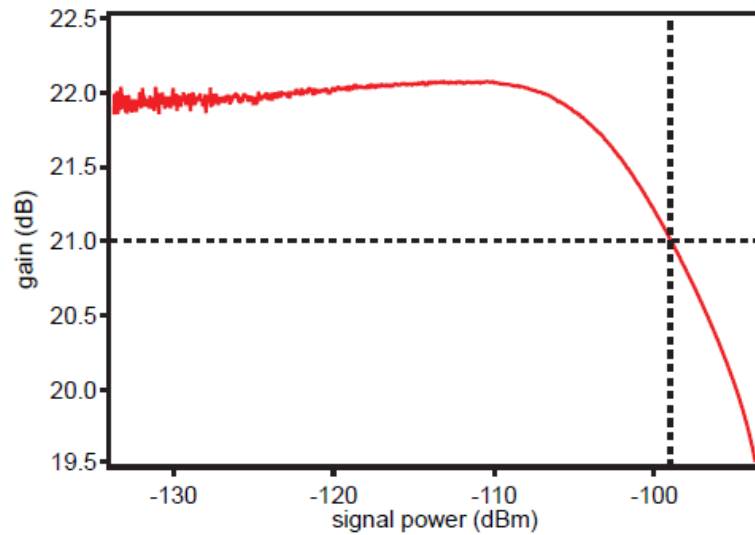
1-dB Compression point



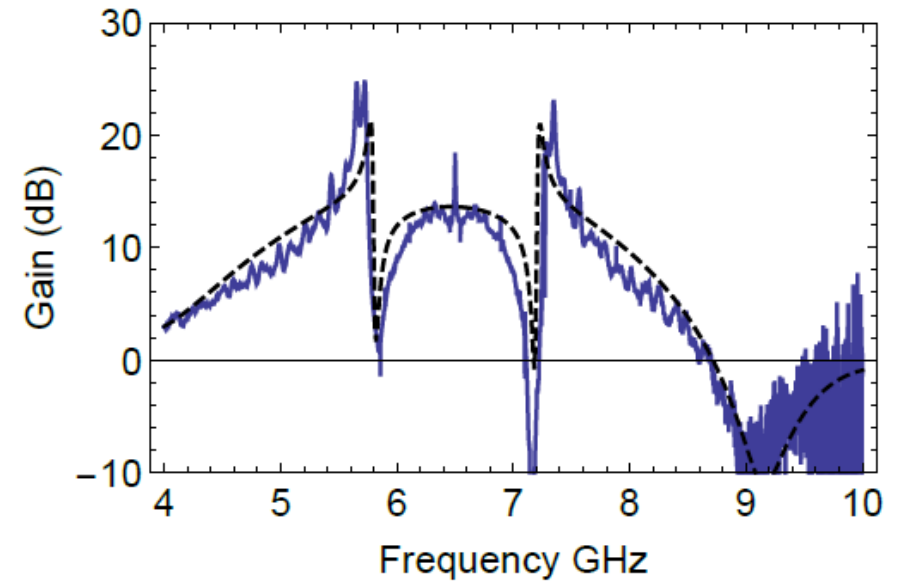
### Phase mismatch and gain.

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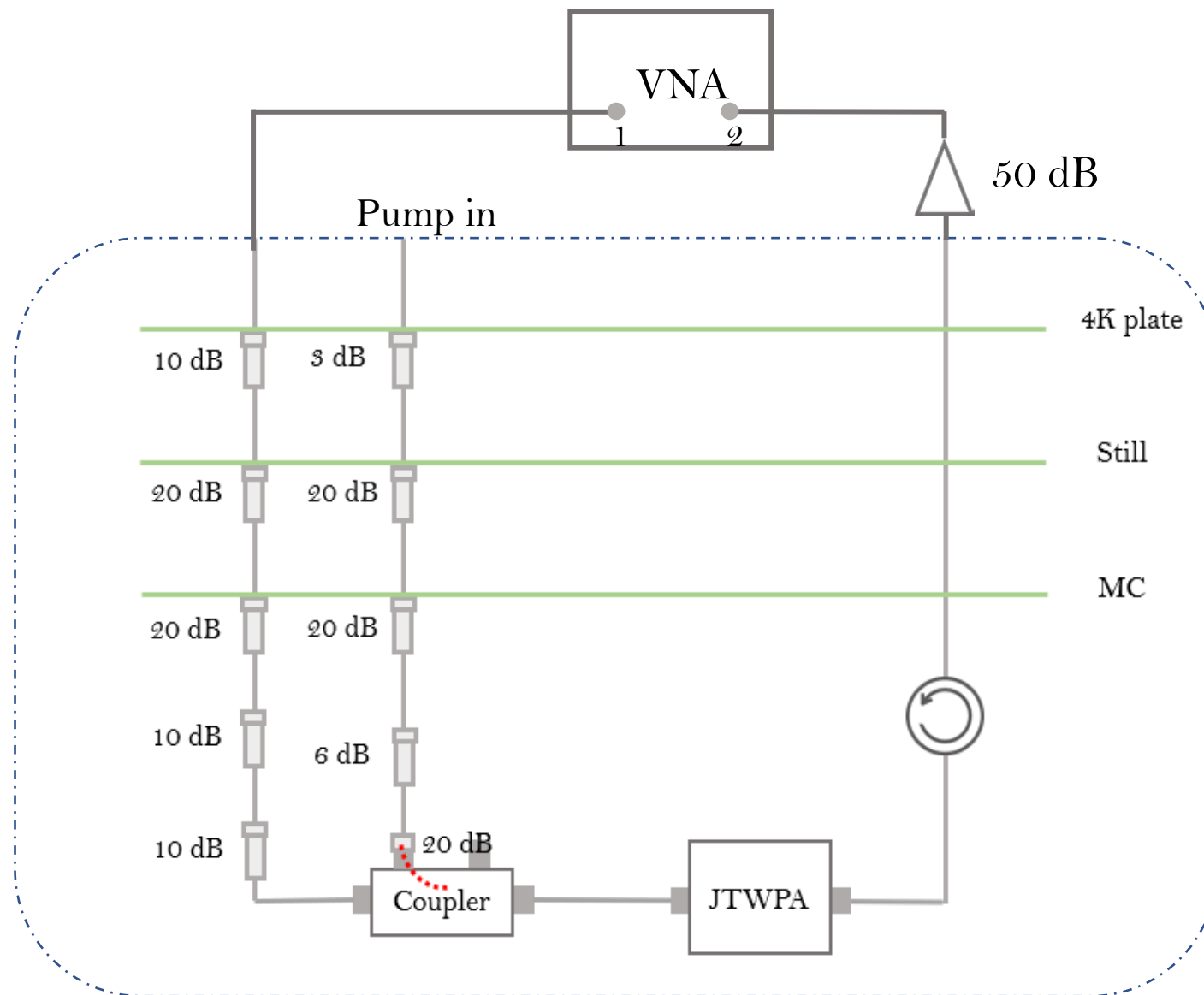
1-dB Compression point



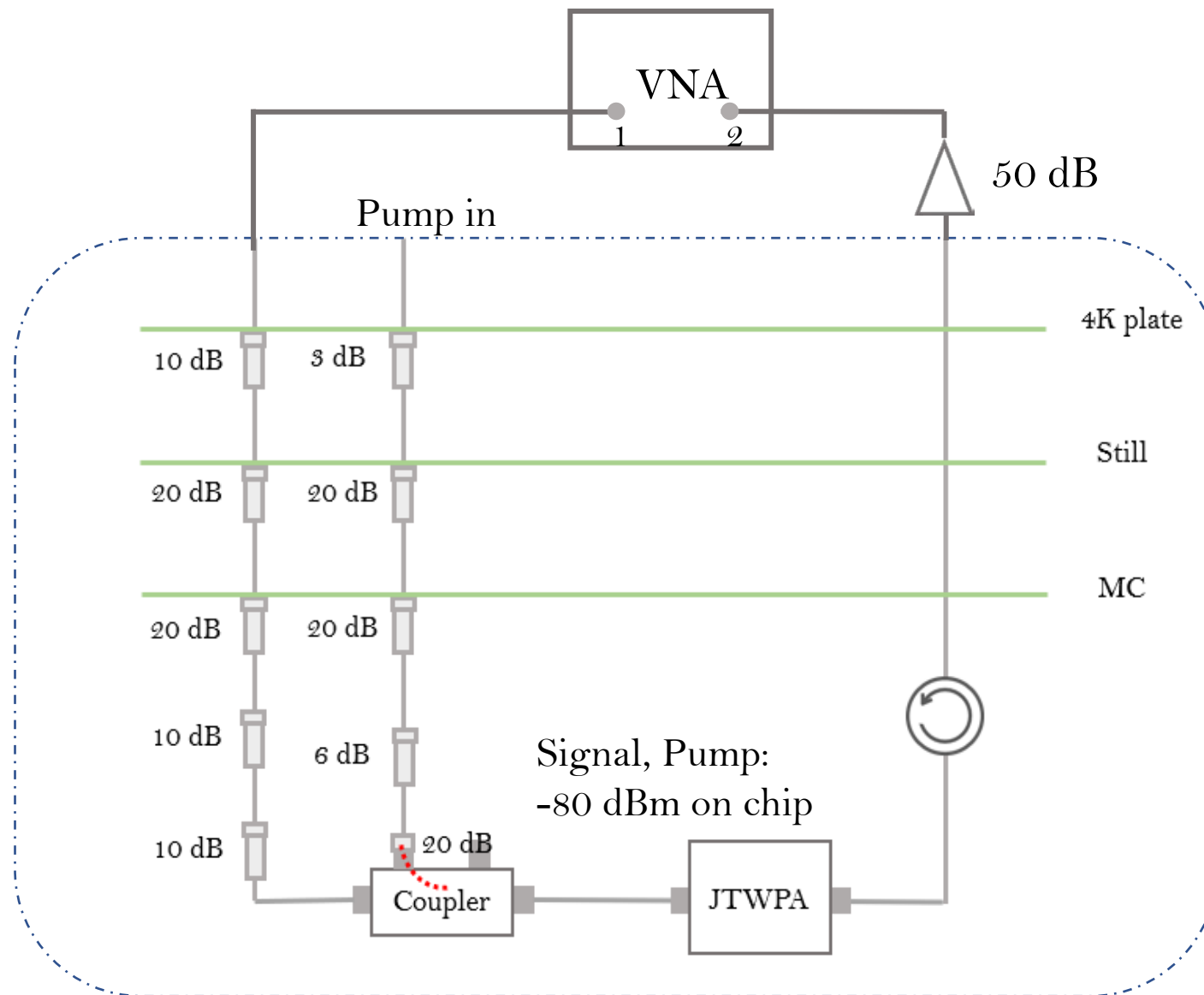
Measured gain spectrum when the pump is detuned



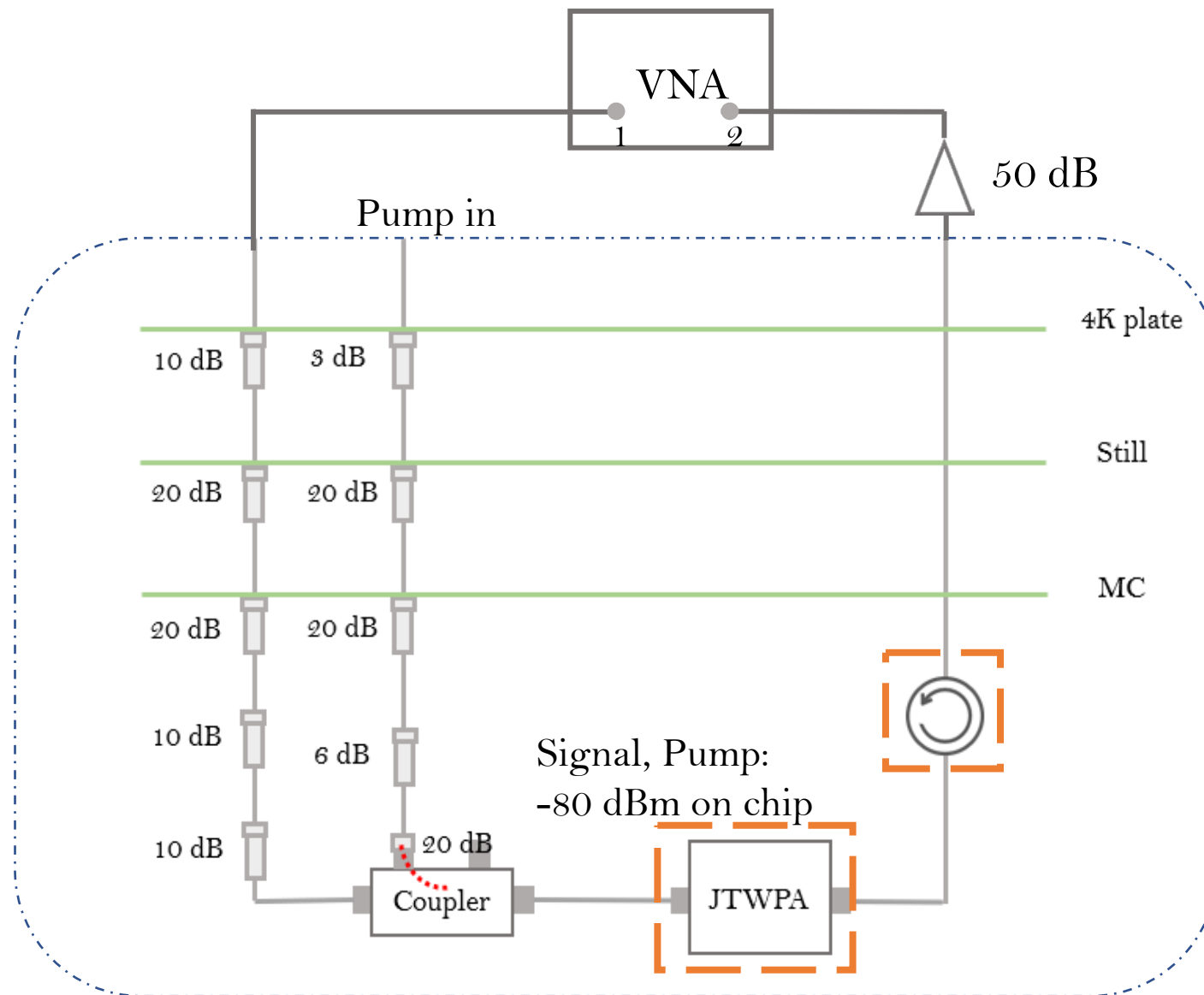
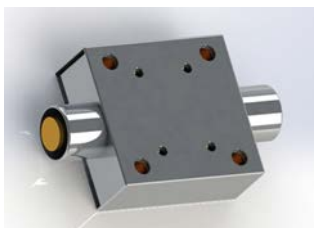
# Current Setup



## Current Setup

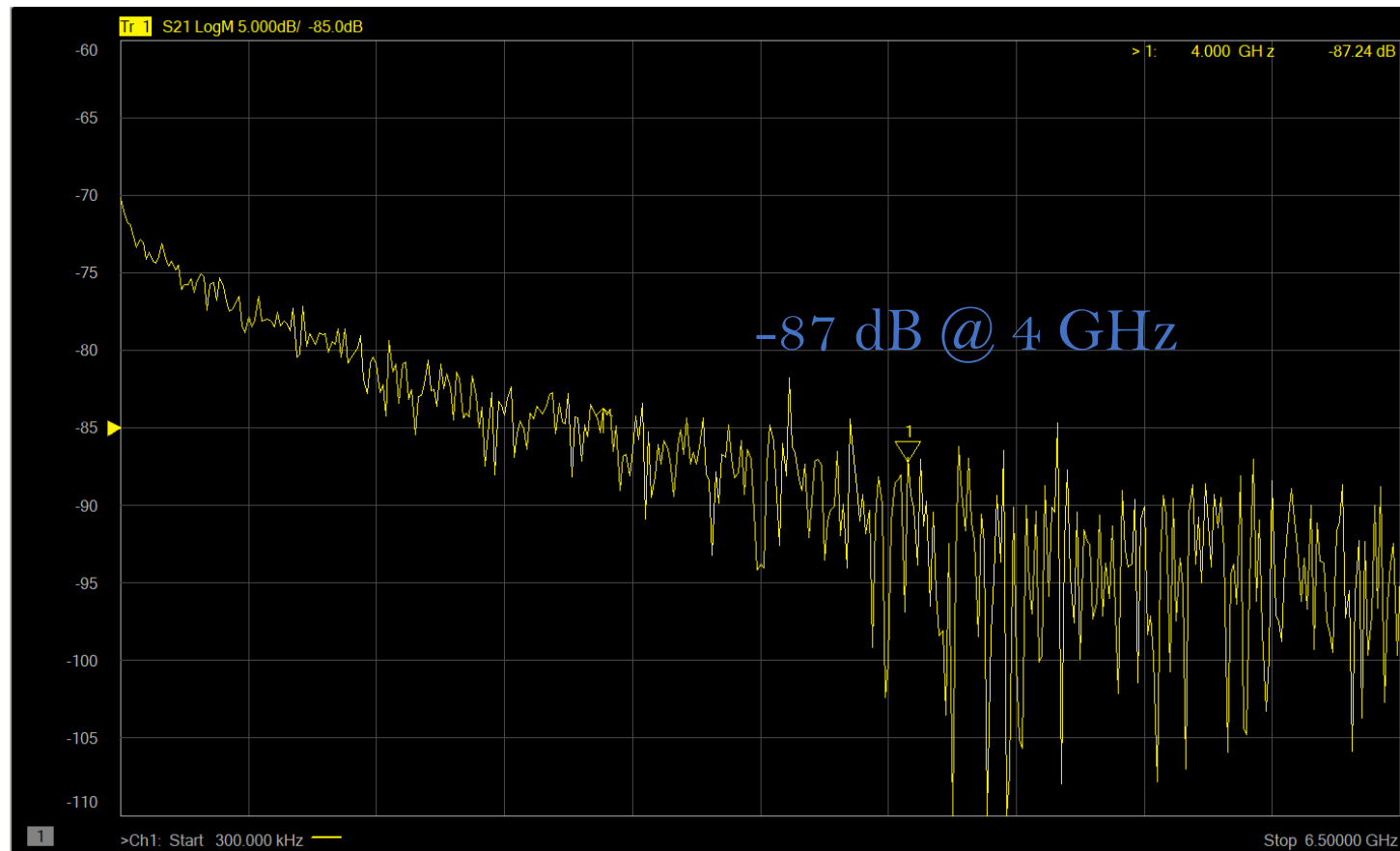


# Current Setup



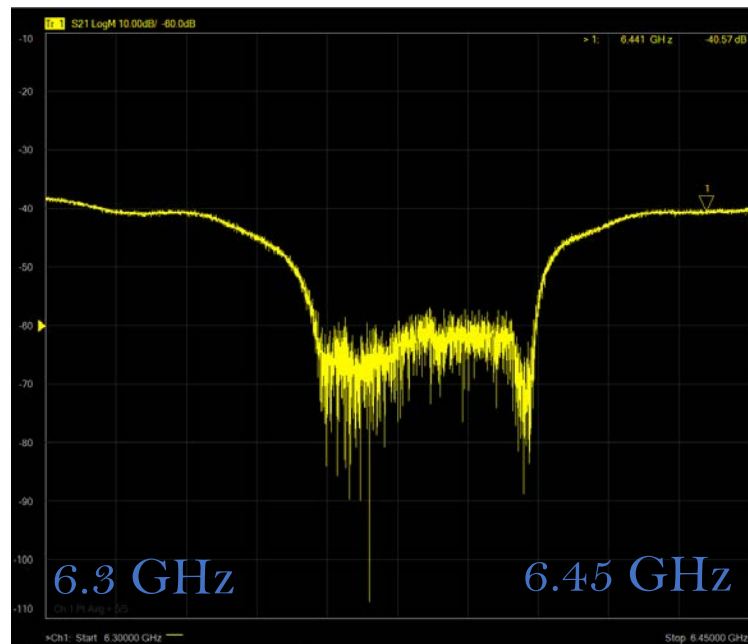
# Room temperature calibration

apply cryogenic switches in the future for better comparison



# Characterization of TWPA

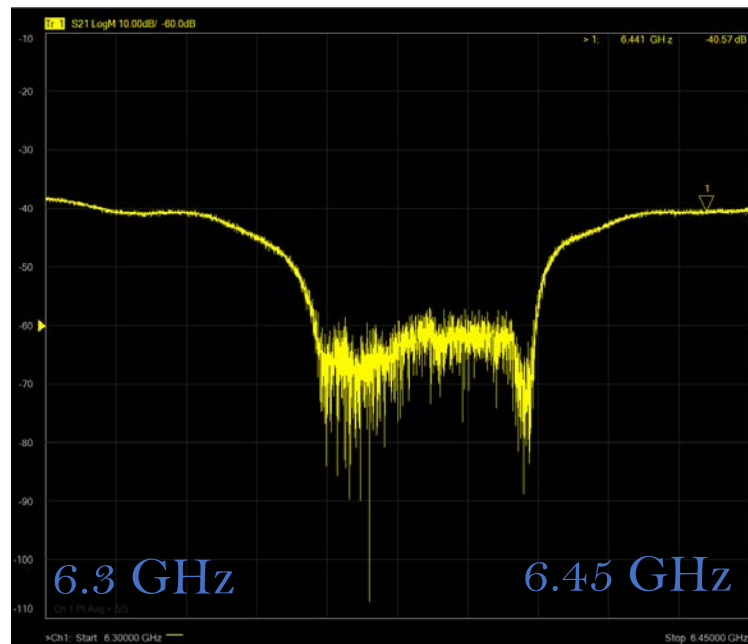
Without shield



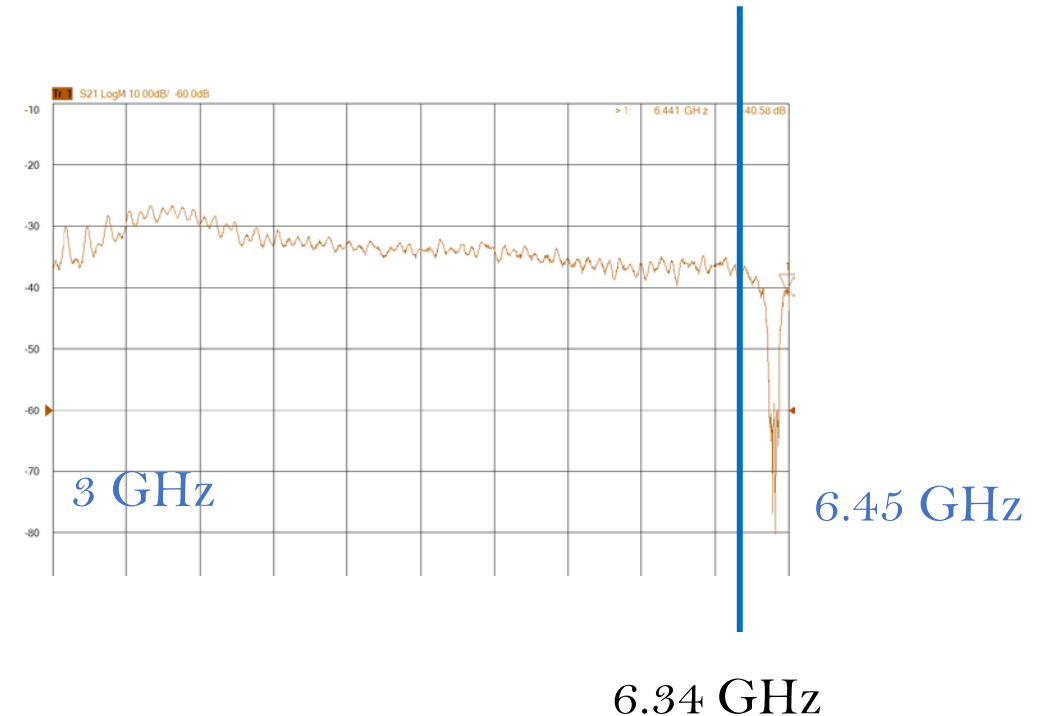
Dispersive feature

# Characterization of TWPA

Without shield

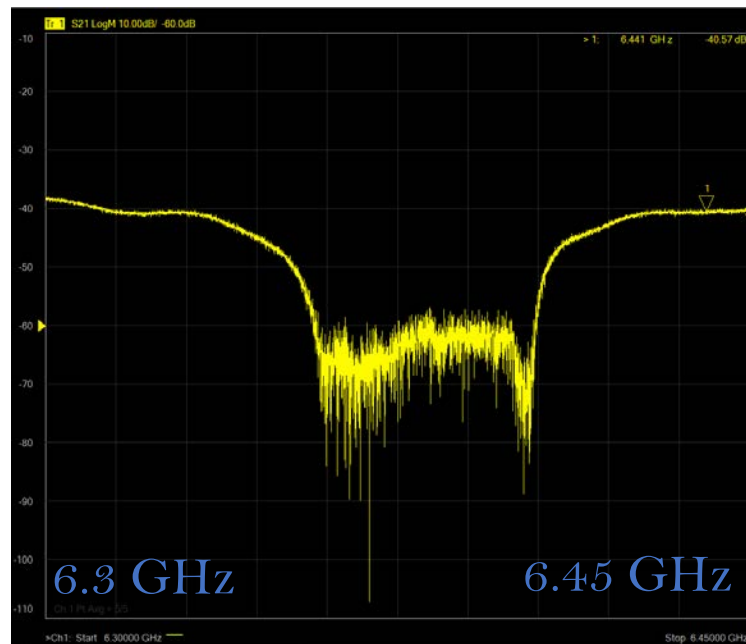
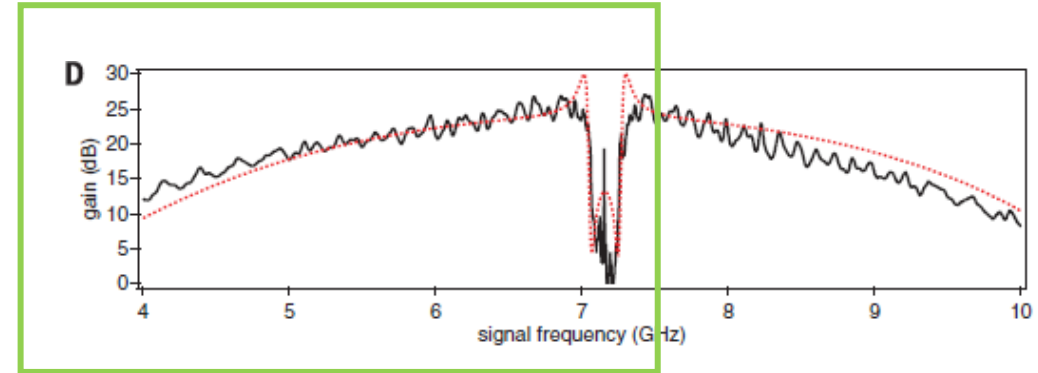


Dispersive feature

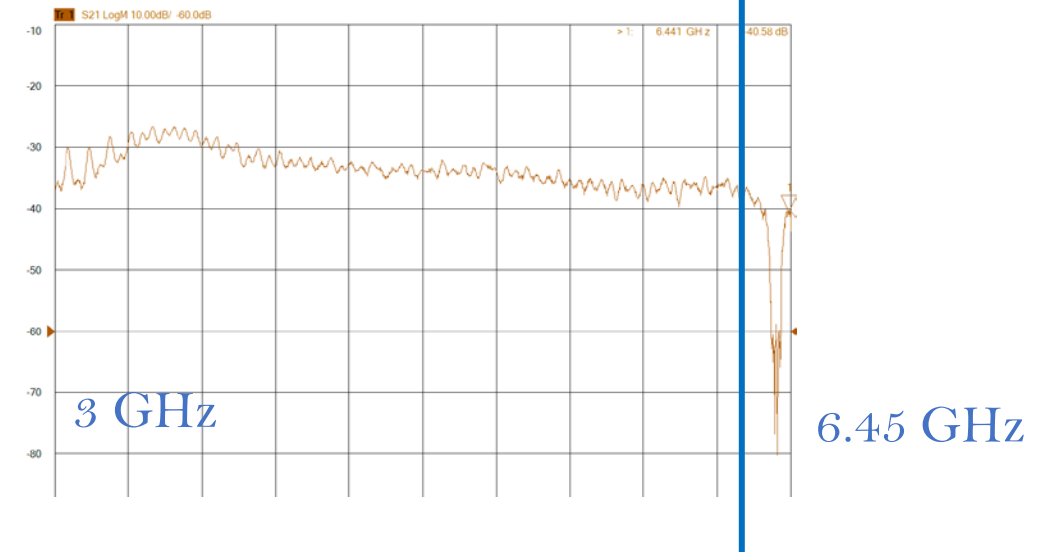


# Characterization of TWPA

Without shield



Dispersive feature



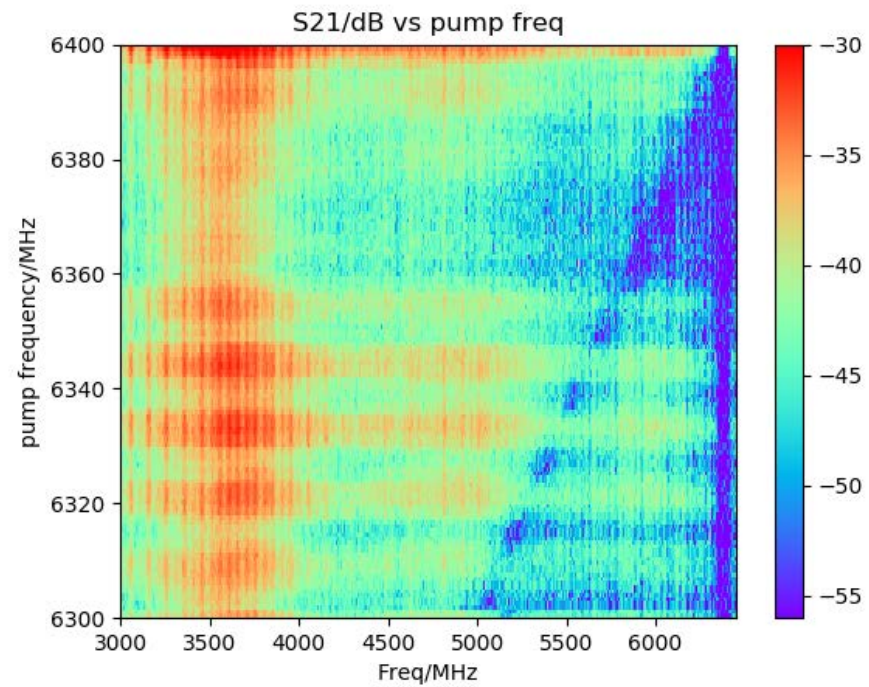
6.34 GHz



Pump frequency/power search

# Pump frequency/power search

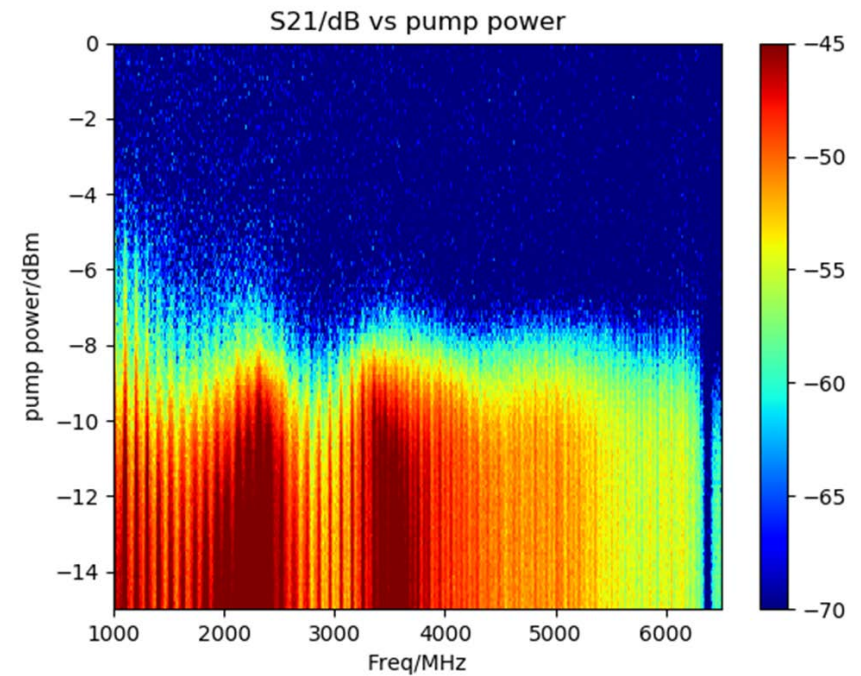
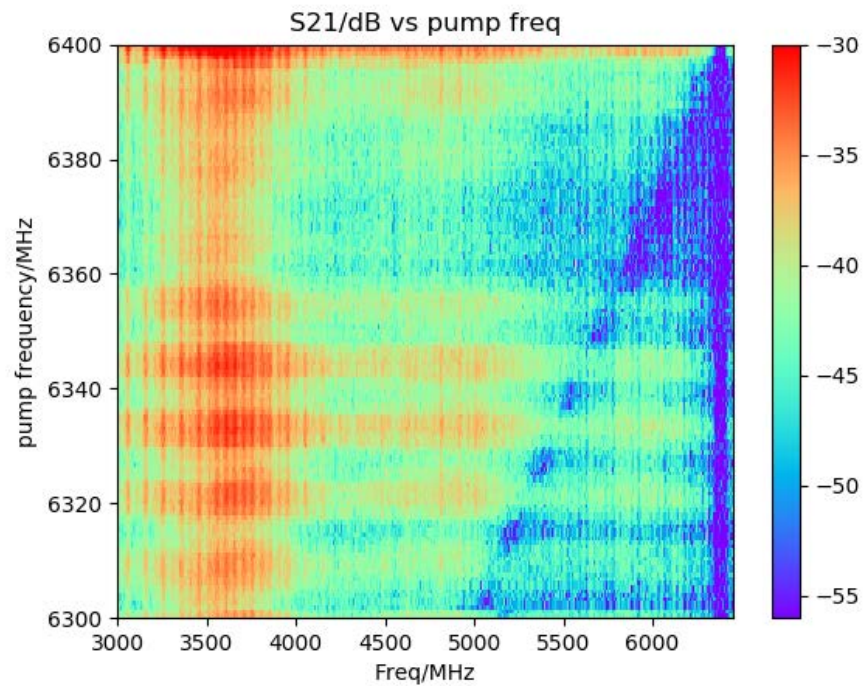
Sweep pump frequency from 5 GHz to 6.4 GHz in 10 MHz step, pump power -14 dBm



# Pump frequency/power search

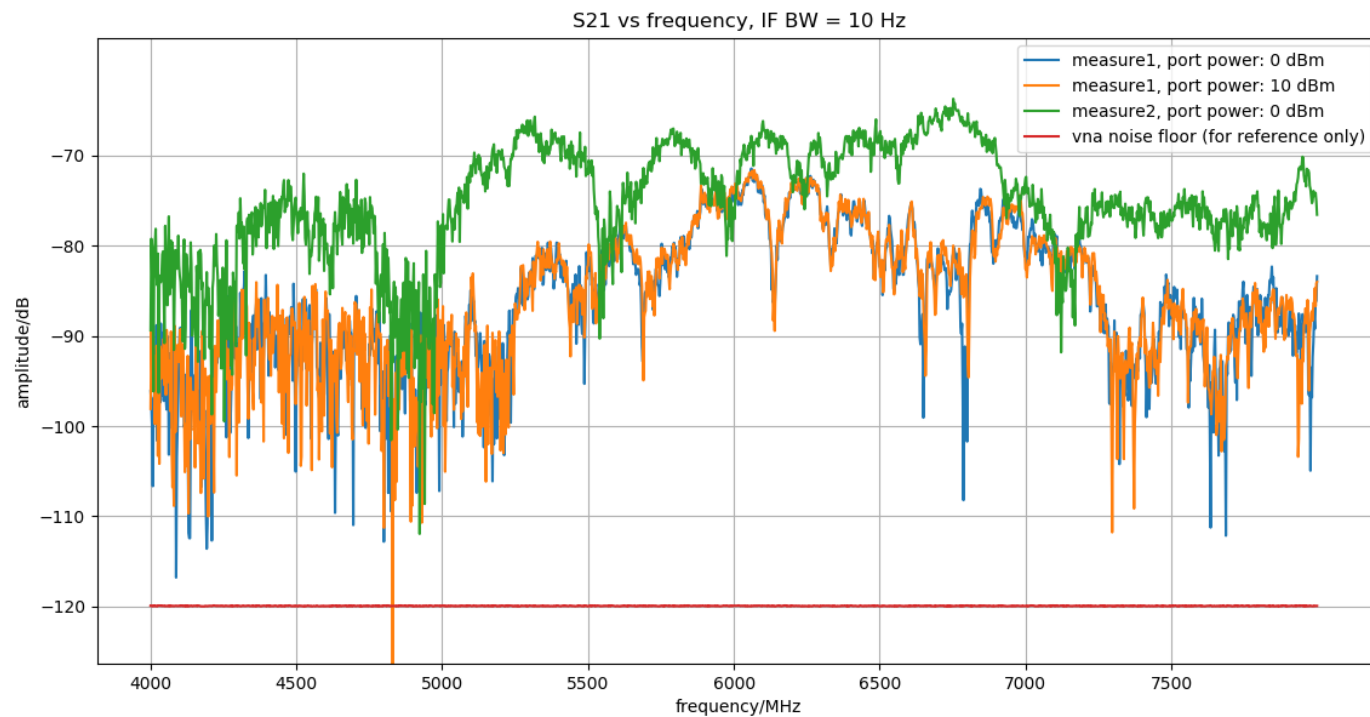
Sweep pump frequency from 5 GHz to 6.4 GHz in 10 MHz step, pump power -14 dBm

Sweep pump power from -15 dBm to 0 dBm in 0.1 dB step



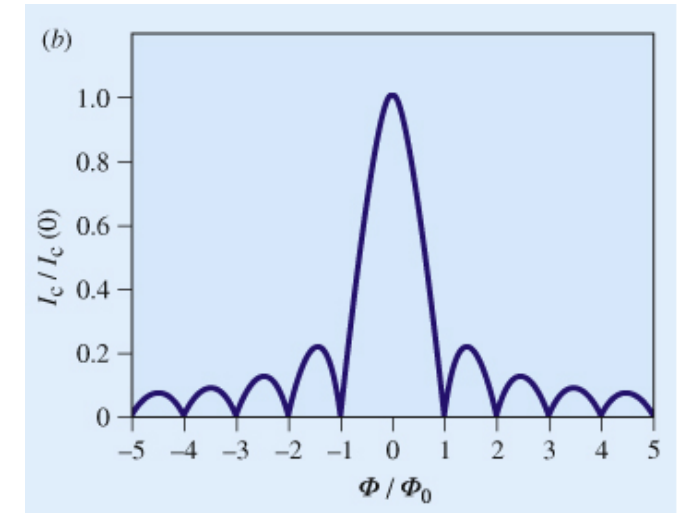
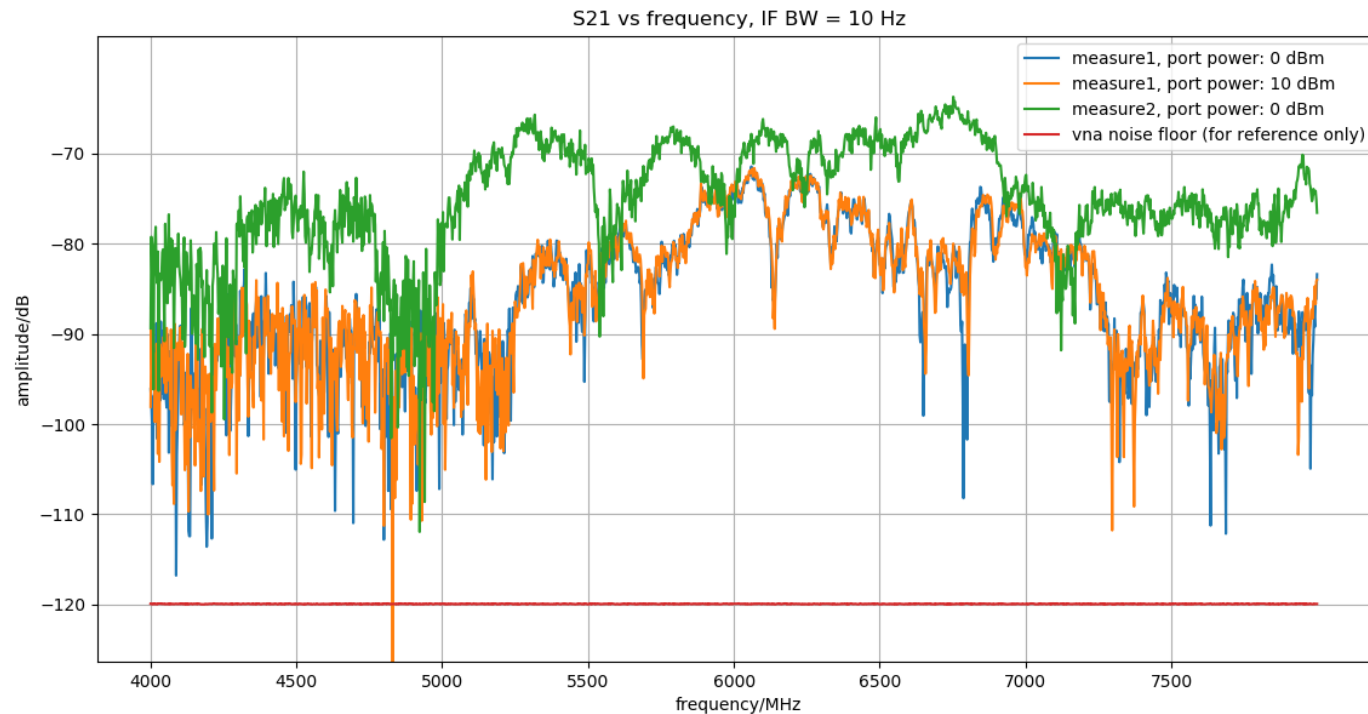
# Weird behavior without shield

Without shield, with circulator



# Weird behavior without shield

Without shield, with circulator



Critical current vs magnetic flux

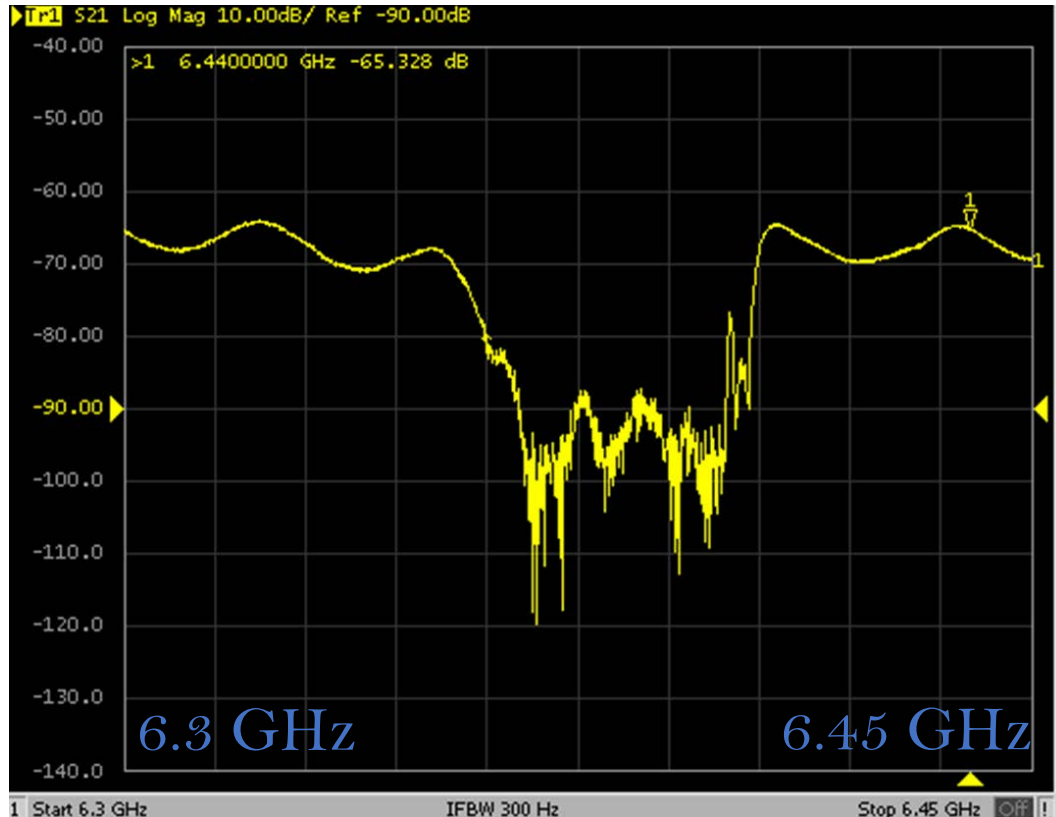
*The Josephson effect: 50 years of science and technology. Paul A Warburton*

# Characterization of TWPA

With magnetic shield, without circulator

# Characterization of TWPA

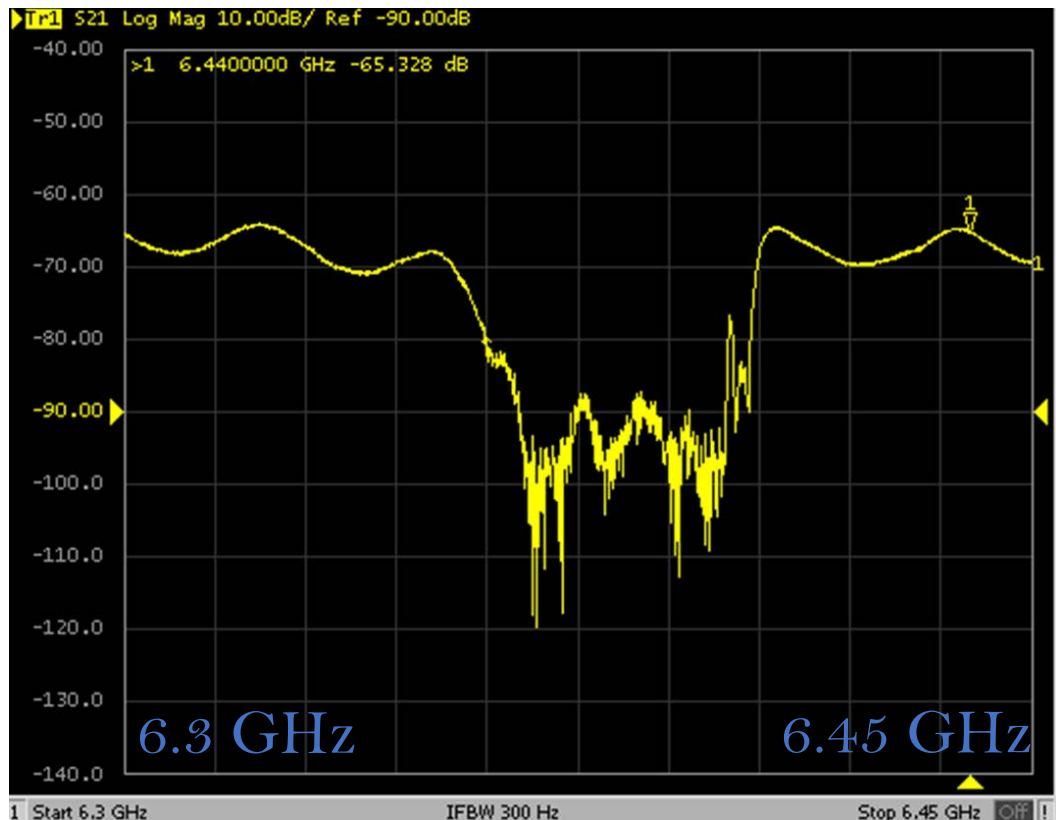
With magnetic shield, without circulator



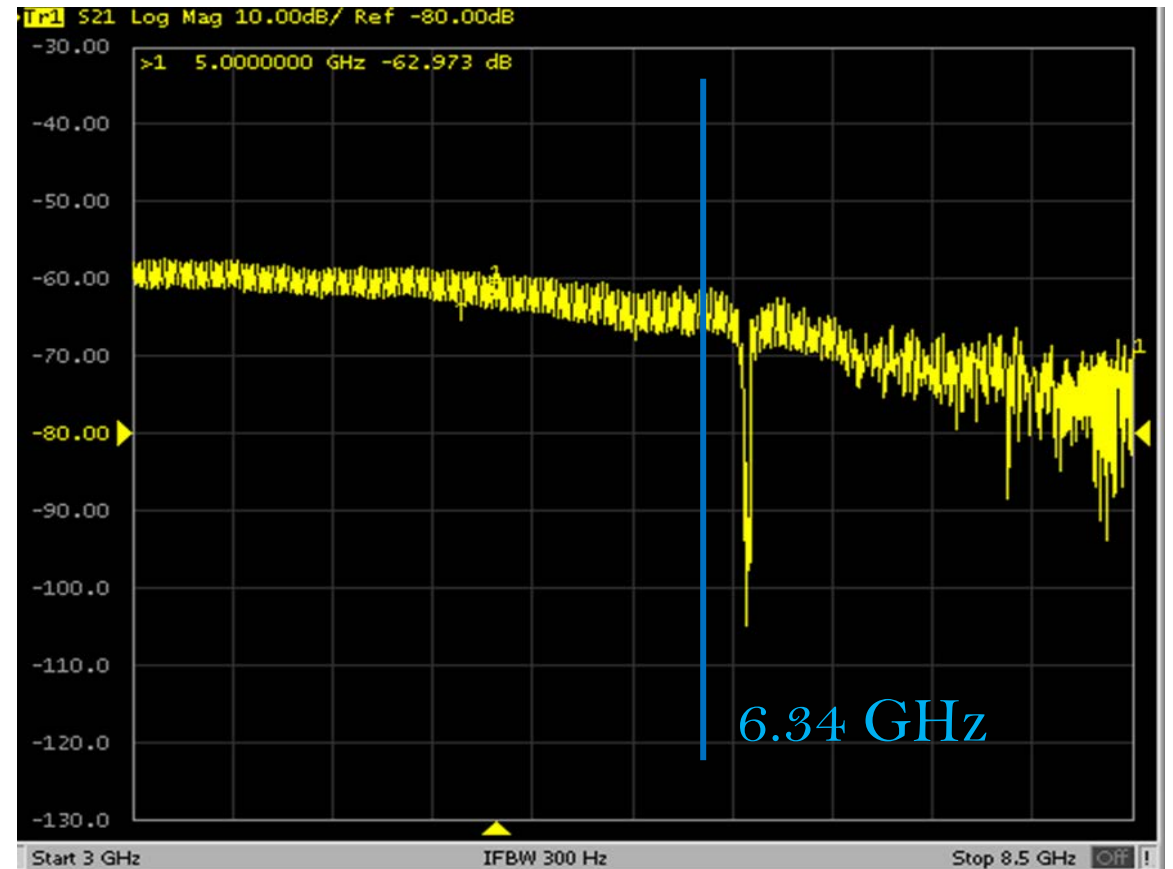
Dispersive feature

# Characterization of TWPA

With magnetic shield, without circulator



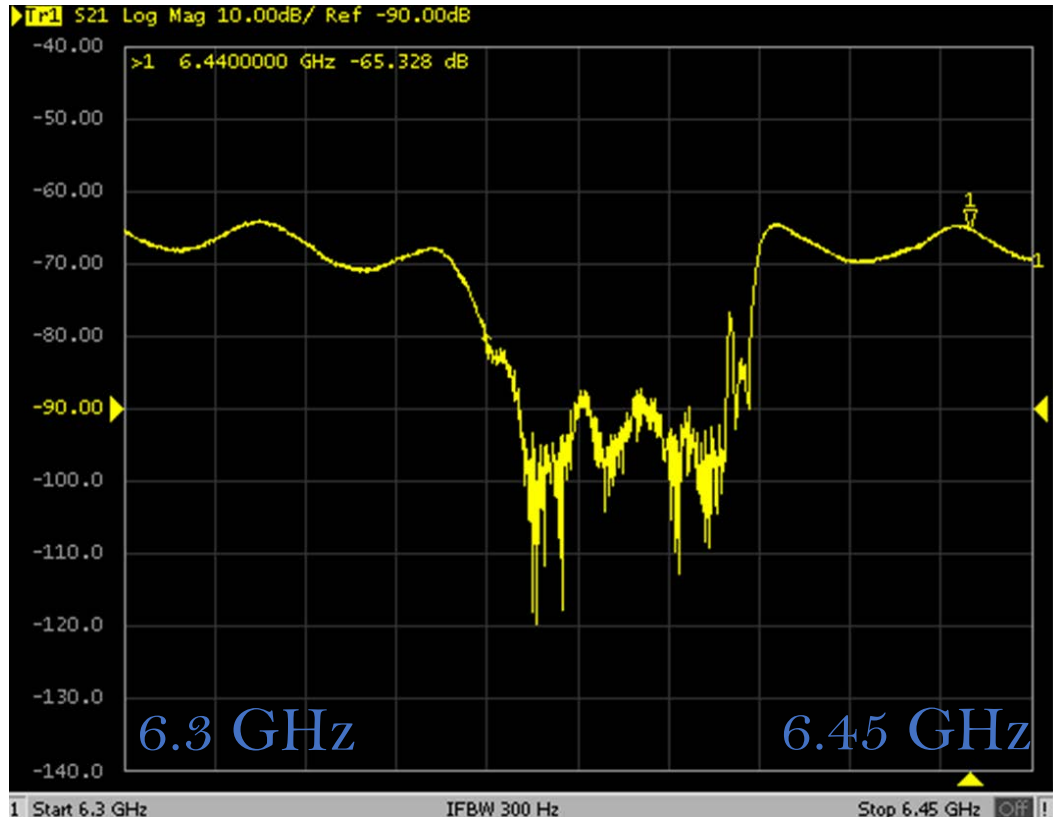
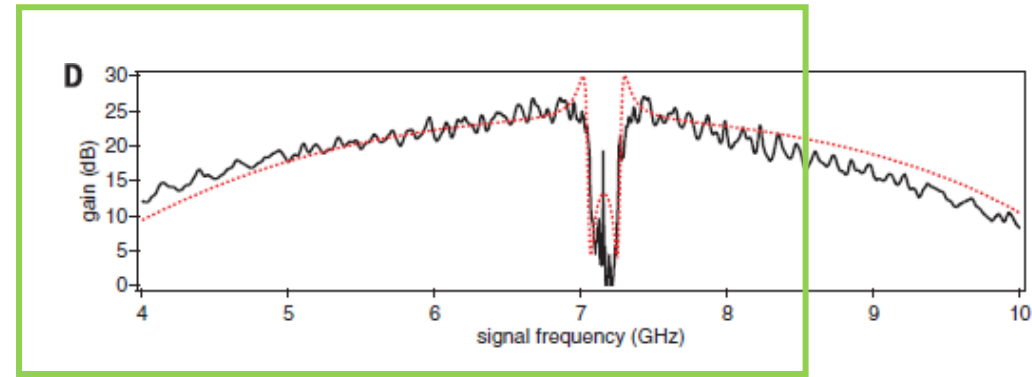
Dispersive feature



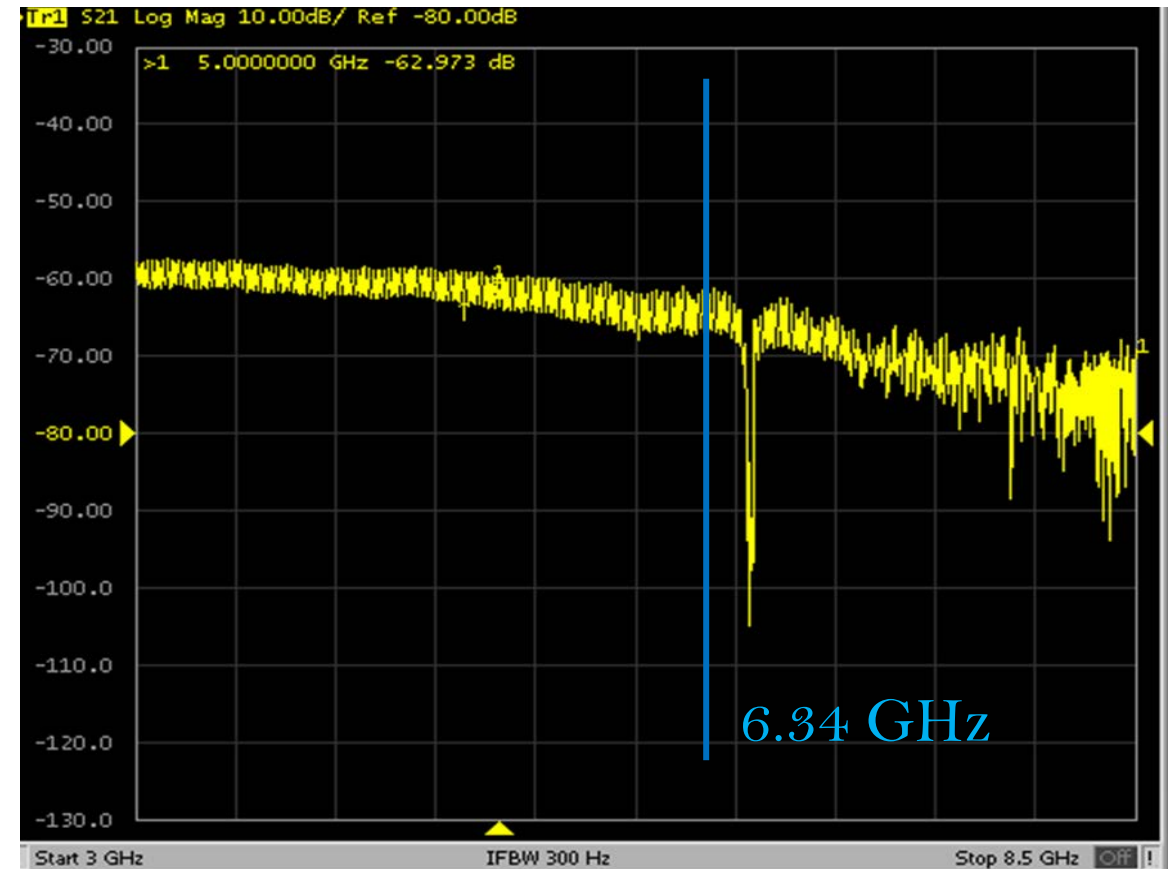


# Characterization of TWPA

With magnetic shield, without circulator



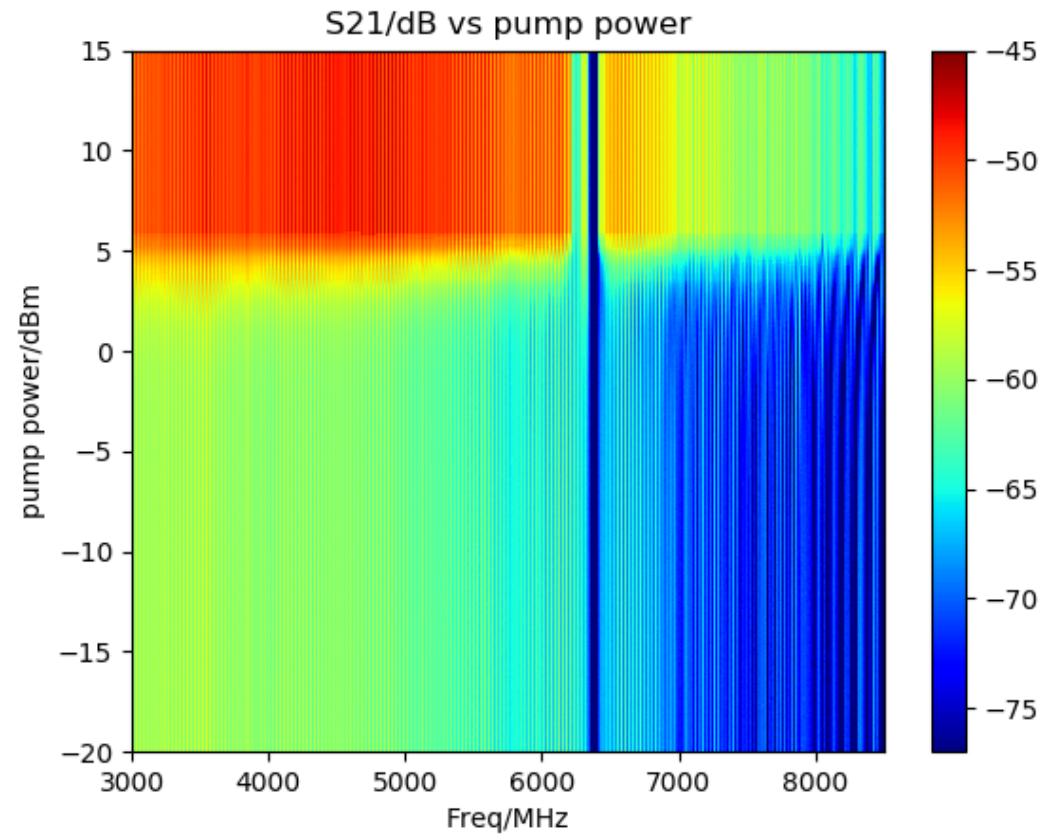
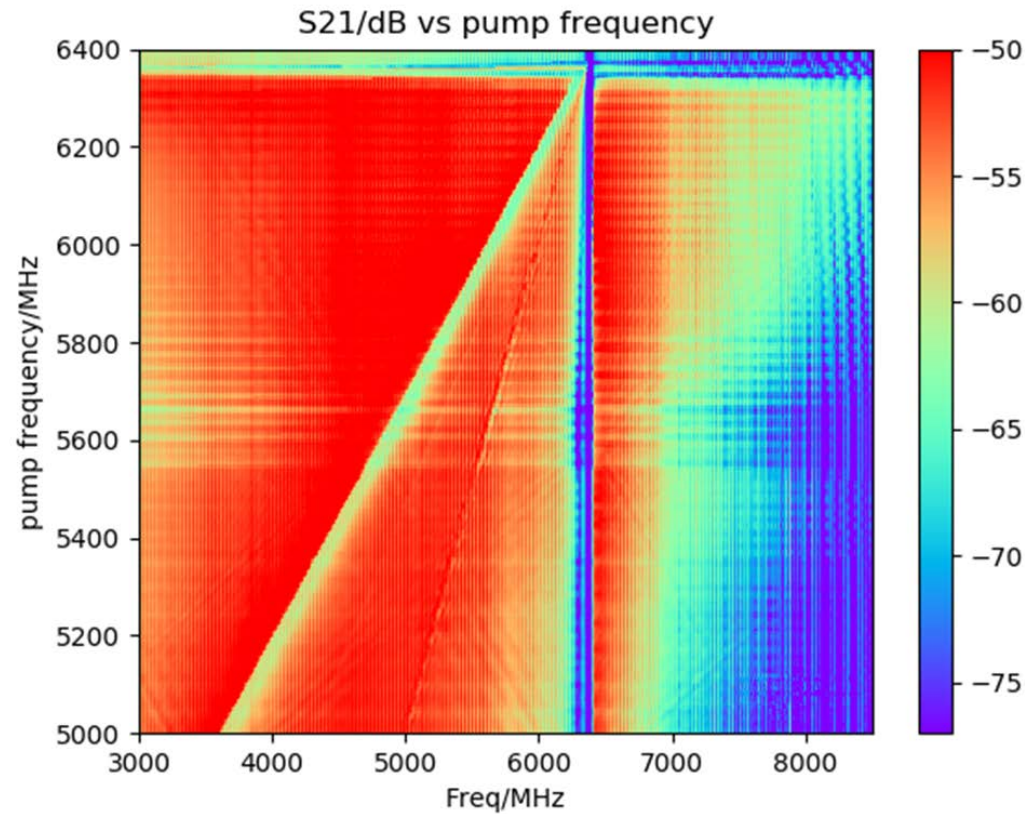
Dispersive feature



# Pump frequency/power search (port power: 0 dBm)

Sweep pump frequency from 5 GHz to 6.4 GHz in 1 MHz step, pump power 7.5 dBm

Sweep pump power from -20 dBm to 15 dBm in 0.1 dB step (@6.31 GHz)

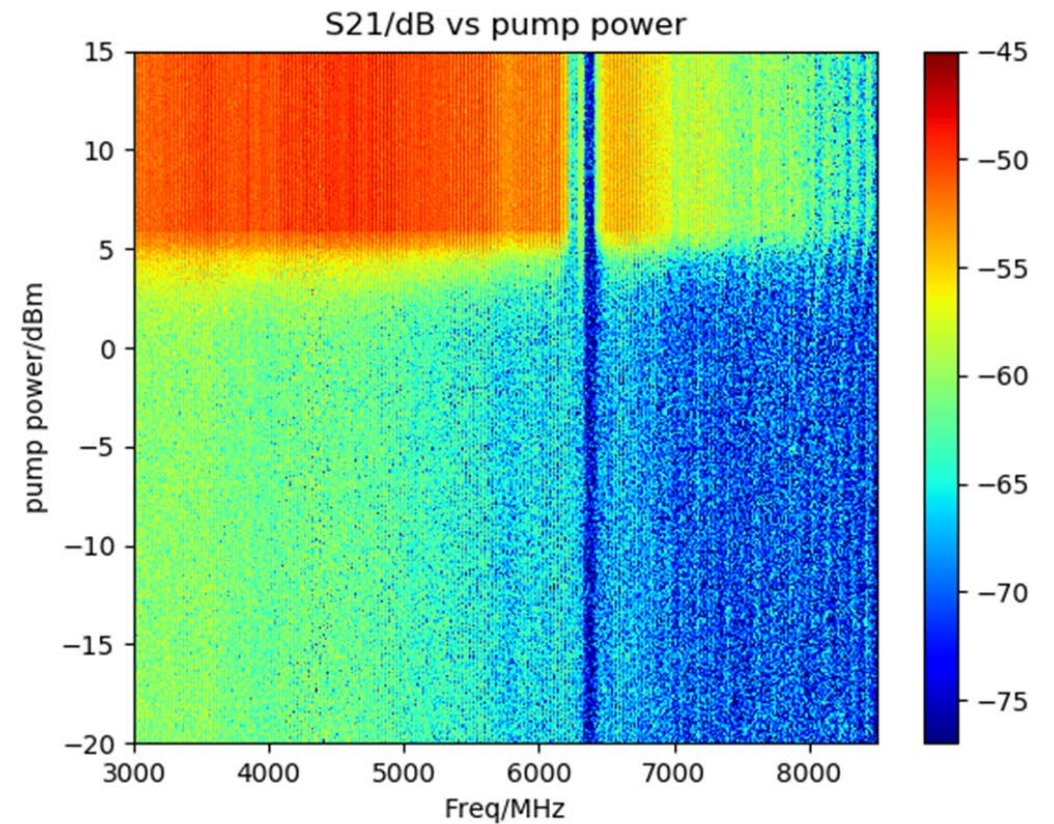
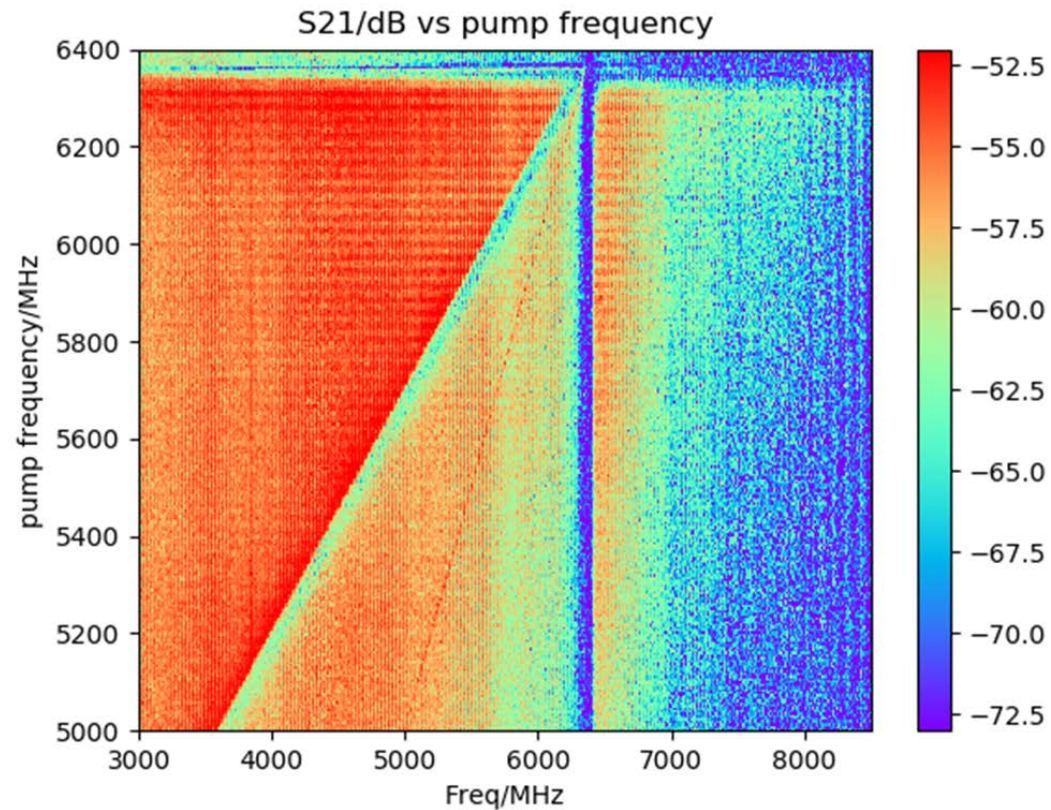




# Pump frequency/power search (port power: -30 dBm)

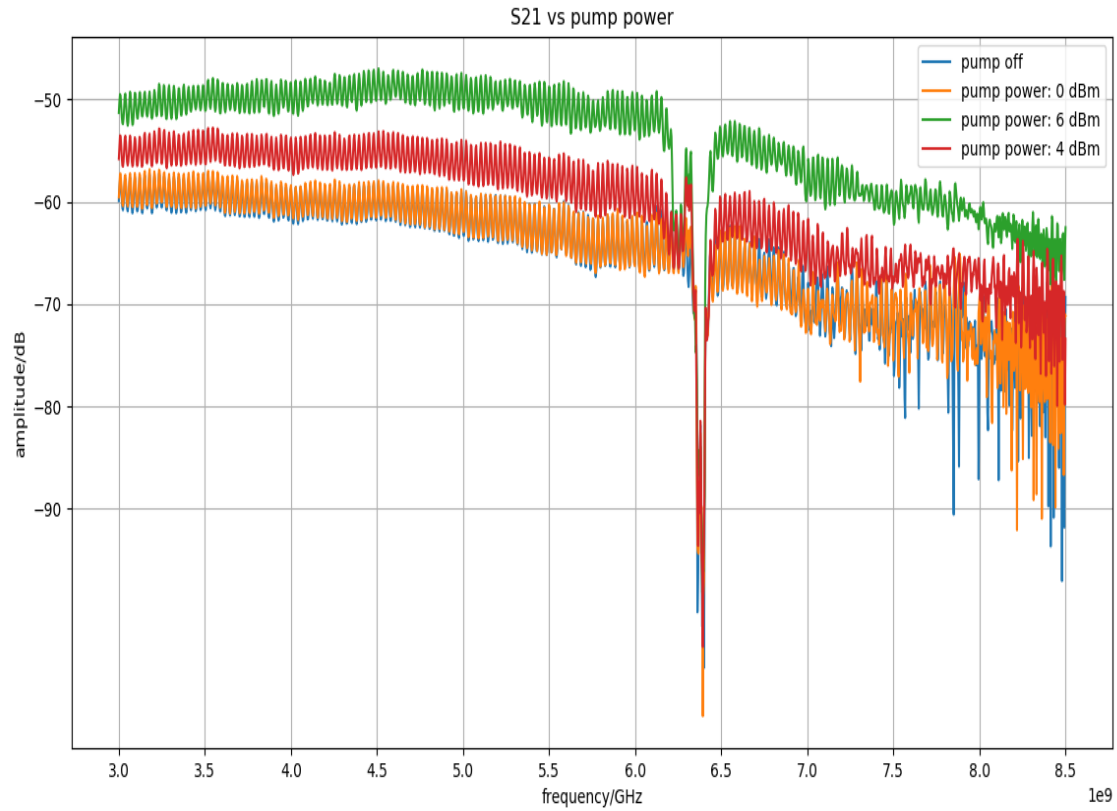
Sweep pump frequency from 5 GHz to 6.4 GHz in 1 MHz step, pump power 5 dBm

Sweep pump power from -20 dBm to 15 dBm in 0.1 dB step @6.31 GHz



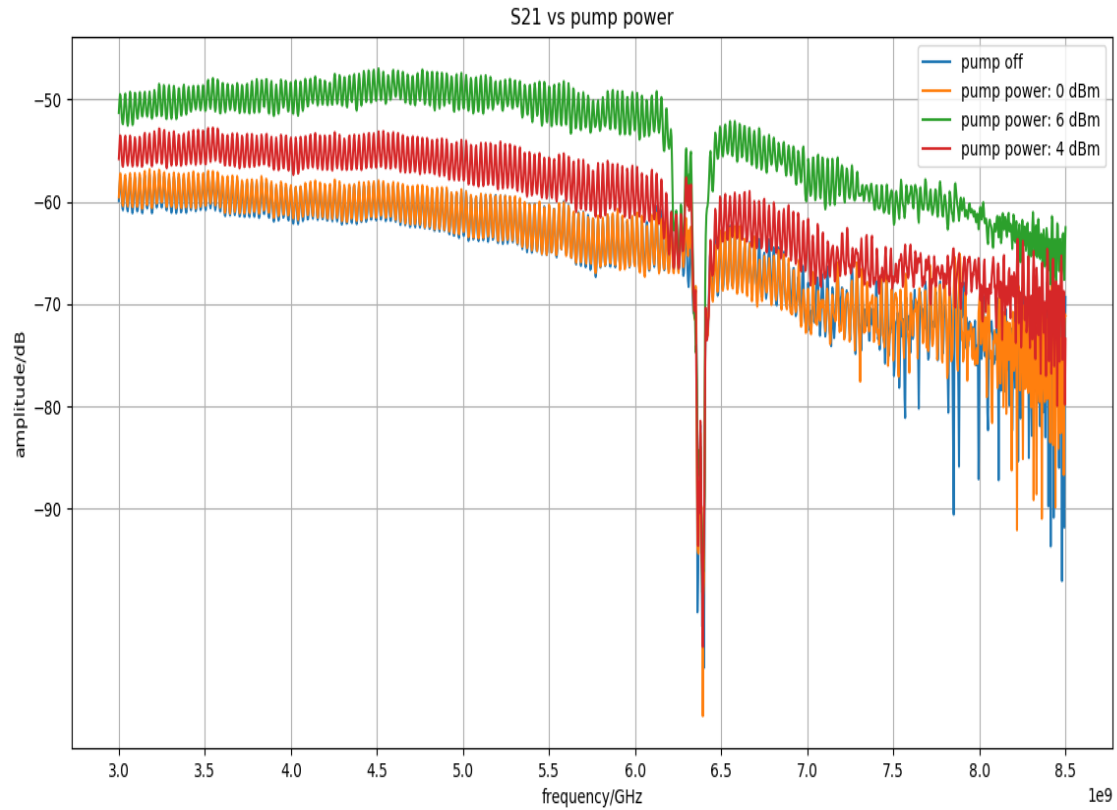
# Pump power linecut

Port power: 0 dBm

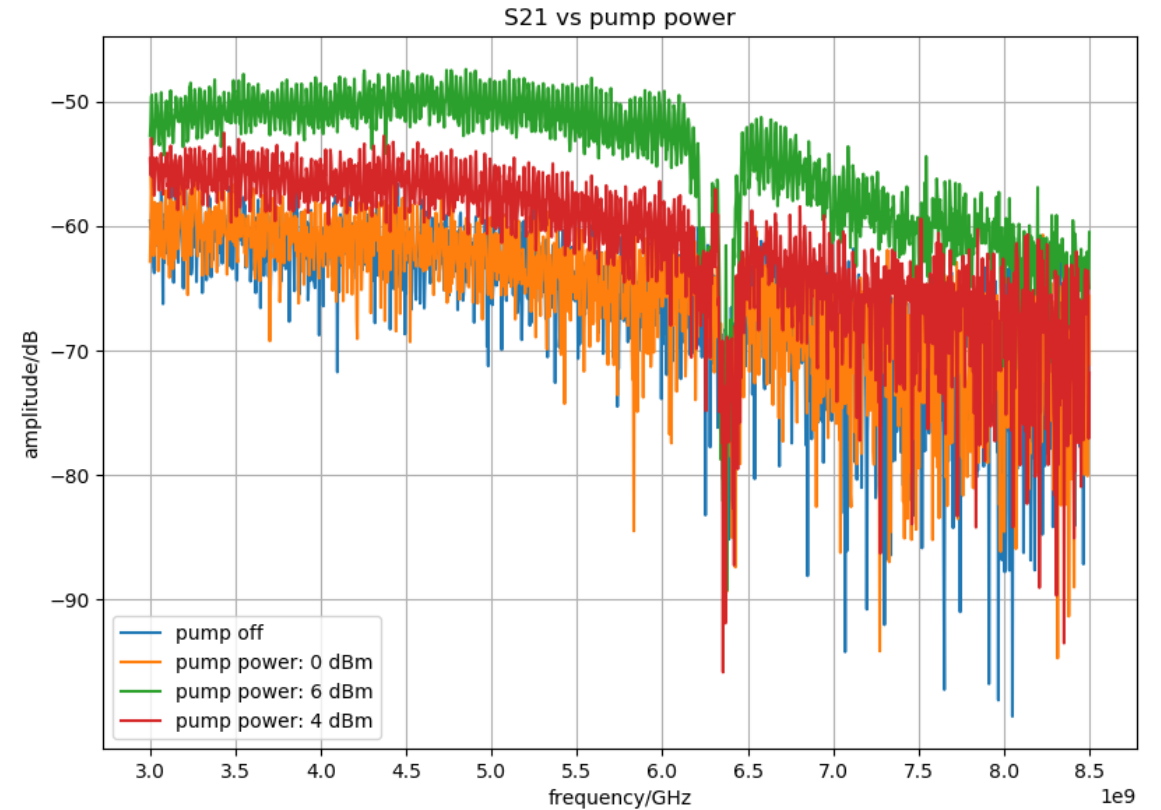


# Pump power linecut

Port power: 0 dBm



Port power: -30 dBm

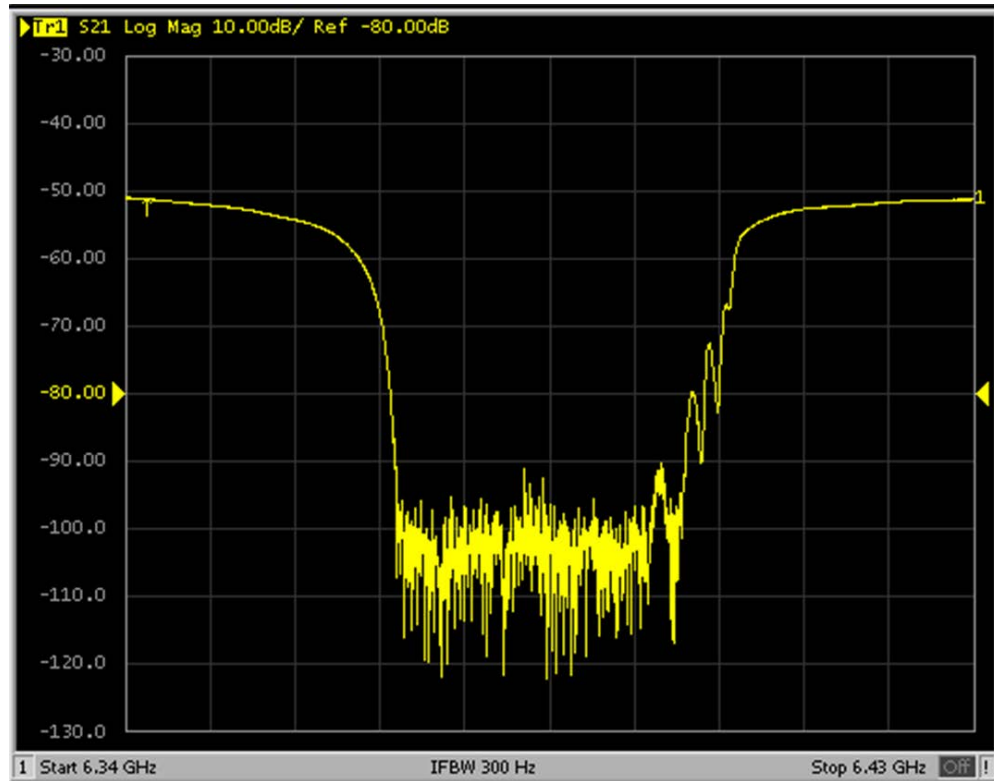
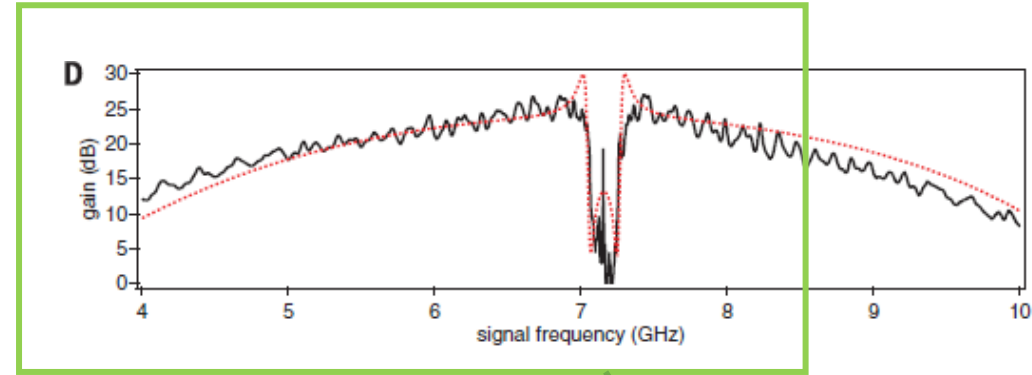


# Characterization of TWPA

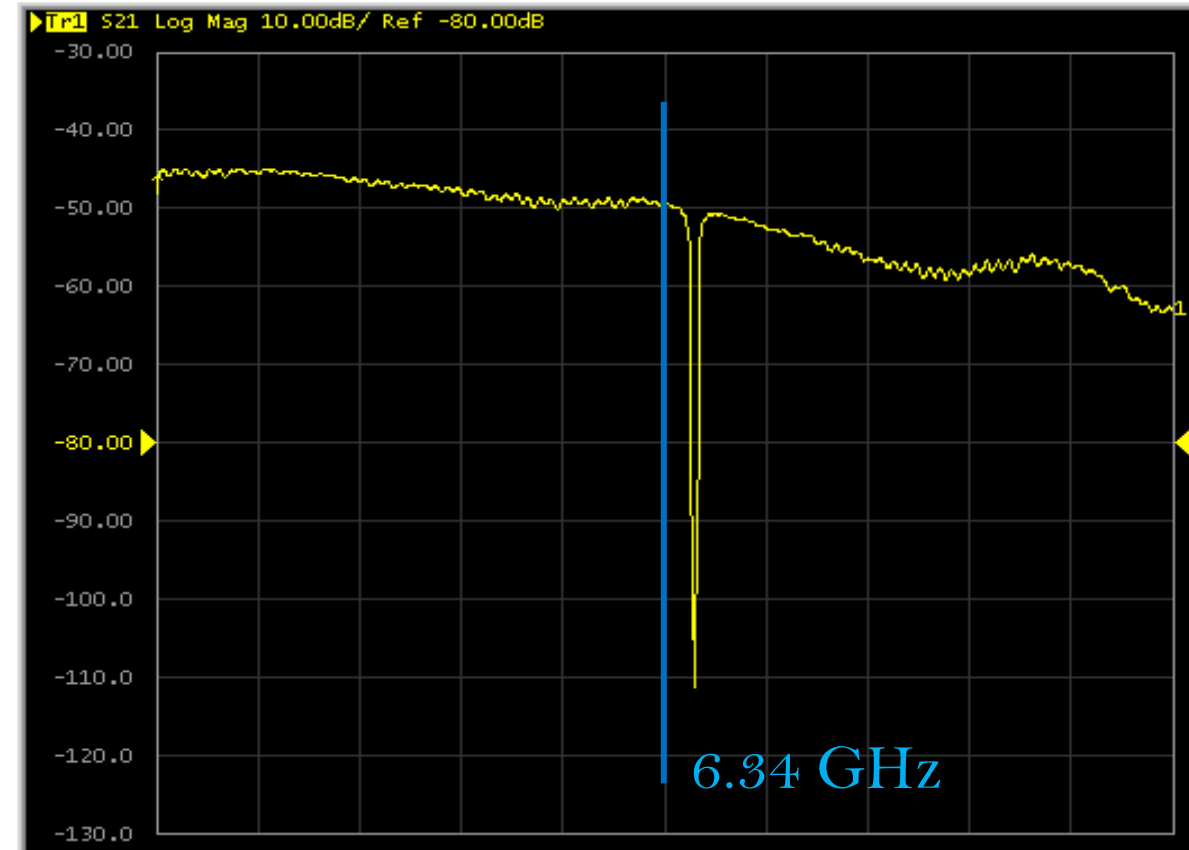
With magnetic shield, with circulator

# Characterization of TWPA

With magnetic shield, with circulator



Dispersive feature



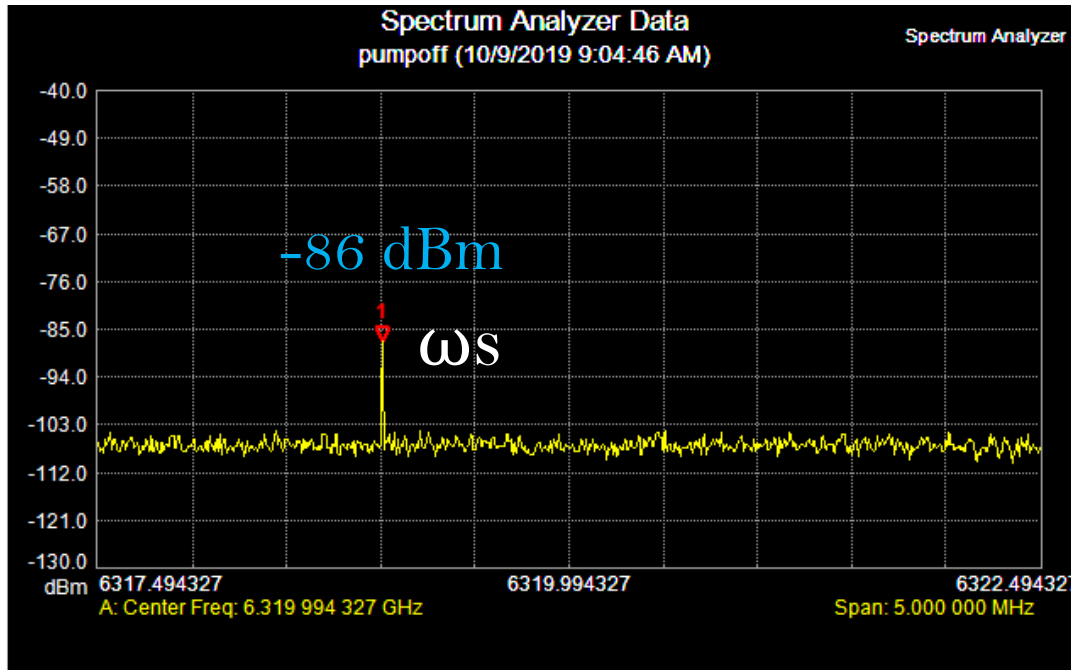
signal and idler

Four wave mixing:  $\omega_i = 2\omega_p - \omega_s$



signal and idler

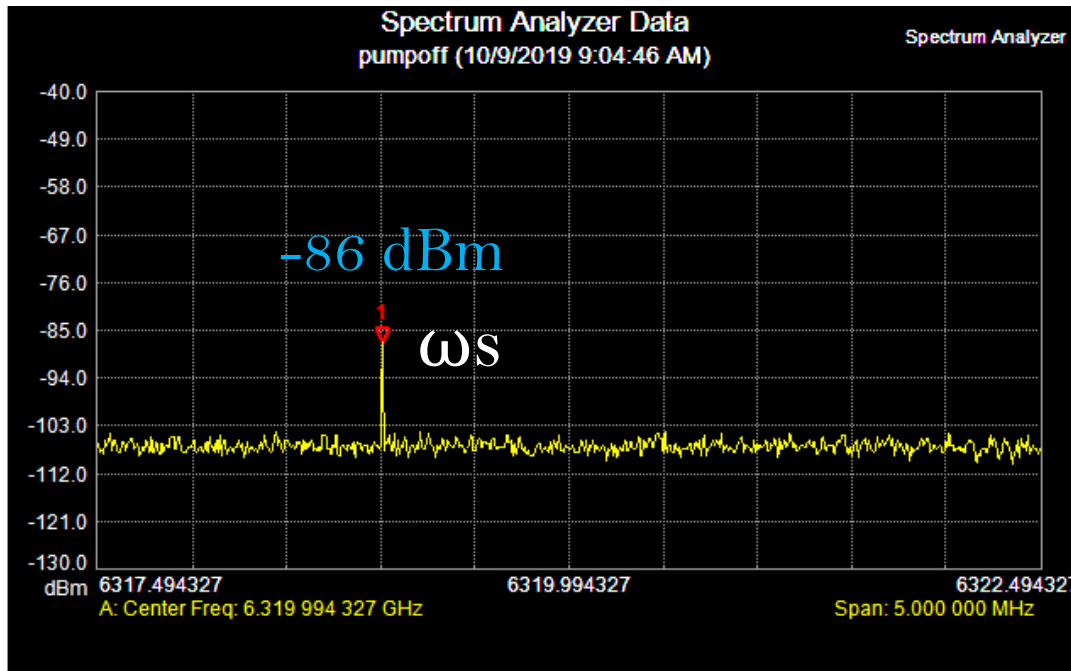
Four wave mixing:  $\omega_i = 2\omega_p - \omega_s$



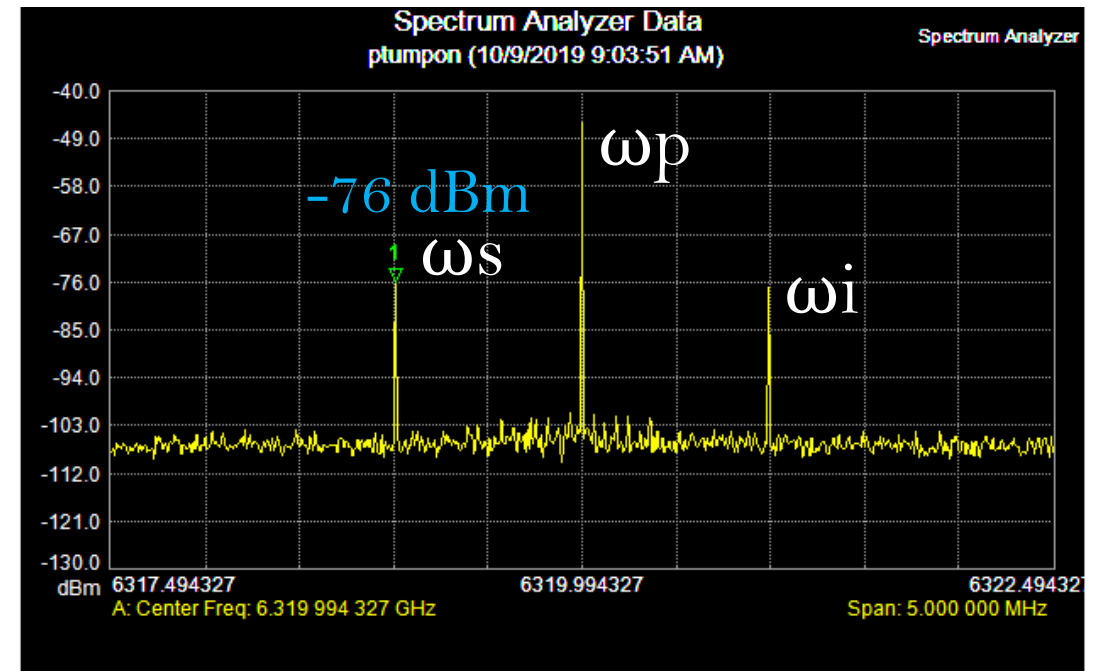
Pump off

# signal and idler

Four wave mixing:  $\omega_i = 2\omega_p - \omega_s$



Pump off

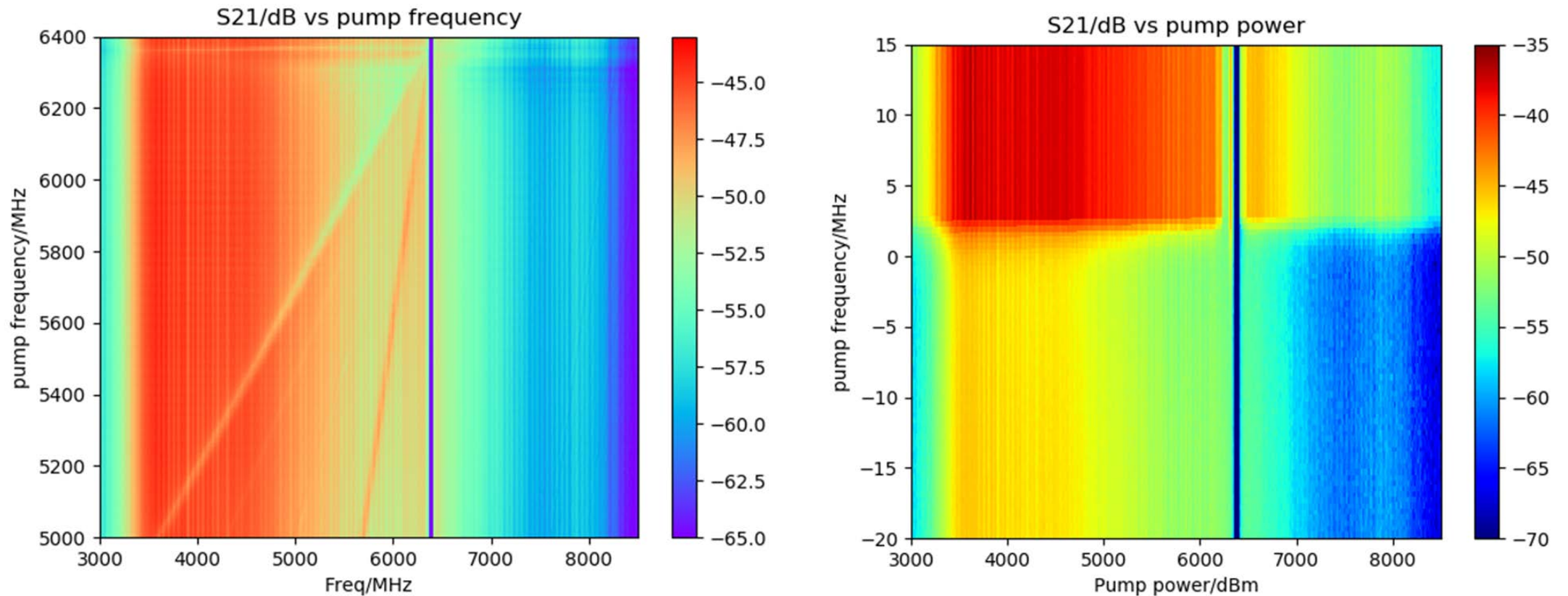


Pump on

# Pump frequency/power search (port power: 0 dBm)

Sweep pump frequency from 5 GHz to 6.4 GHz in 1 MHz step, pump power 0 dBm

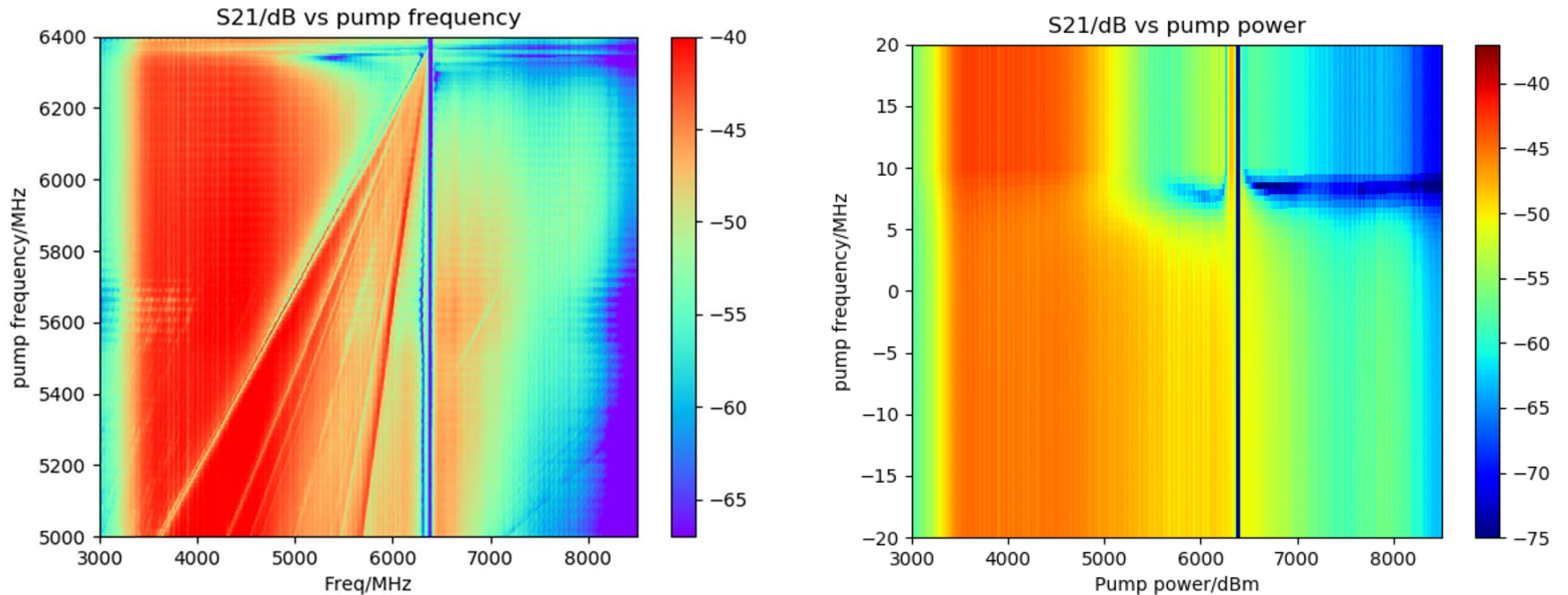
Sweep pump power from -20 dBm to 15 dBm in 0.1 dB step @6.31 GHz



# Pump frequency/power search (port power: 0 dBm)

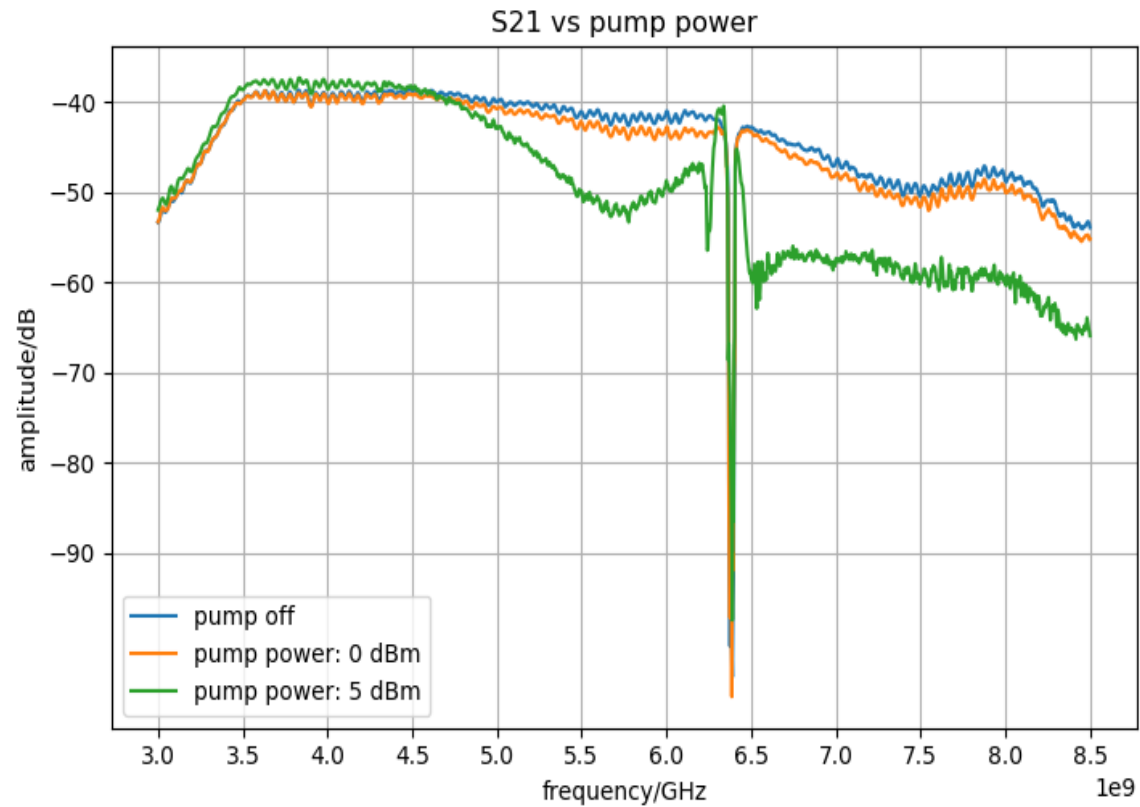
Sweep pump frequency from 5 GHz to 6.4 GHz in 1 MHz step, pump power 7.5 dBm

Sweep pump power from -20 dBm to 15 dBm in 0.1 dB step @6.31 GHz

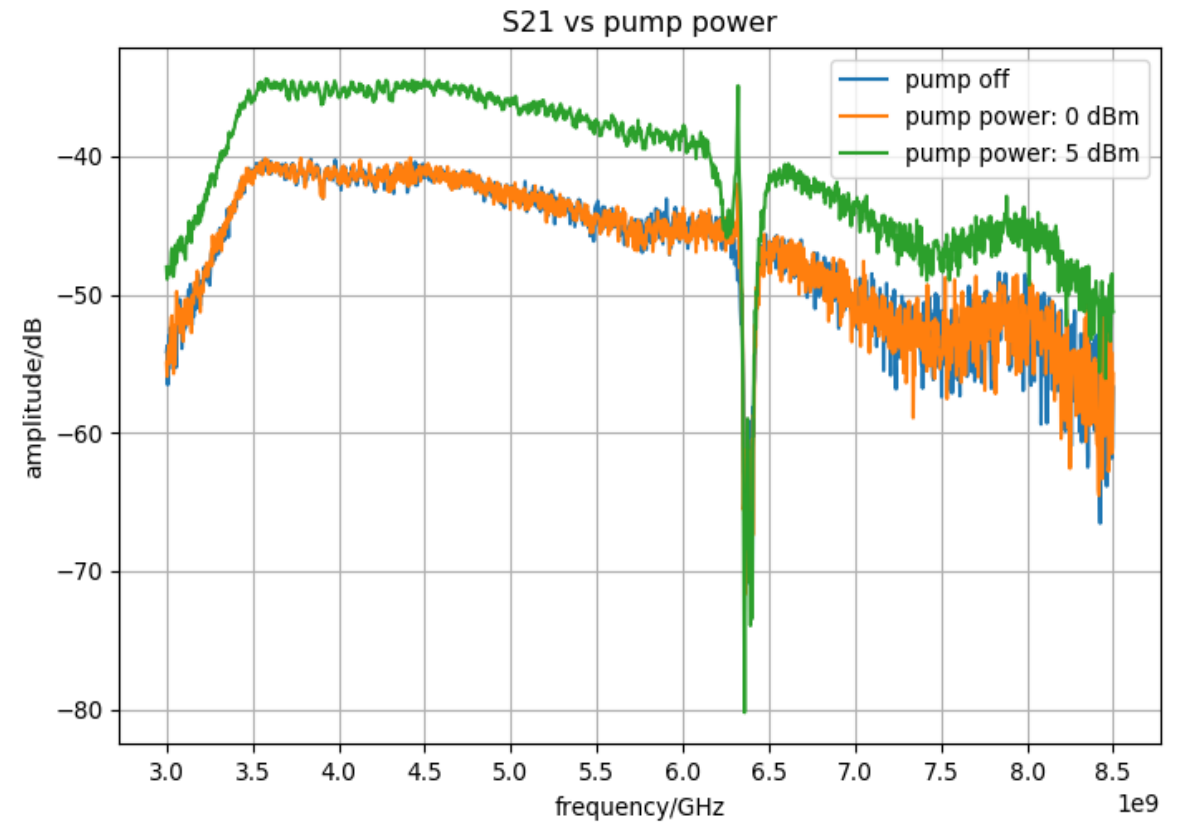


# Pump power linecut

Port power: 0 dBm

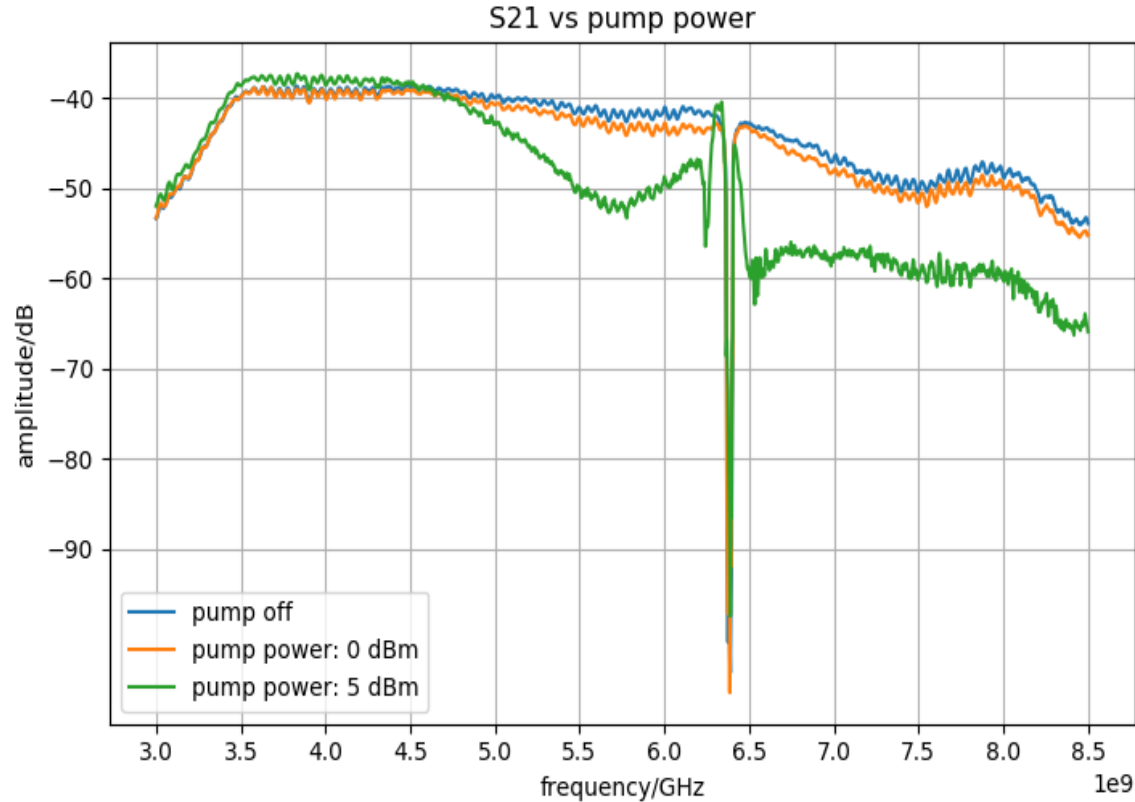


Port power: -30 dBm

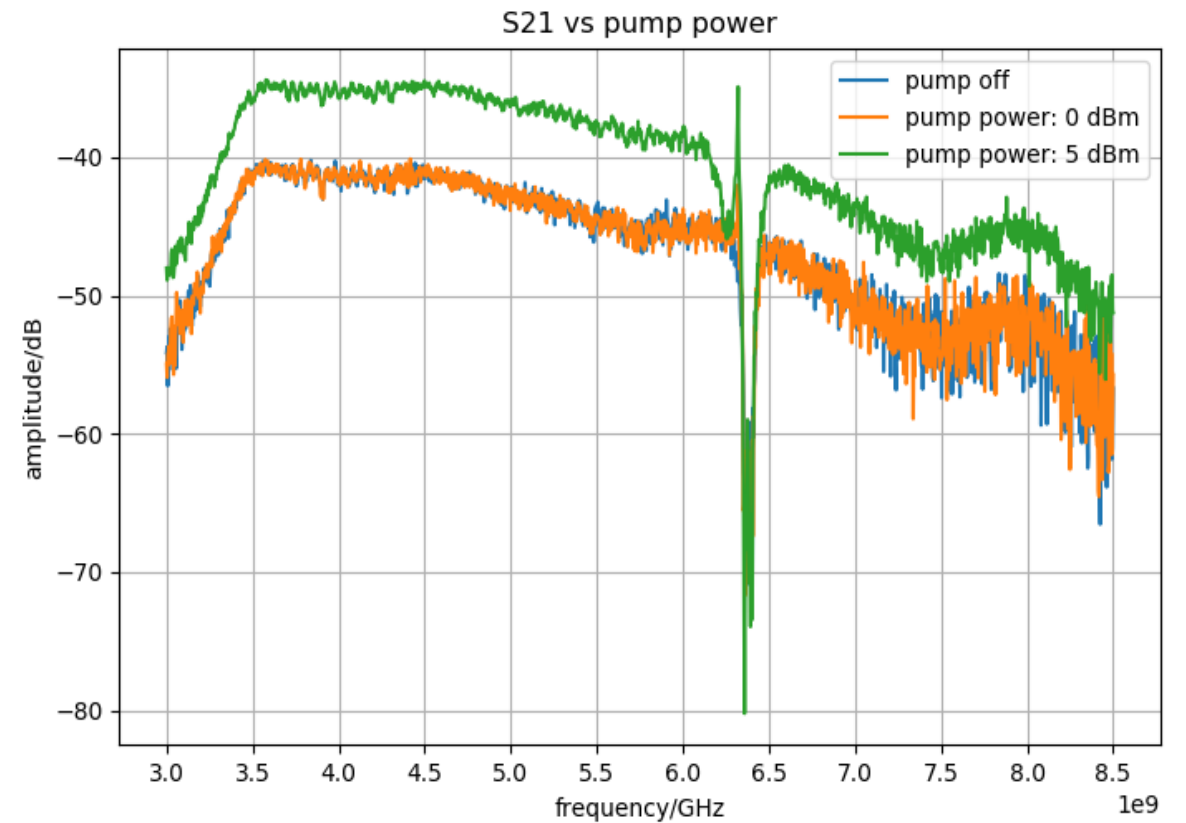


# Pump power linecut

Port power: 0 dBm



Port power: -30 dBm



Leakage of pump power into higher harmonics, which may  
reduce gain  
the onset of a shock wave

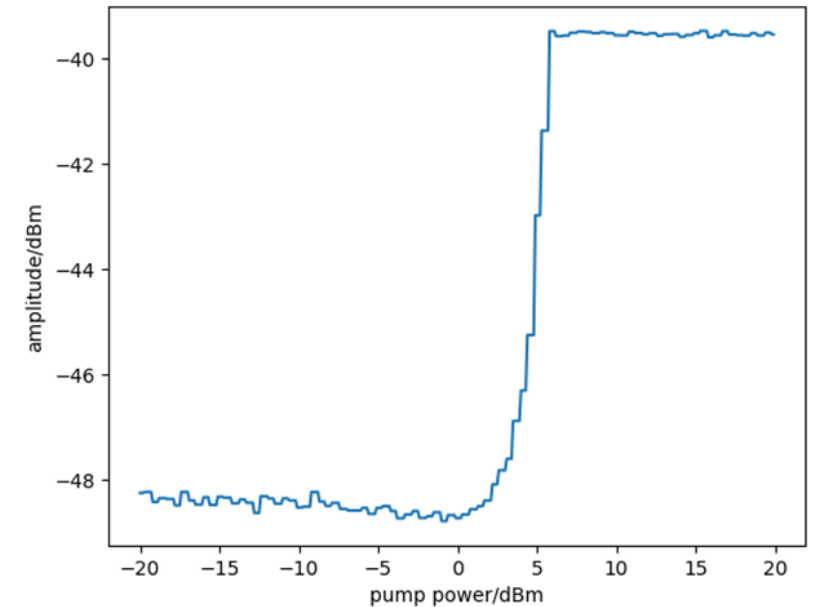


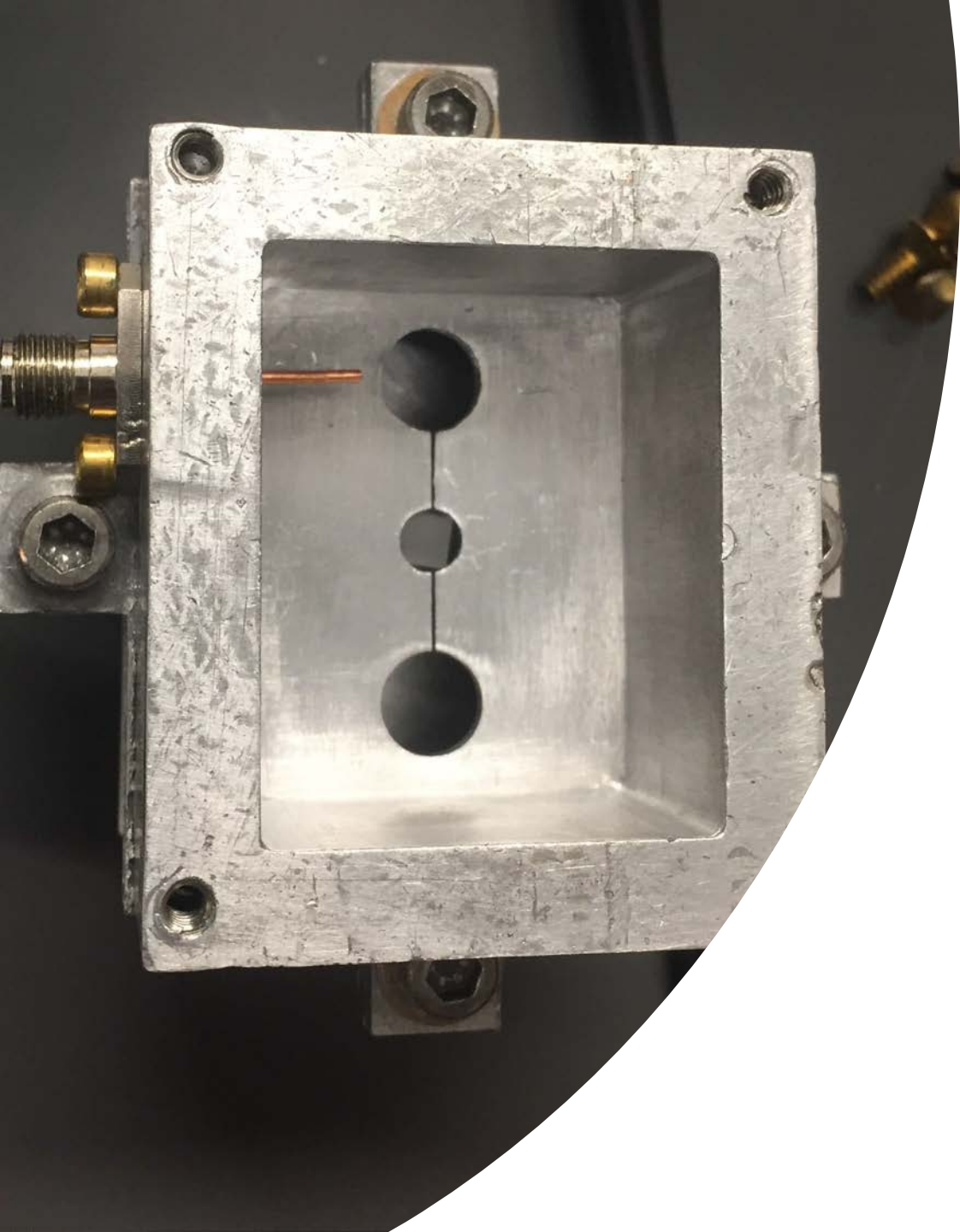




# Conclusion

- We could have a signal gain of 10 dB with -75 dBm, 6.31 GHz pump on chip
- Might exist saturation of room temperature amplifiers
- Even with field off, put on magnetic shield to ensure normal operation





- Characterization of TWPA
- Enhancing sensitivity of EPR
- Setting up of HEMT

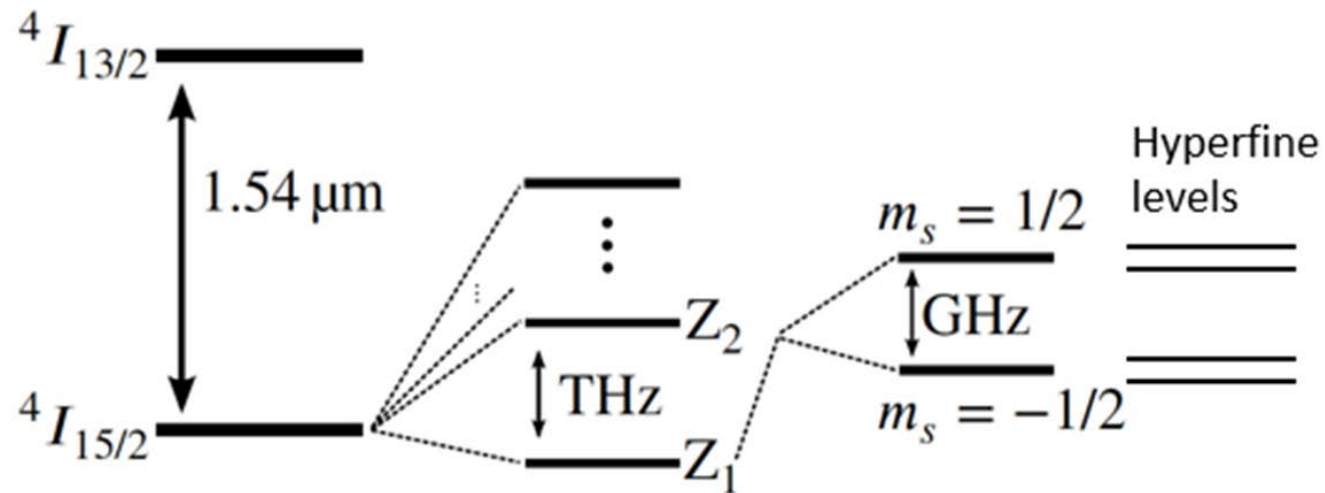
# Motivation

$\text{Er}^{+3}$ :  $\text{Y}_2\text{O}_3$  has long spin coherence time and large, anisotropic g-factor

# Motivation

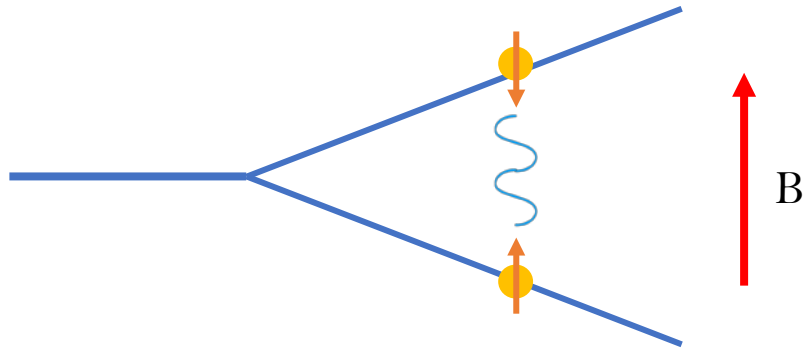
$\text{Er}^{+3}$ :  $\text{Y}_2\text{O}_3$  has **long spin coherence time** and large, anisotropic g-factor

$$\mathcal{H} = \boxed{\mu_B(B \cdot g_e \cdot S)} + S \cdot A \cdot I + I \cdot Q \cdot I - \mu_N(B \cdot g_n \cdot I)$$



# EPR working principle

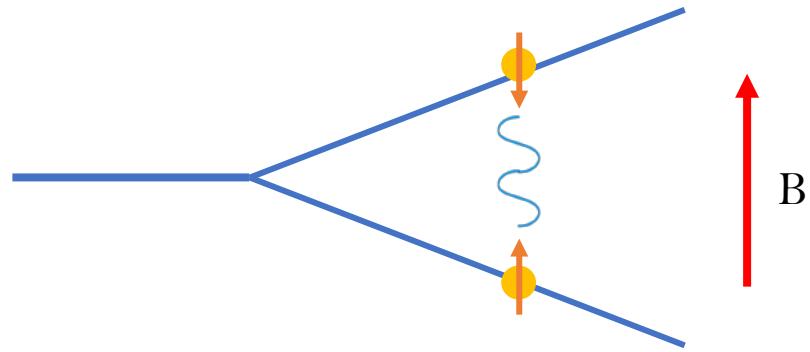
Absorption of photon increases the cavity loss rate



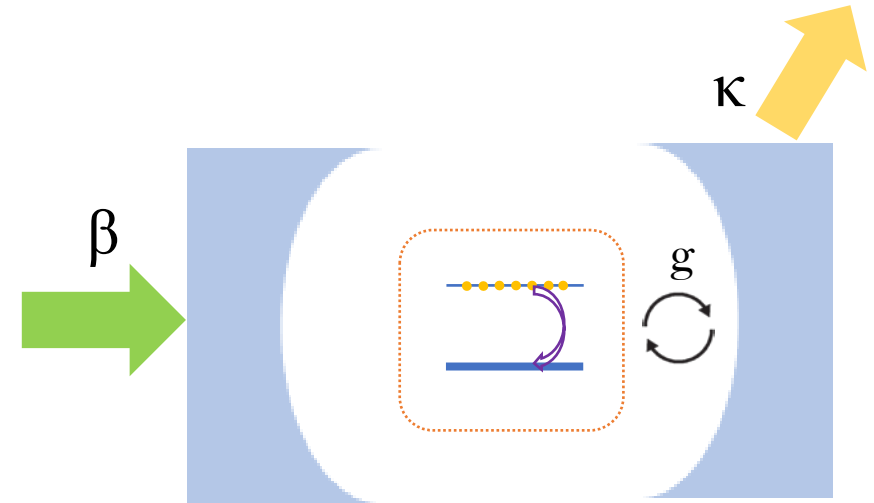
$$h\nu = E = g\mu_B B$$

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Absorption of photon increases the cavity loss rate

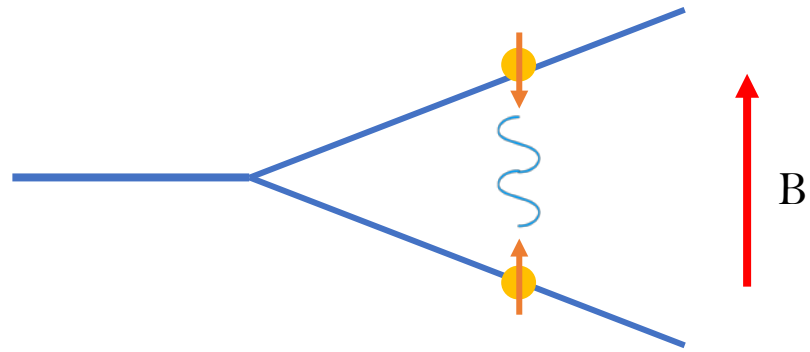


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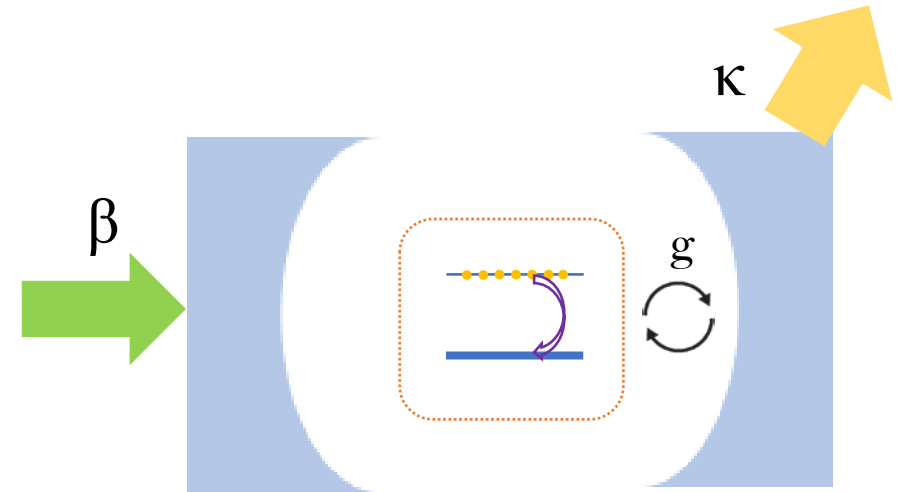


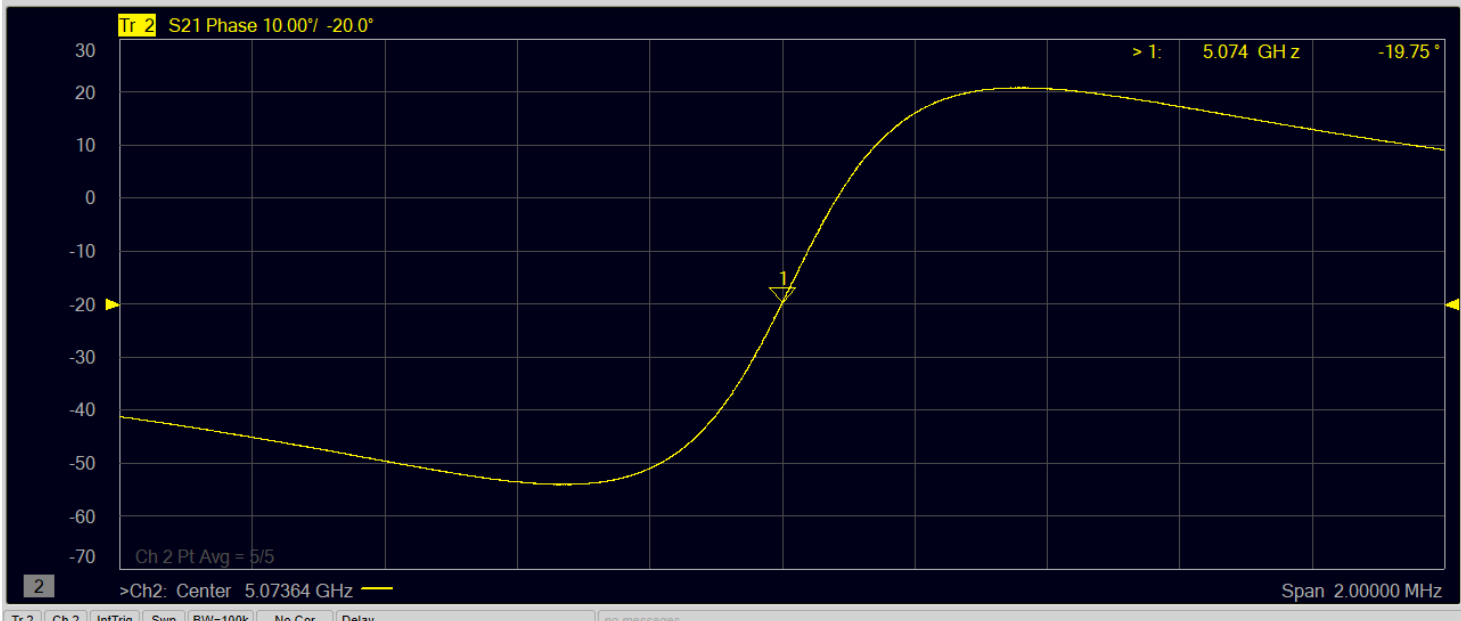
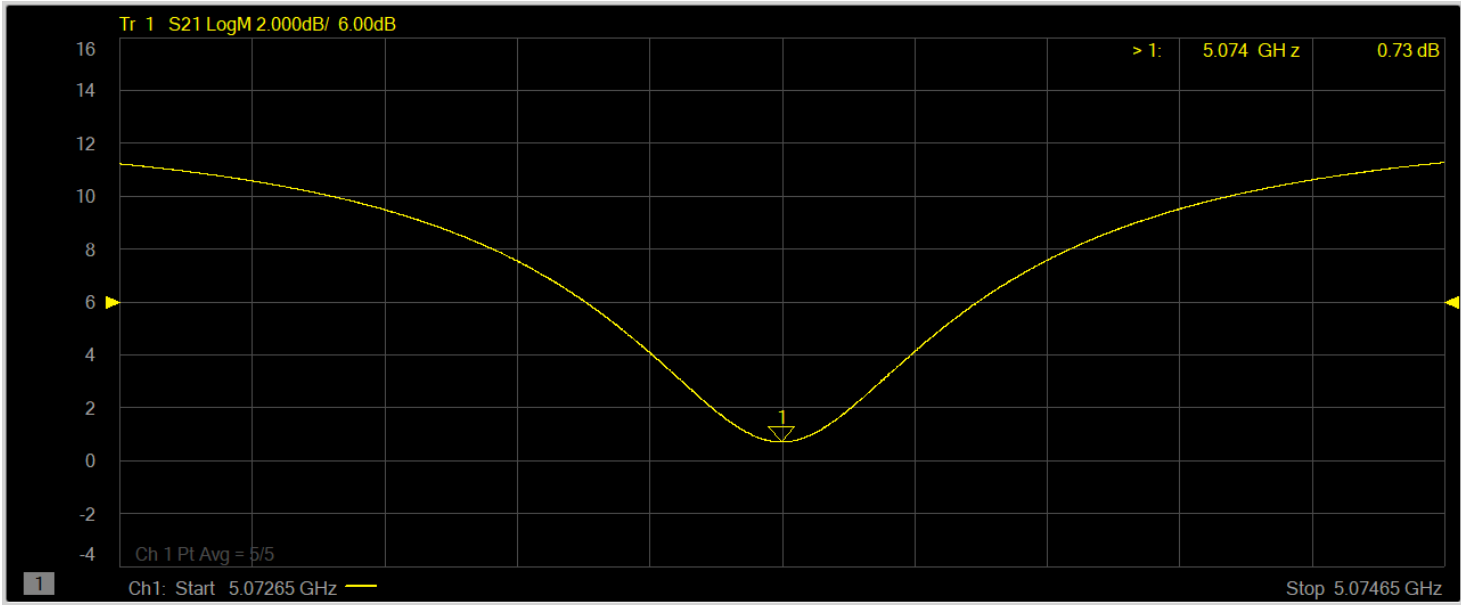
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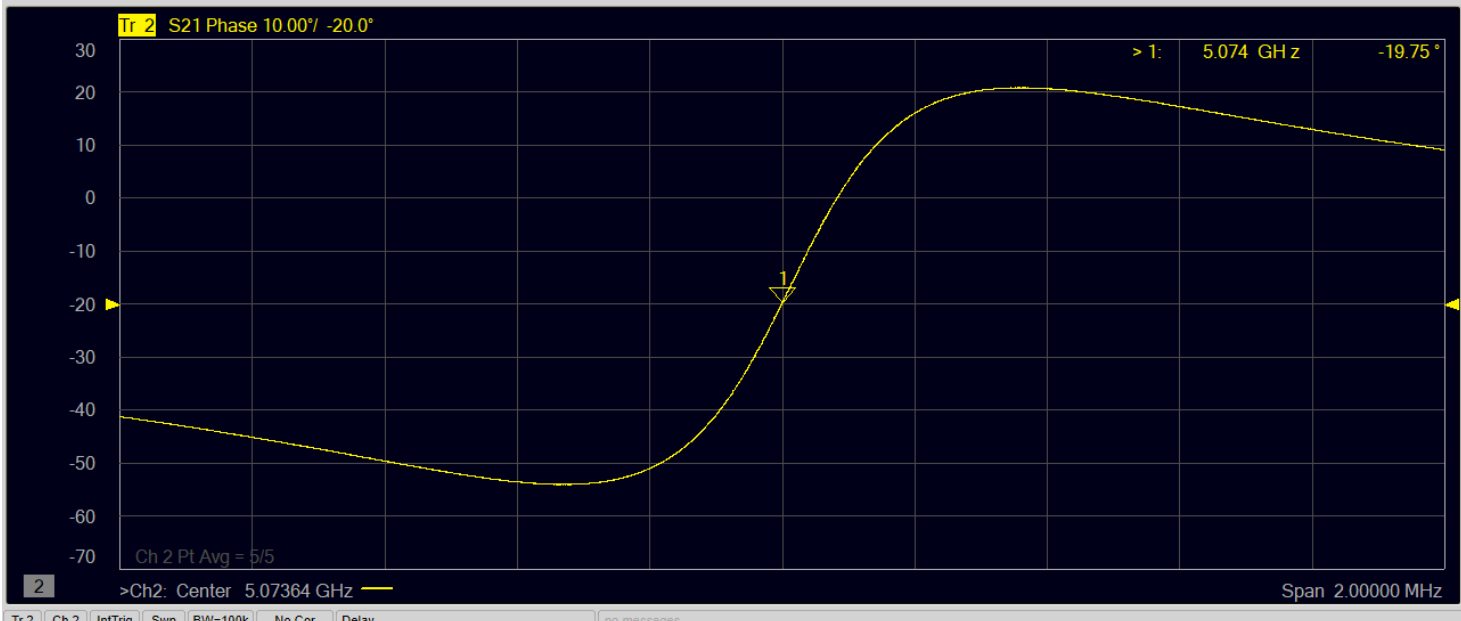
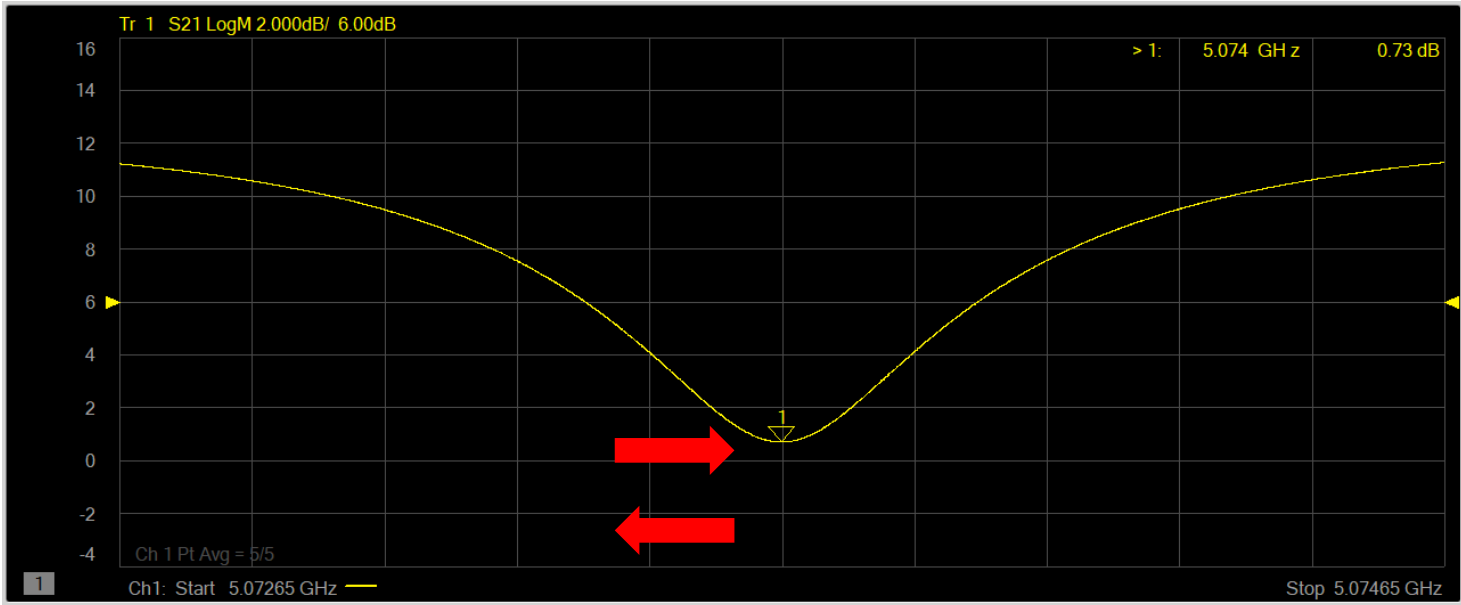


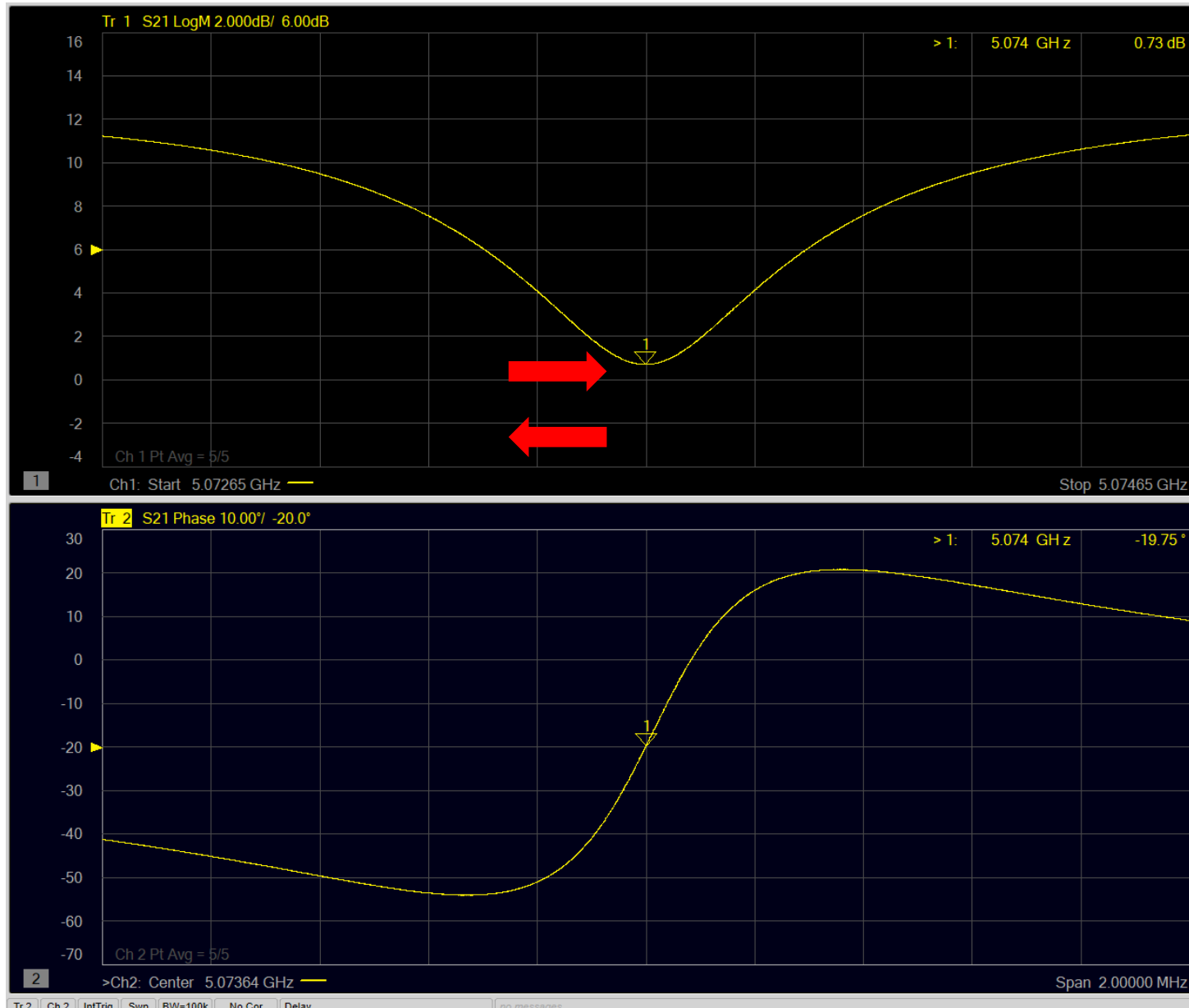
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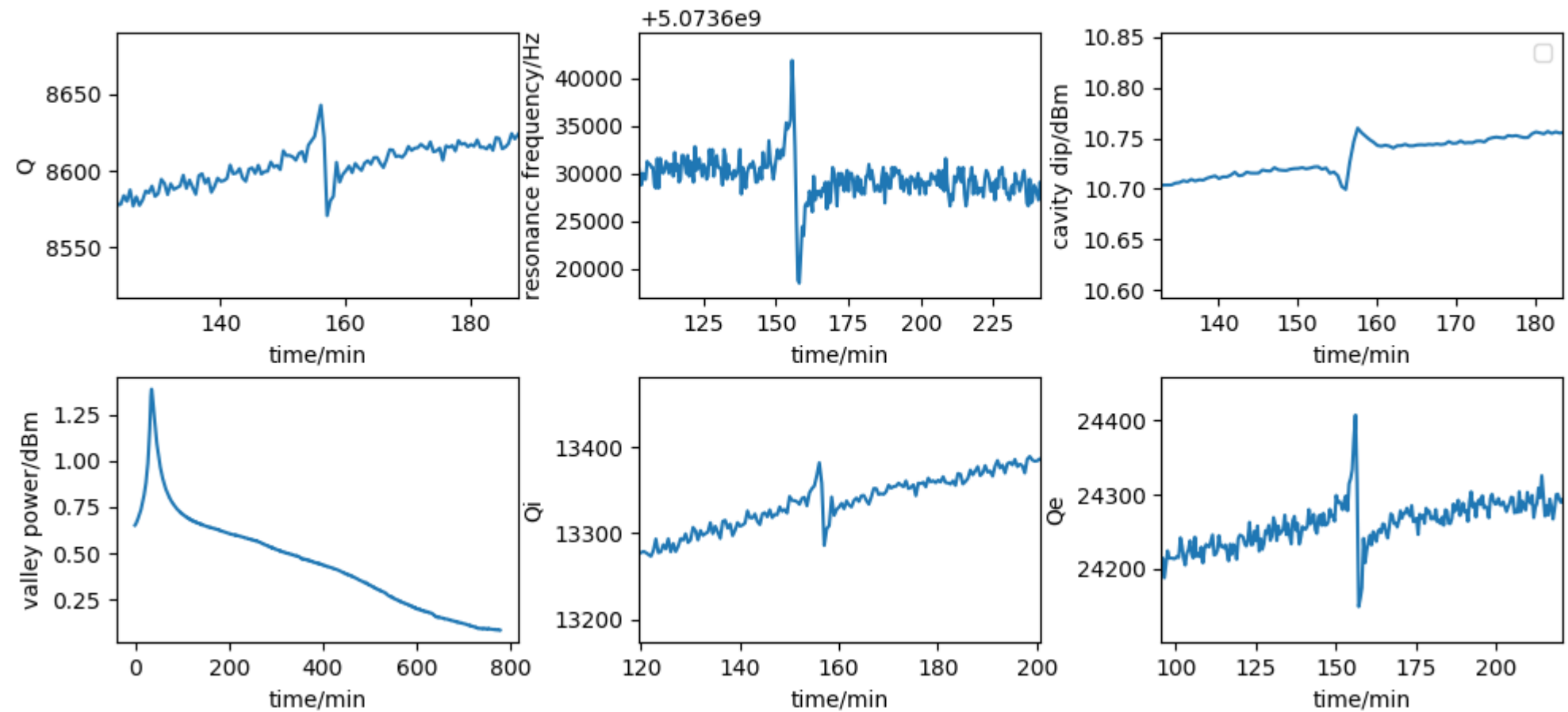


2 MHz span  
1601 points  
-> up to 1.25 kHz sensitivity

slow and noisy  
uncertainty of the size of  
frequency steps  
contain much unnecessary data

# VNA monitoring result of Nd:YSO

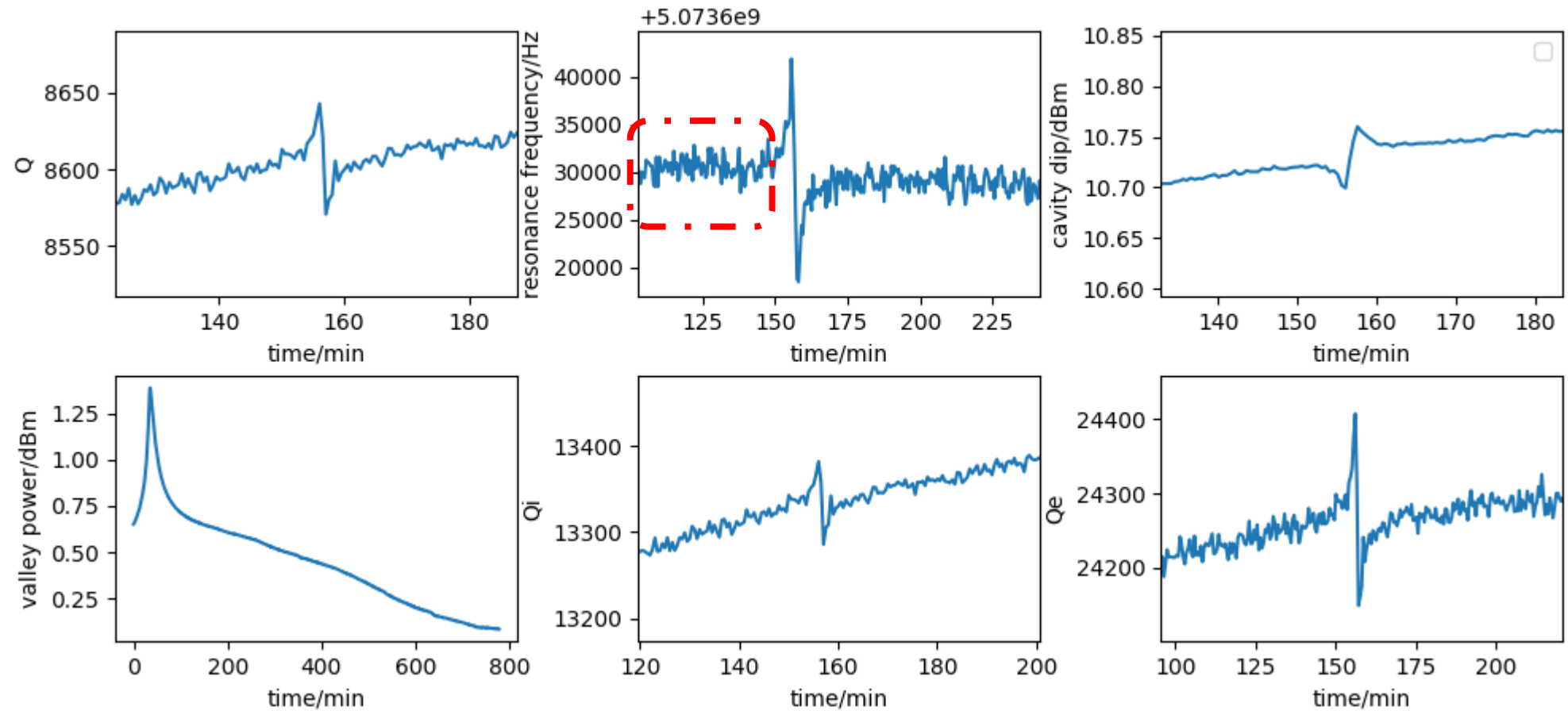
Ramp up from 75 - 375 mT, 0.2 mT step size, D2 direction



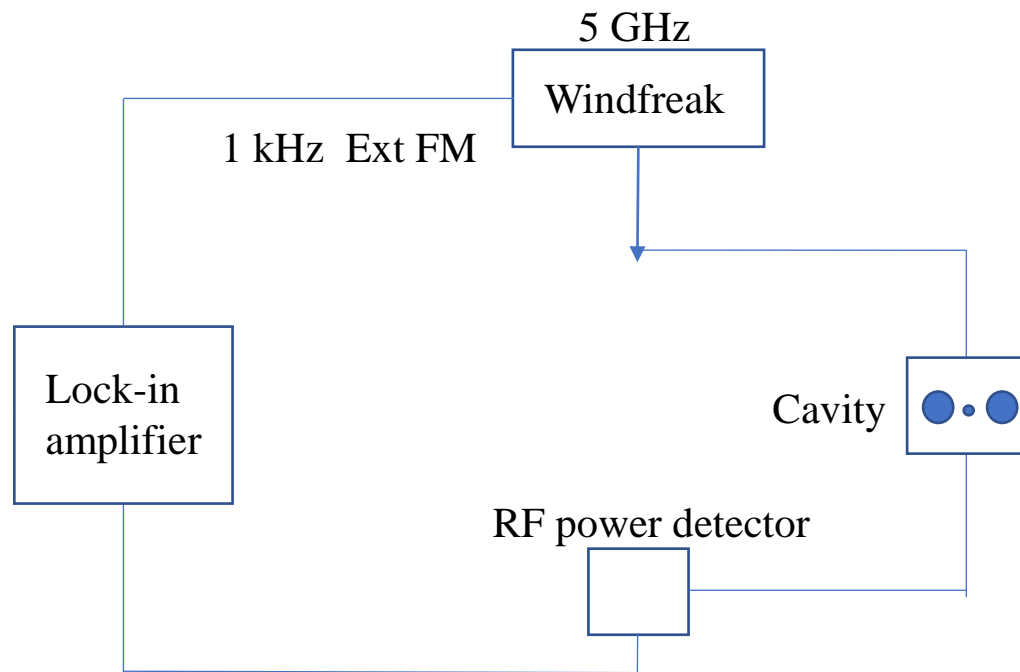
# VNA monitoring result of Nd:YSO

Ramp up from 75 - 375 mT, 0.2 mT step size, D2 direction

$\sim 4000$  Hz resolution



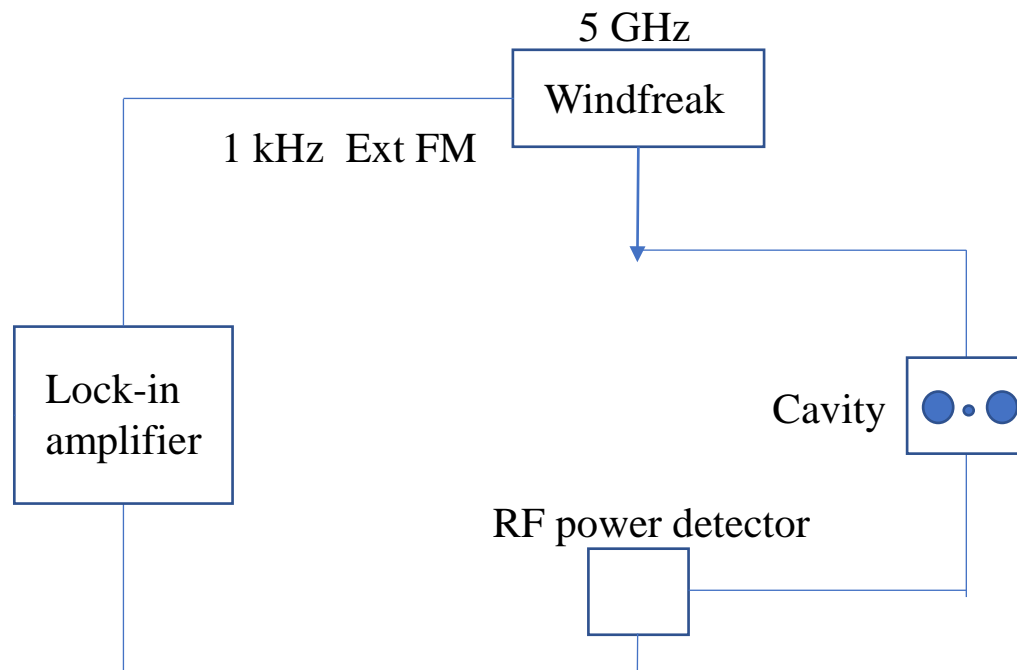
# Lock-in setup



# Lock-in setup

Cavity output:  $a_1(t) = V_1 T(w(t)) * \cos[(w_c + \Delta * \cos(w_d t))t]$

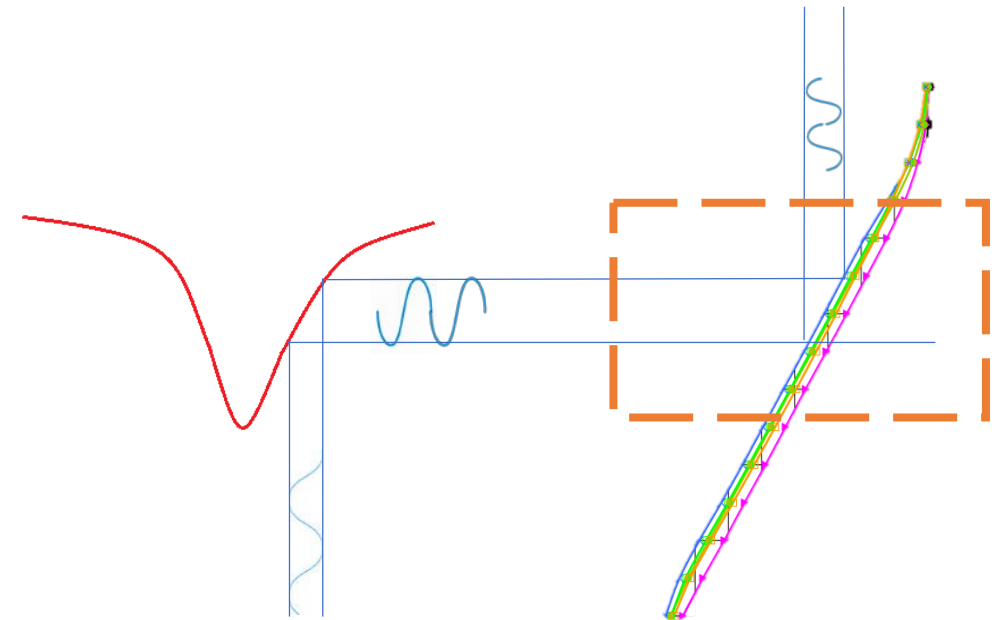
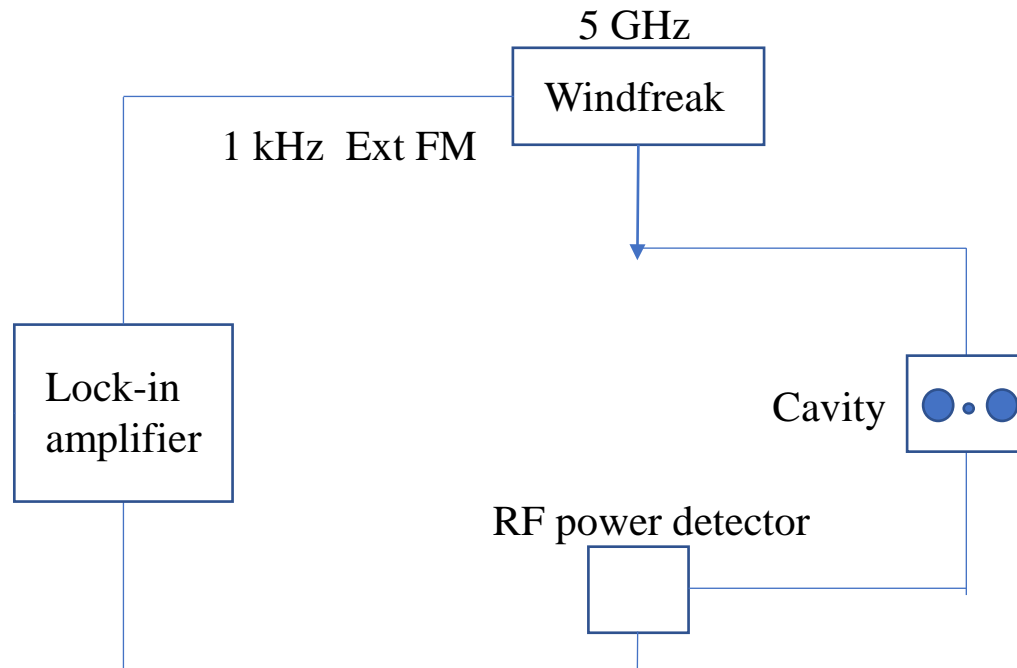
Quasi-sinusoid error signal, demodulated by lock-in amp



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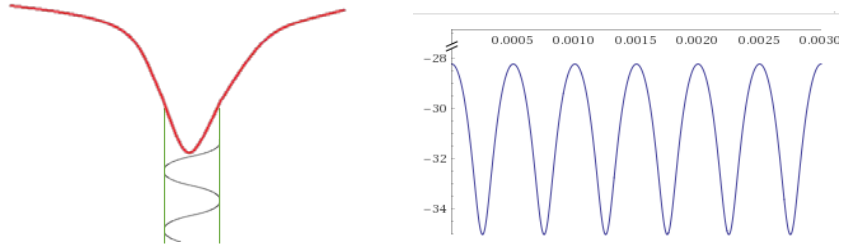
Quasi-sinusoid error signal, demodulated by lock-in amp



$$T(w) = \frac{k_i - k_e + 2i(w - w_0)}{k_i + k_e + 2i(w + w_0)}$$

# Output of power detector $V(w)$

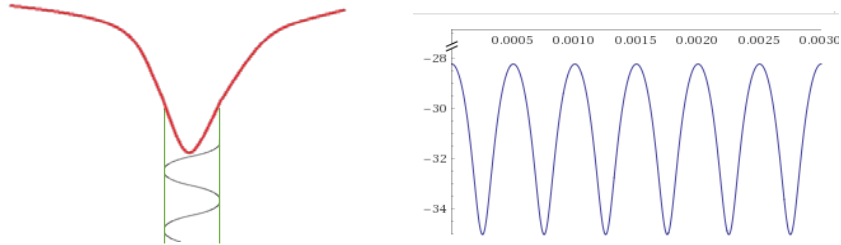
1



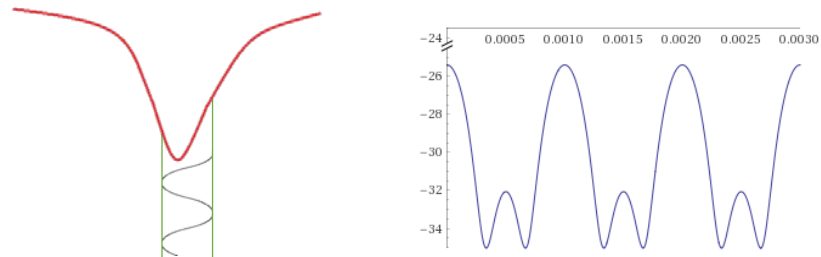


# Output of power detector $V(w)$

①

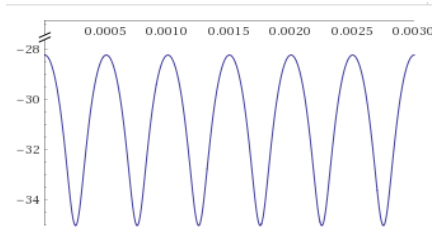
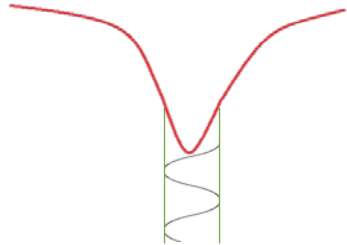


②

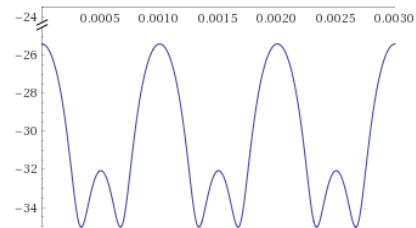
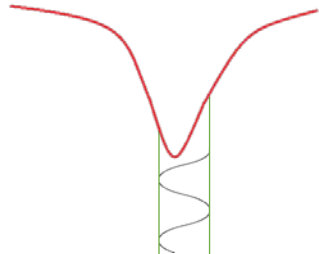


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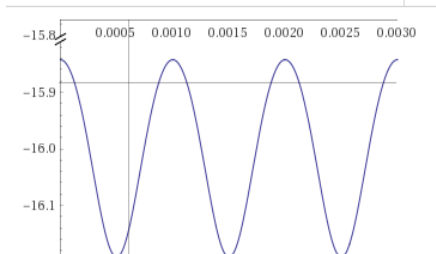
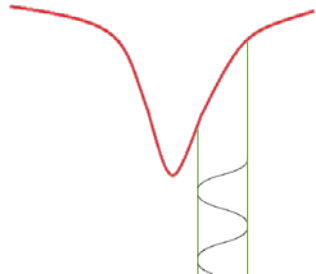
①



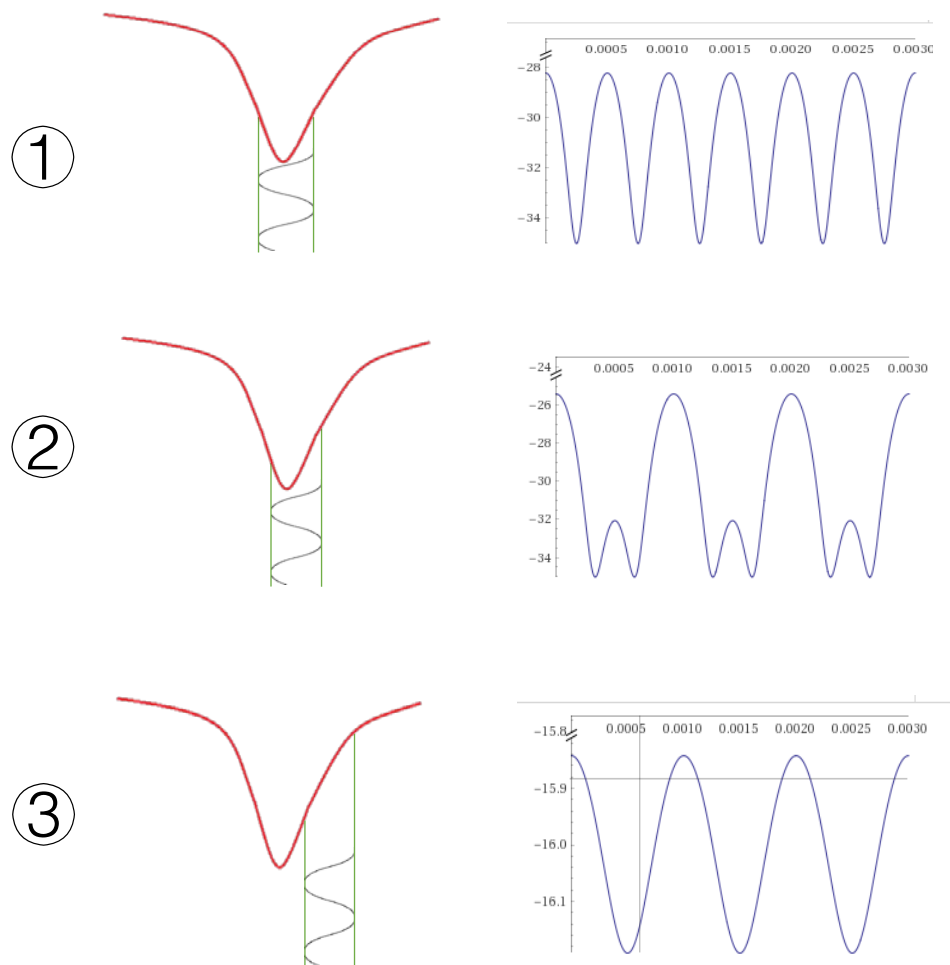
②



③

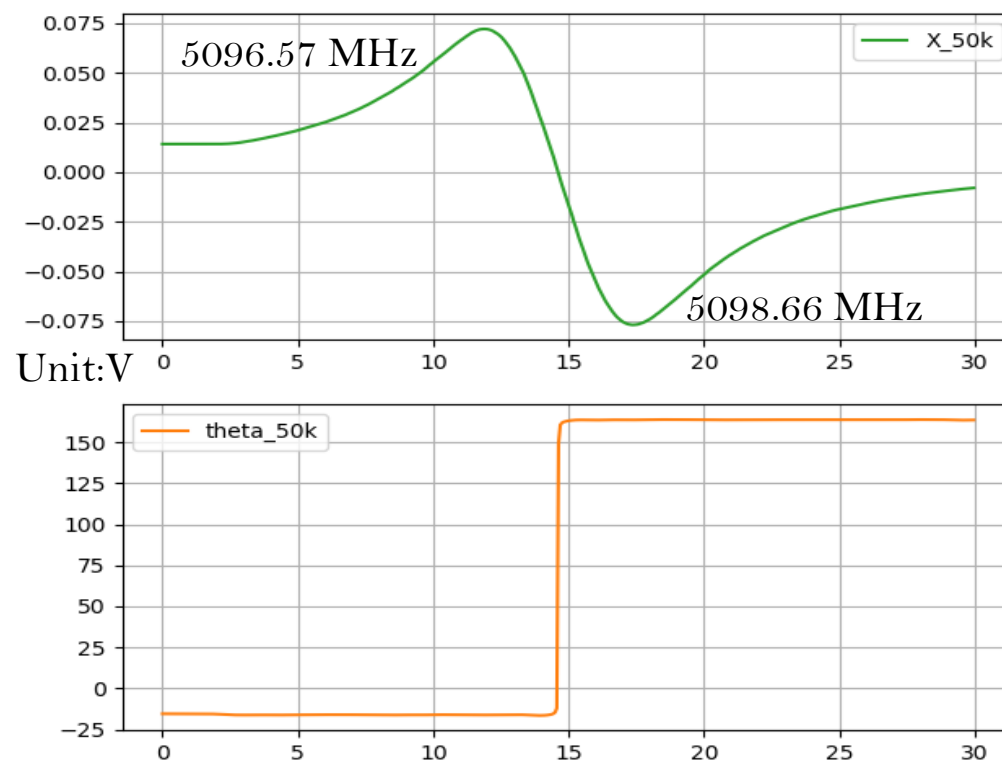


## Output of power detector $V(w)$

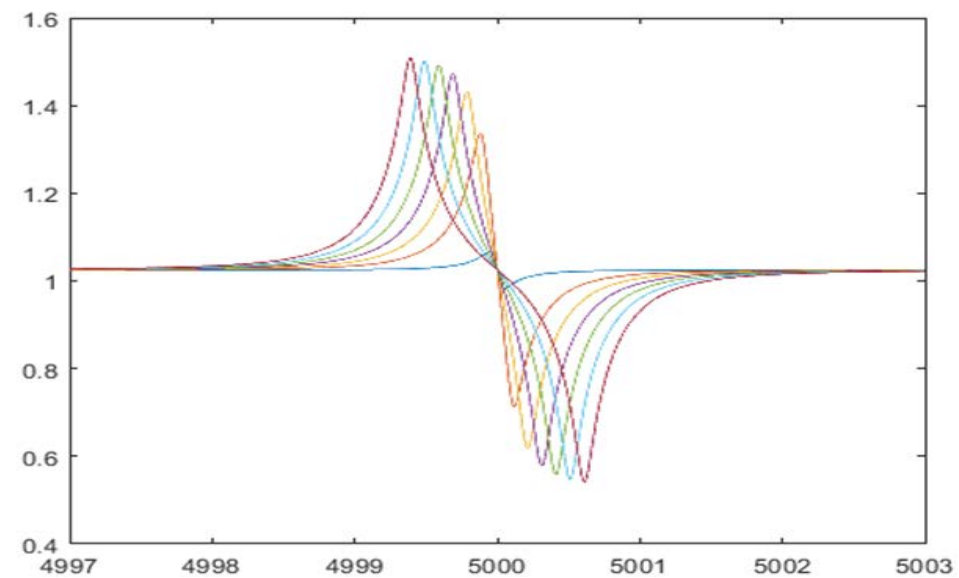


## Lock-in display

$$a_1 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(w_d t)$$



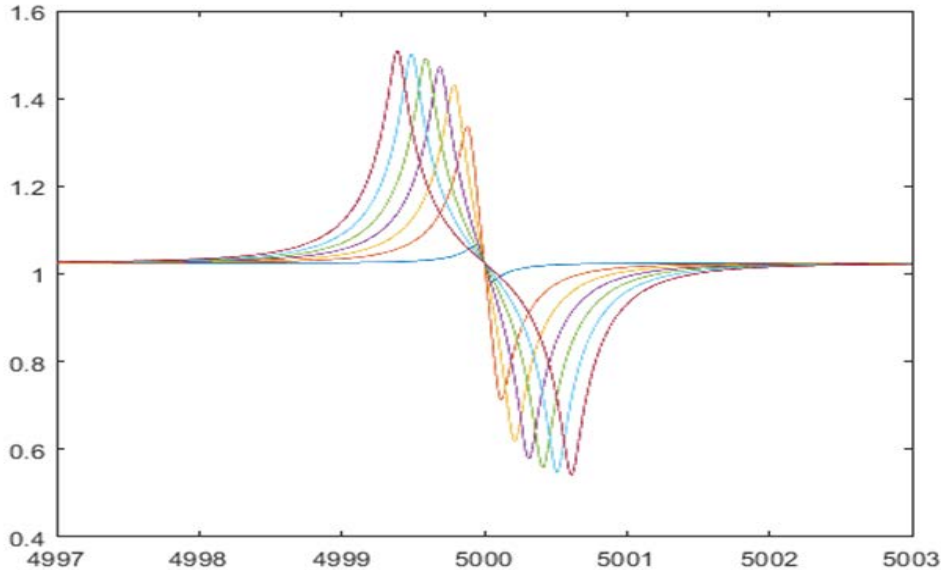
# System optimization



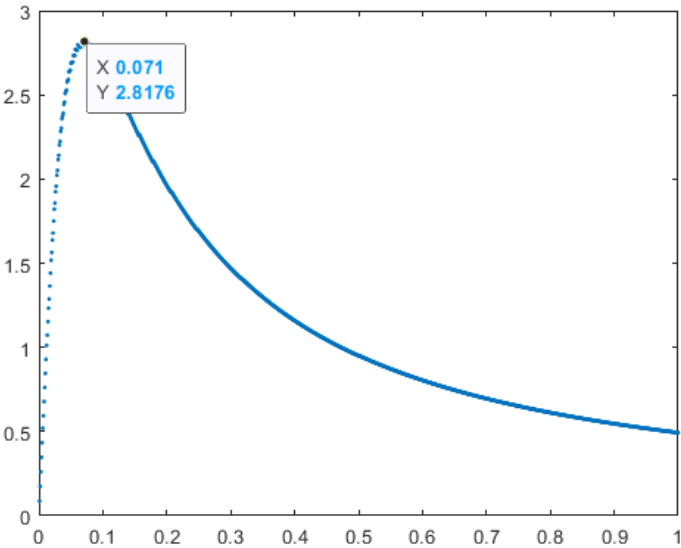
Feature distorted at large deviation

Slope goes down

# System optimization

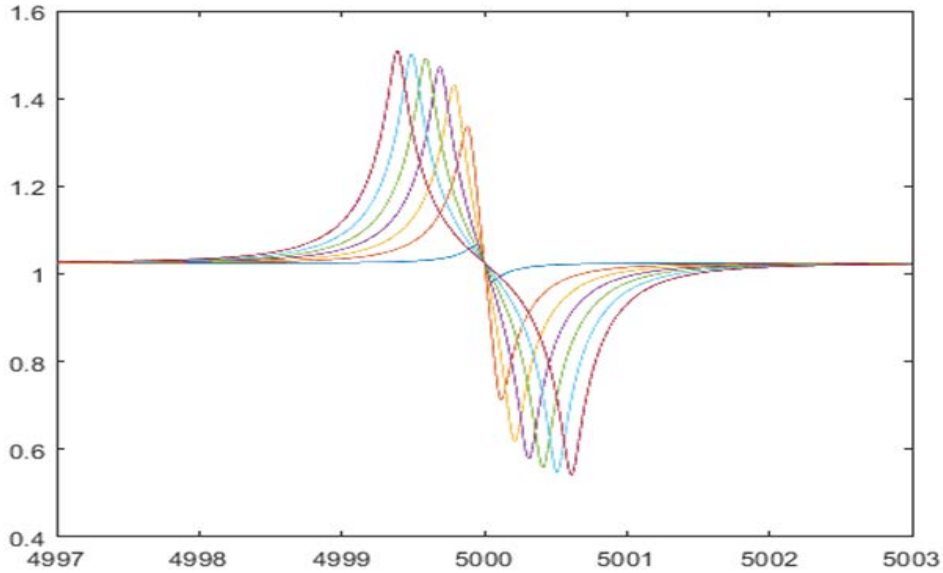


Feature distorted at large deviation  
Slope goes down

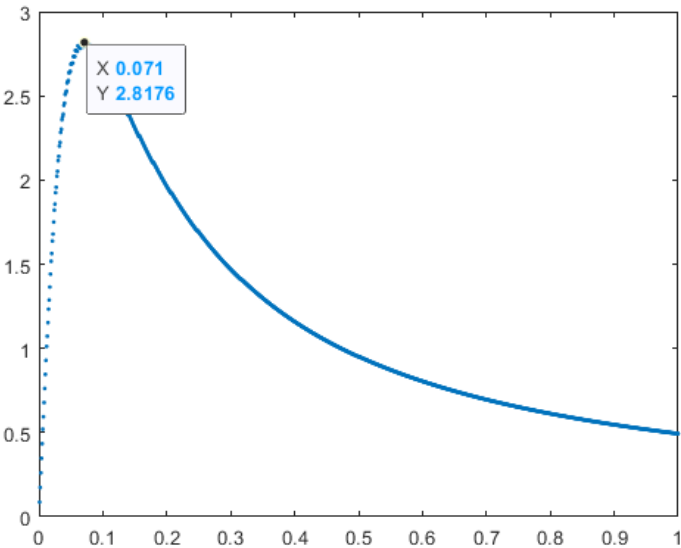


Cavity slope vs deviation frequency

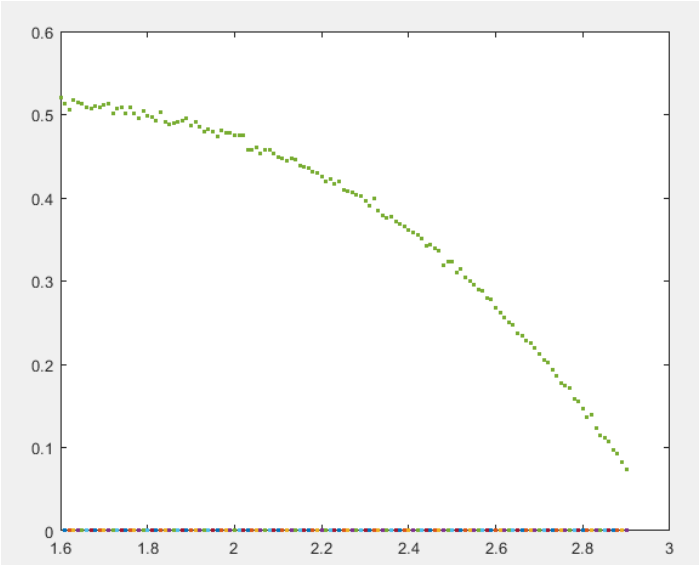
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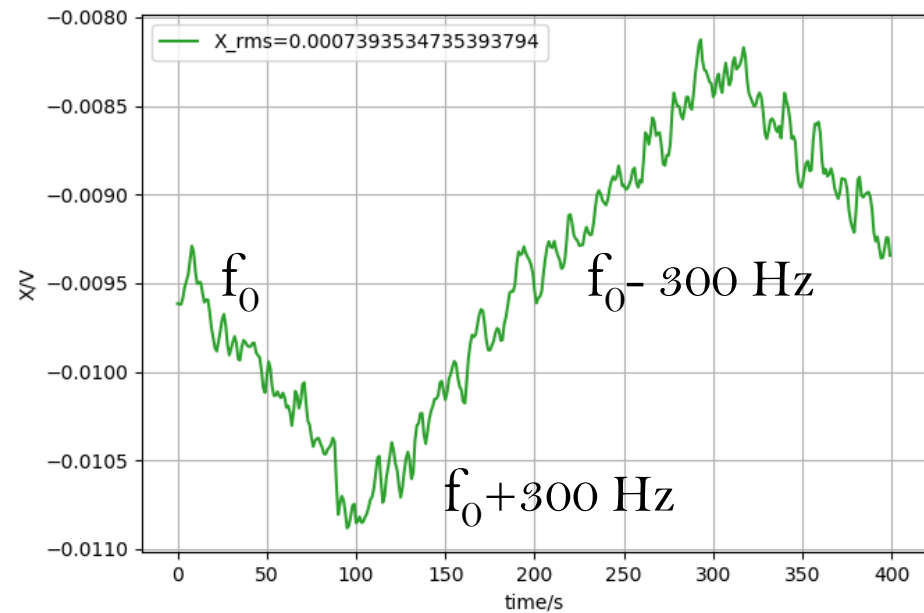


Best deviation vs  $\kappa_i + \kappa_e$

# Experimental result

Simulated frequency shift

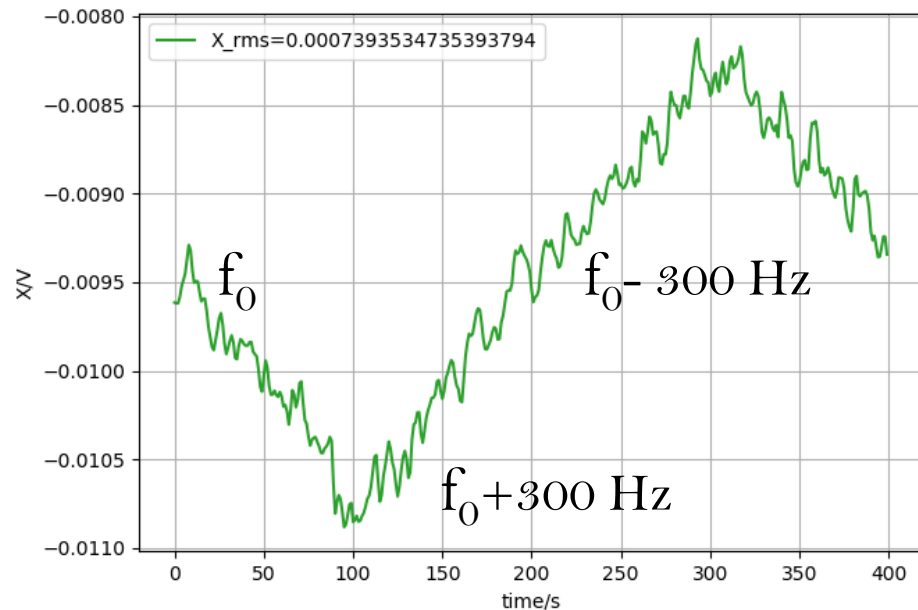
10 times enhancement of sensitivity



## Experimental result

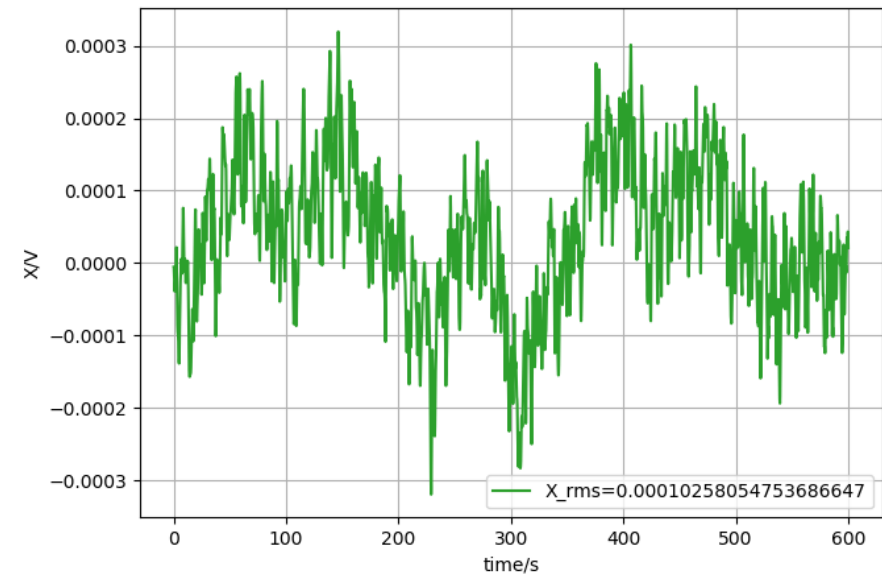
Simulated frequency shift

10 times enhancement of sensitivity



To further enhance sensitivity

- ① a feedback loop to stabilize the RF source frequency
- ② a better power detector
- ③ source with better FM control



0.1 V rms noise



## Complex frequency shift

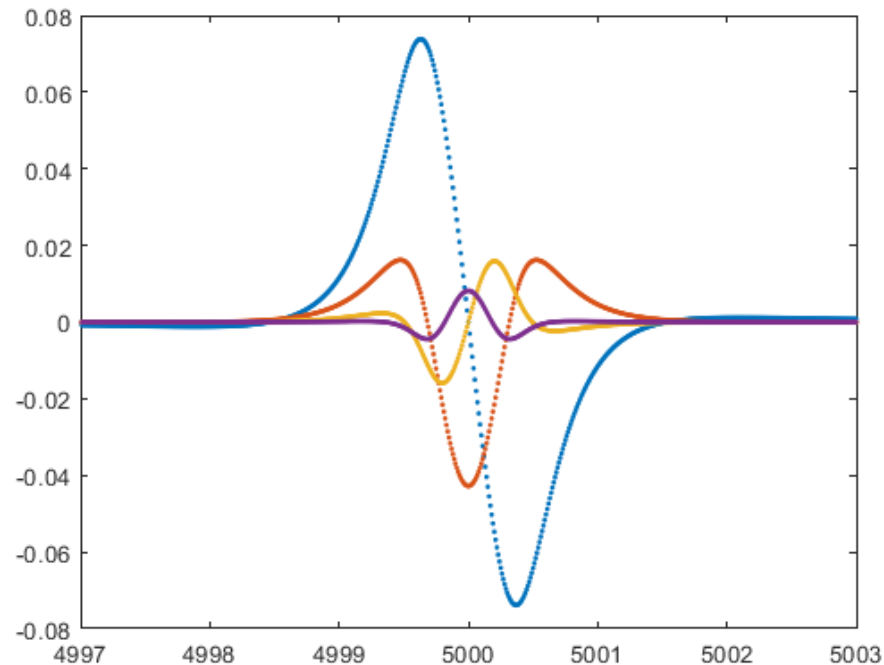
$$\frac{\Delta \tilde{f}}{f} = \frac{\Delta f}{f} + i\Delta \frac{1}{2Q}$$

*Cavity perturbation by superconducting films in microwave magnetic and electric fields. D.-N. Peligrad et al.*

## Complex frequency shift

$$\frac{\Delta \tilde{f}}{f} = \frac{\Delta f}{f} + i\Delta \frac{1}{2Q}$$

*Cavity perturbation by superconducting films in microwave magnetic and electric fields. D.-N. Peligrad et al.*



$$a_1 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(w_d t)$$

$$a_2 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(2w_d t)$$

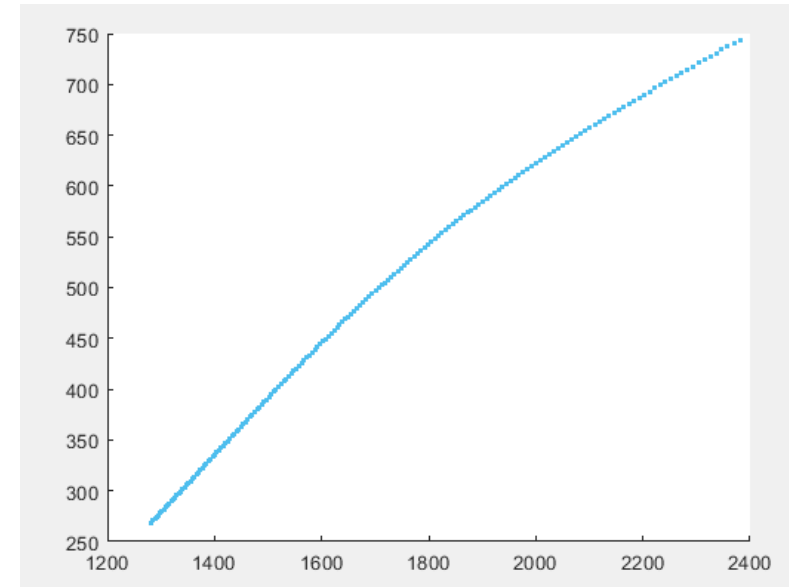
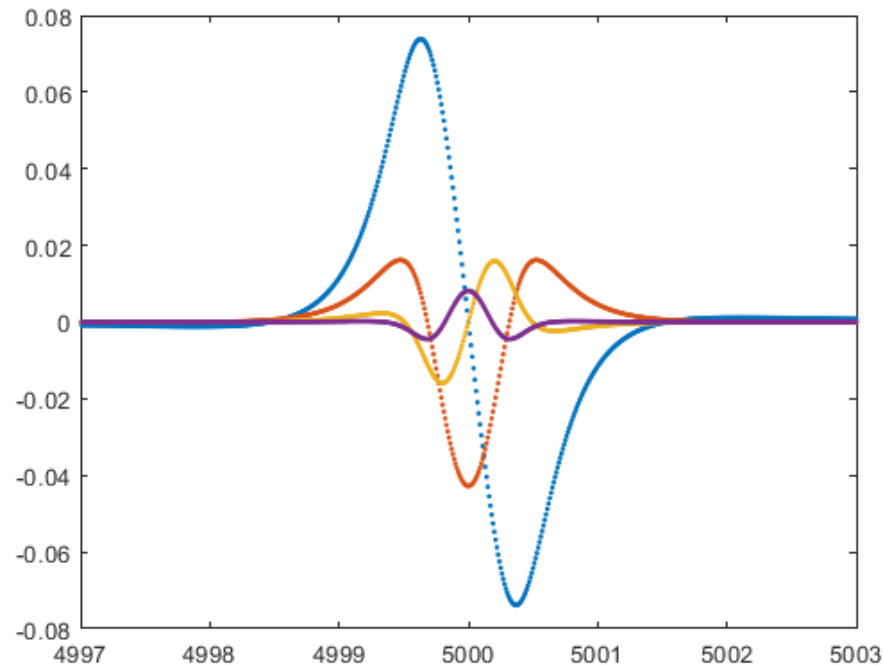
$$a_3 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(3w_d t)$$

$$a_4 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(4w_d t)$$

## Complex frequency shift

$$\frac{\Delta \tilde{f}}{f} = \frac{\Delta f}{f} + i\Delta \frac{1}{2Q}$$

*Cavity perturbation by superconducting films in microwave magnetic and electric fields. D.-N. Peligrad et al.*



$a_4/a_2$  vs  $Q$

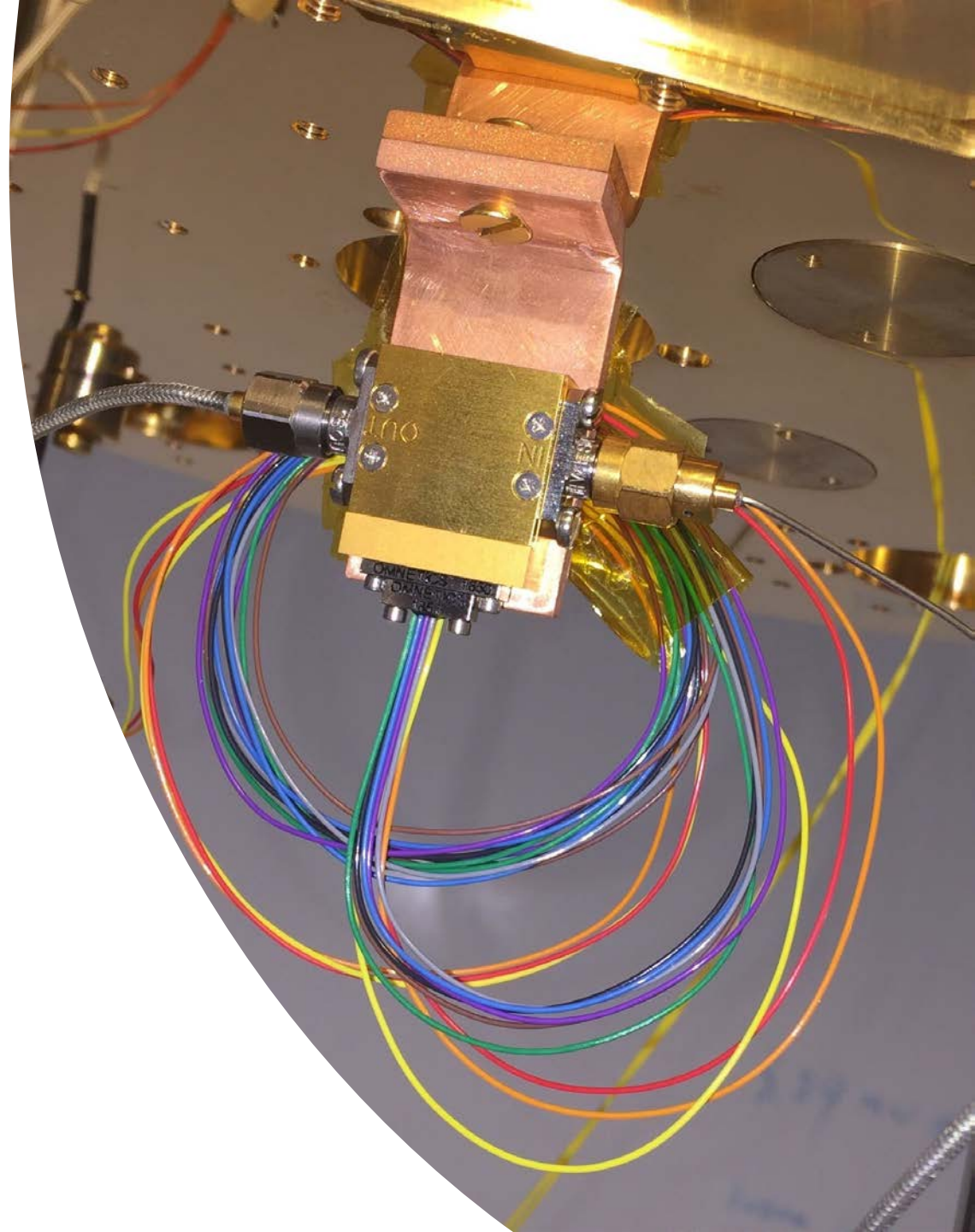
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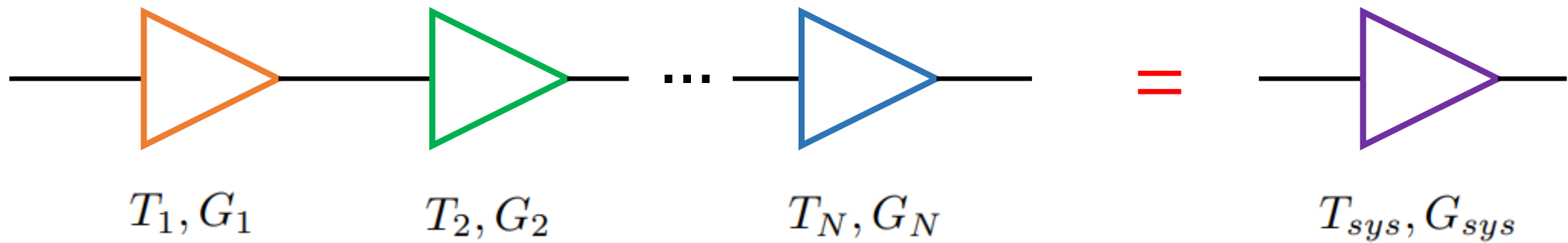
$$a_4 = \frac{w_d}{\pi} \int_0^{\frac{w_d}{2\pi}} V(w) * \cos(4w_d t)$$

- Characterization of TWPA
- Enhancing sensitivity of EPR
- Setting up of HEMT



# Necessity of HEMT

- The noise figure of an amplification chain largely depends on the first amplifier

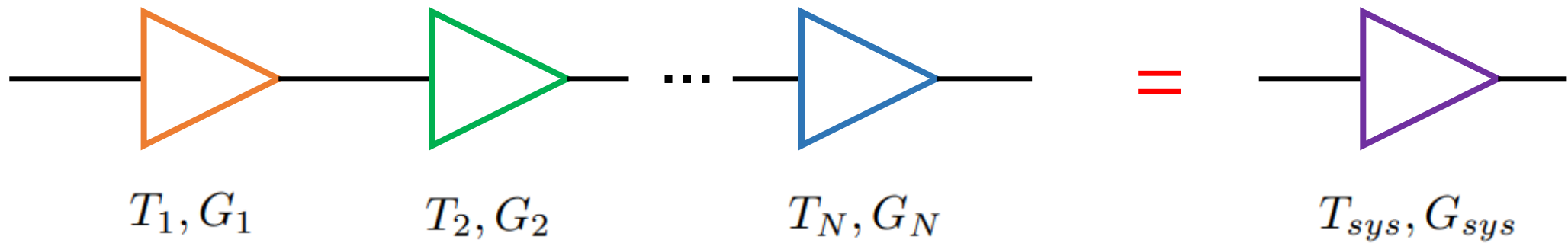


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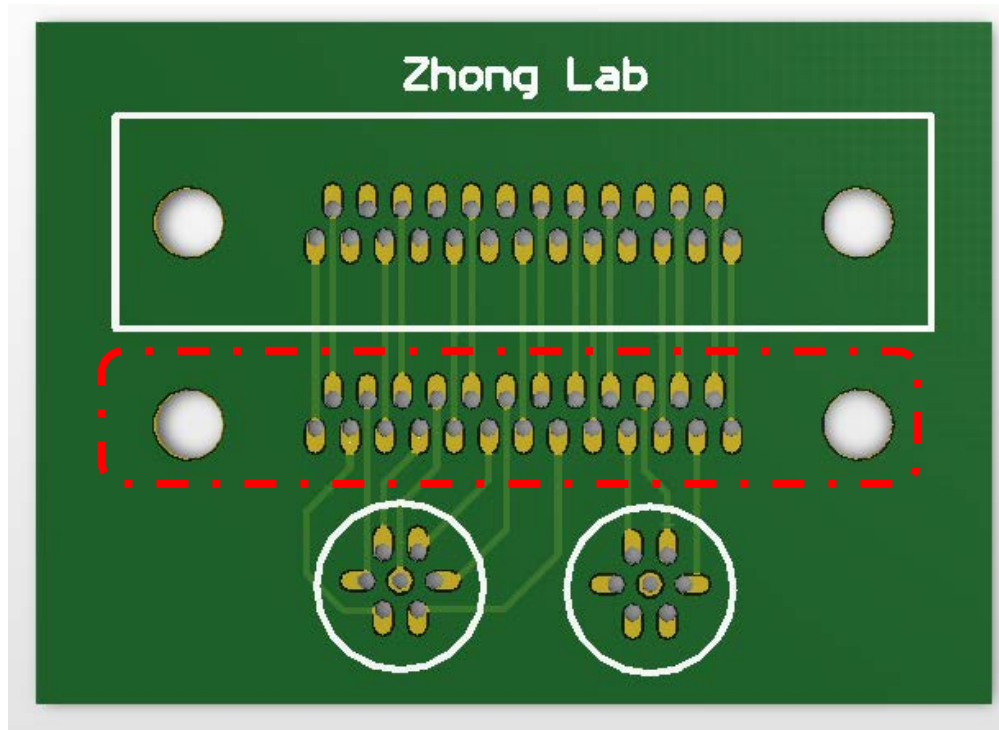
Friis formula:

$$T_{sys} = T_1 + \frac{T_2}{G_1} + \frac{T_3}{G_1 G_2} + \dots + \frac{T_N}{G_1 G_2 \dots G_{N-1}}$$



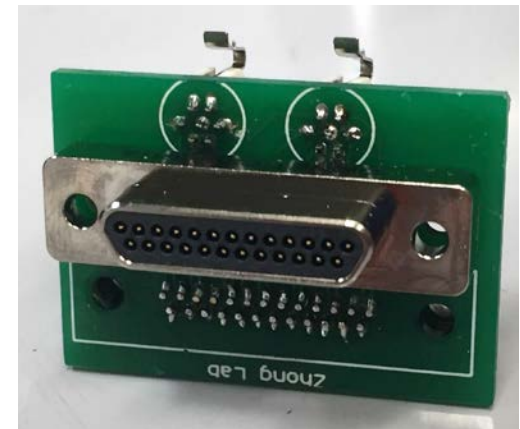
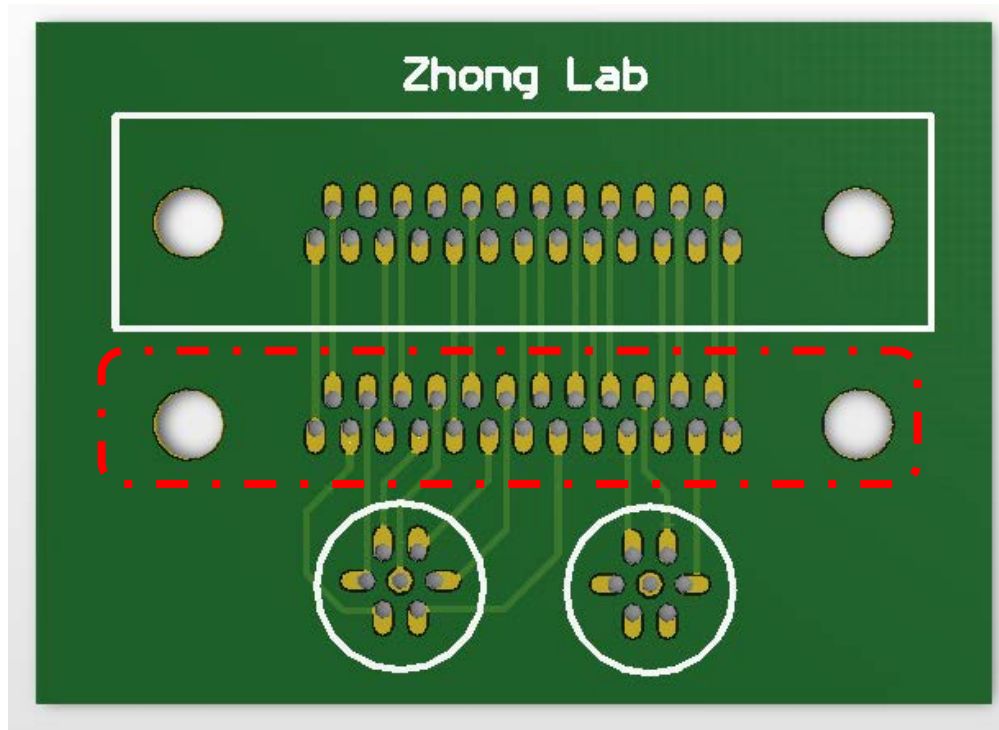
# DC connection

- Split the 25 pins into three parts



# DC connection

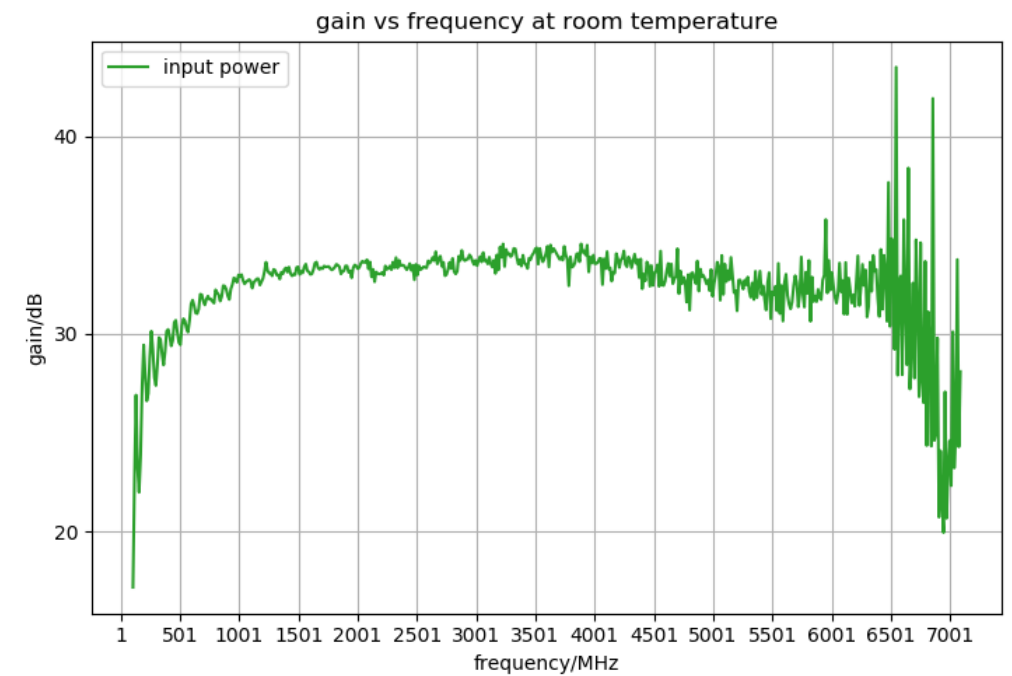
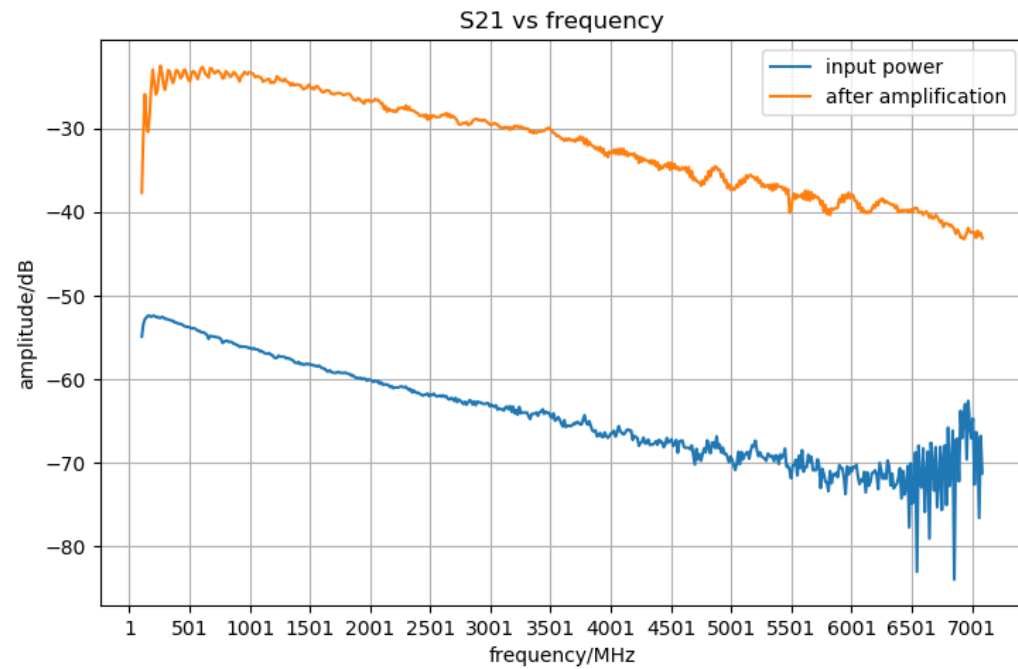
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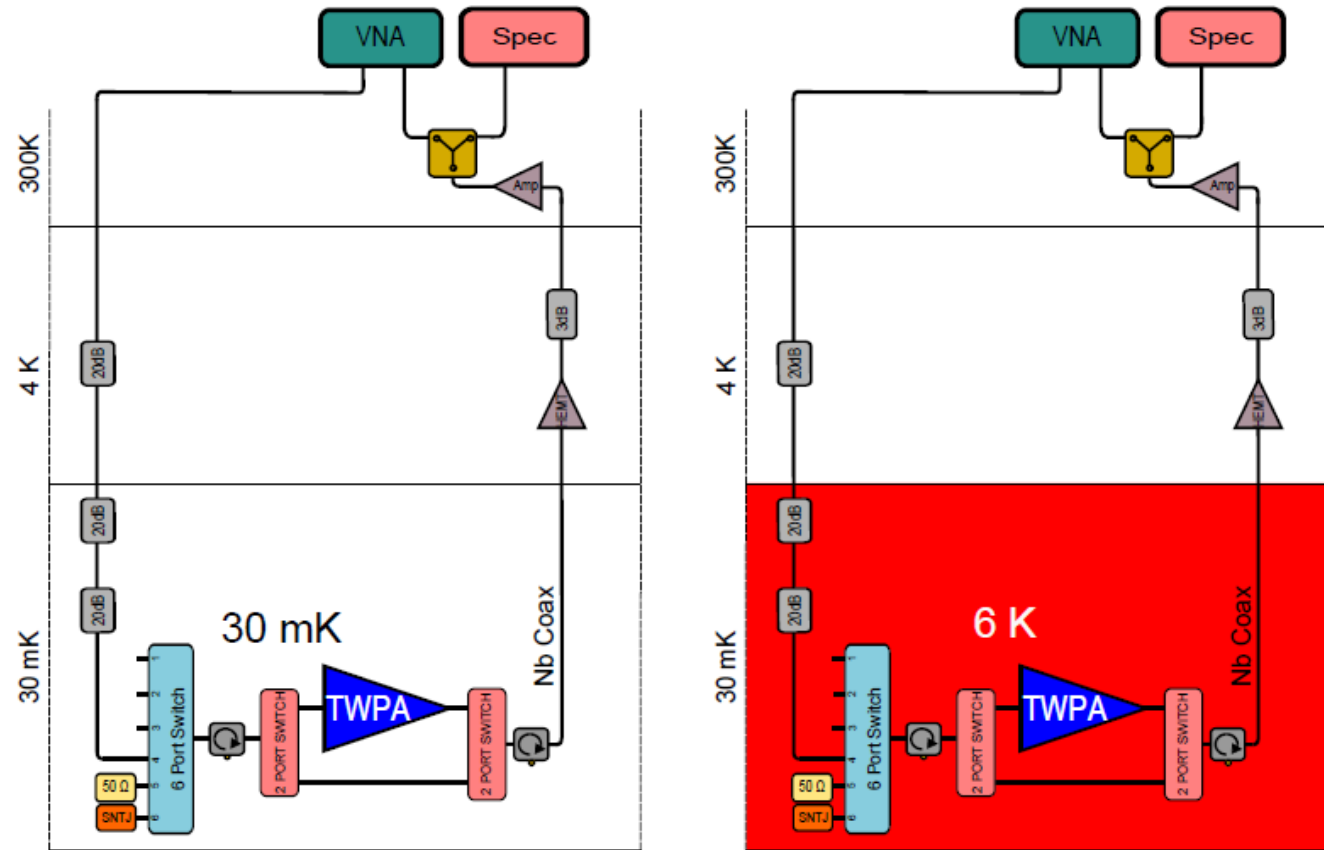
# Room temperature amplification

- To get better curve, use VNA with calibration



# Noise figure measurement

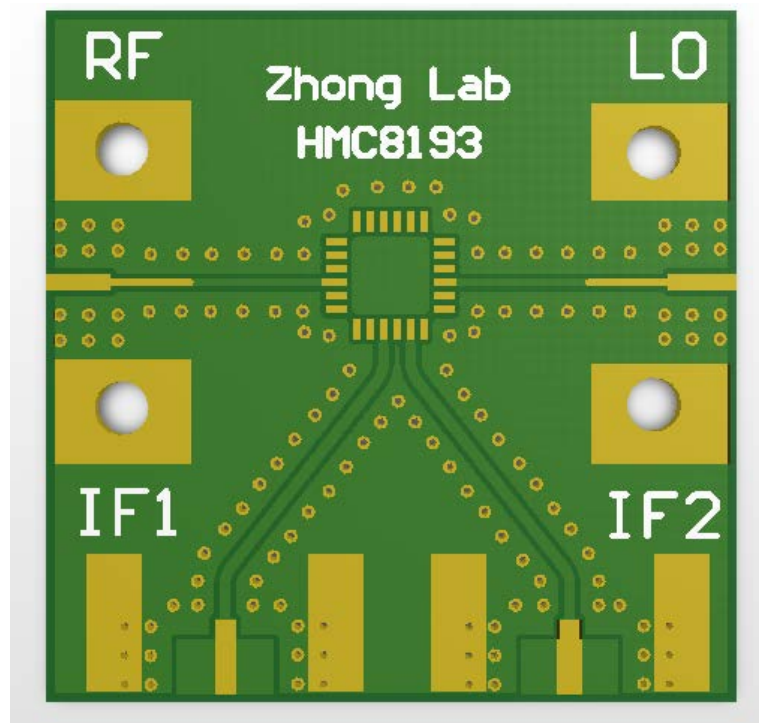
## Y factor method



*Traveling wave parametric amplifier with Josephson junctions using minimal resonator phase matching. Supplemental information. T.C. White et al.*

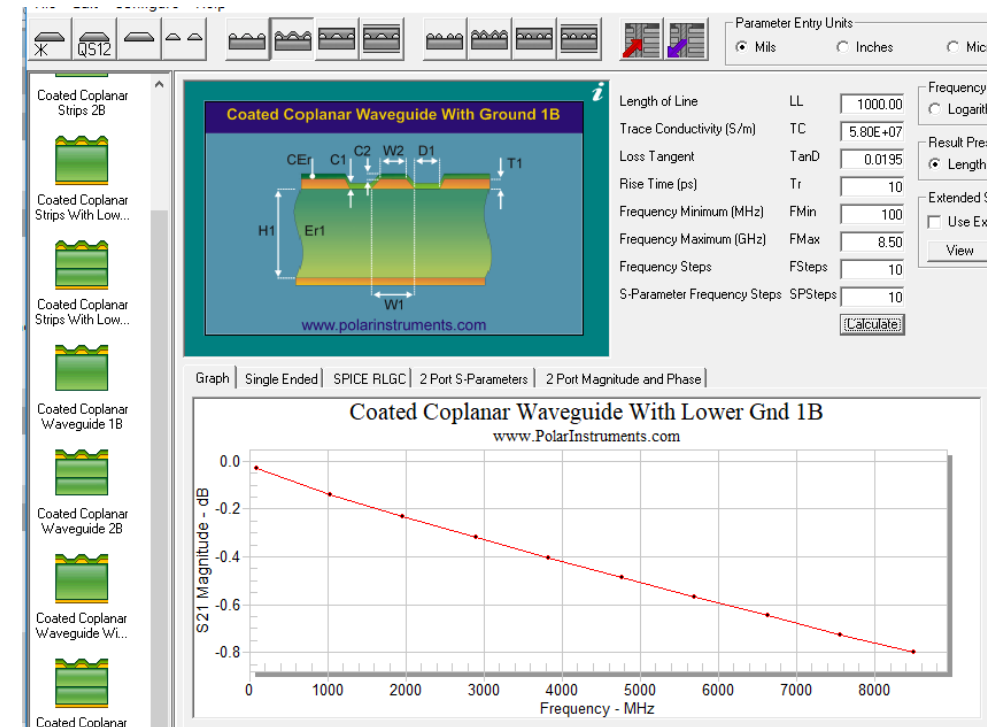
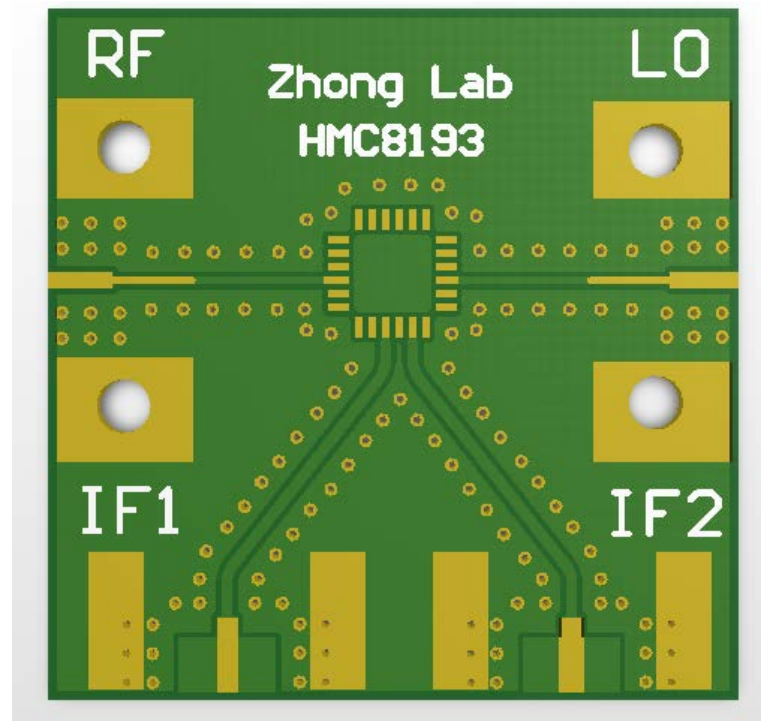
# Test board & IQ demodulator

- 10 mil width, 7.5 mil gap, 7.1 mil thickness



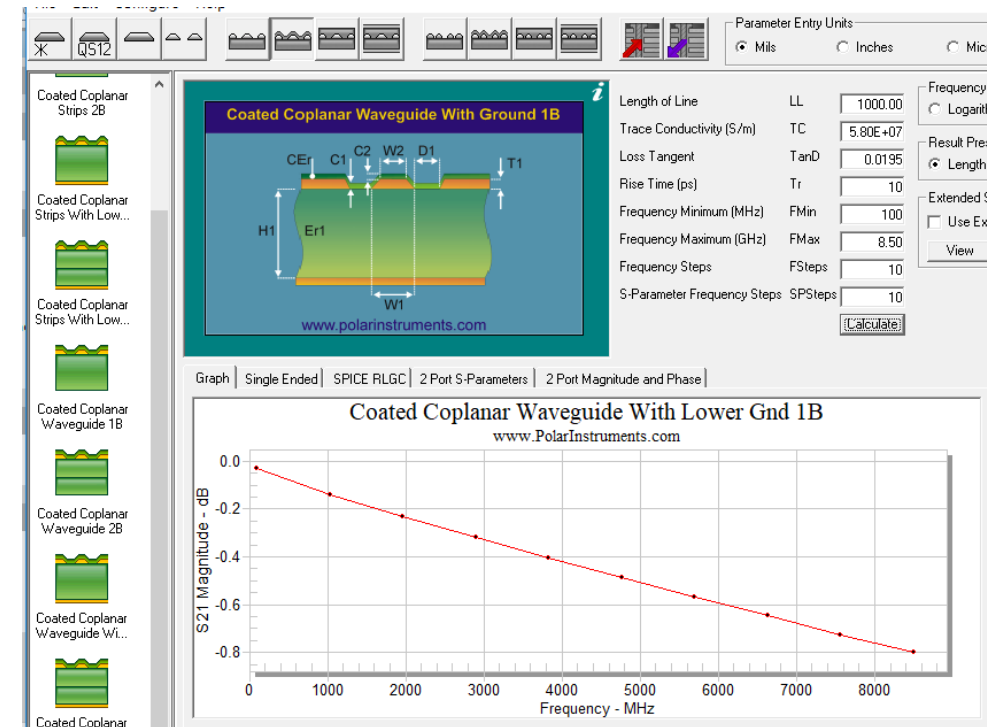
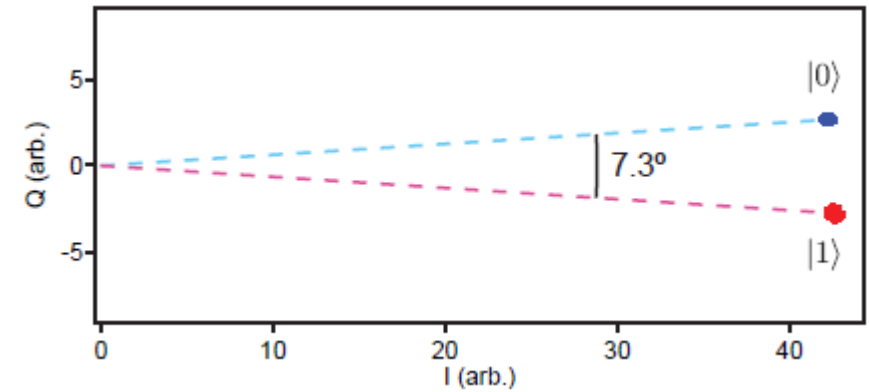
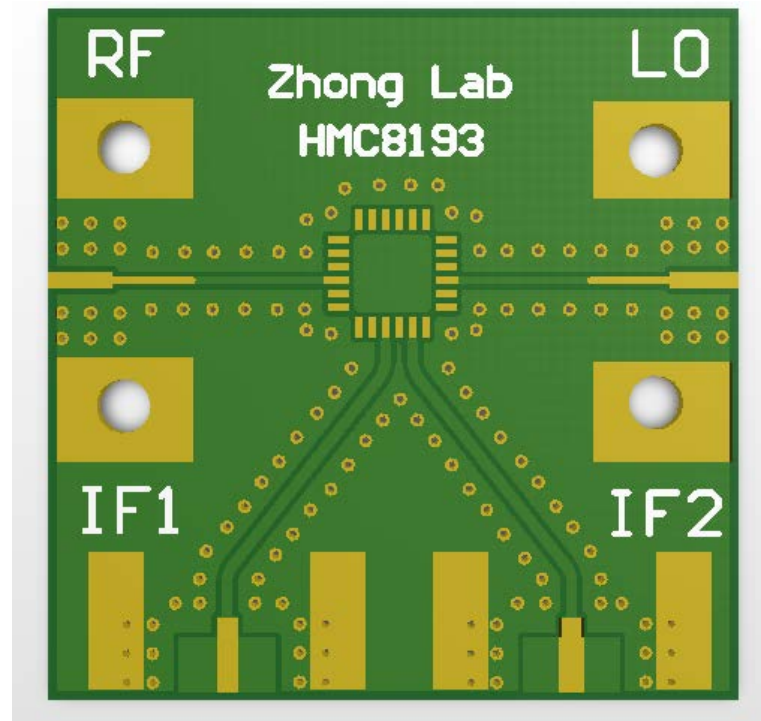
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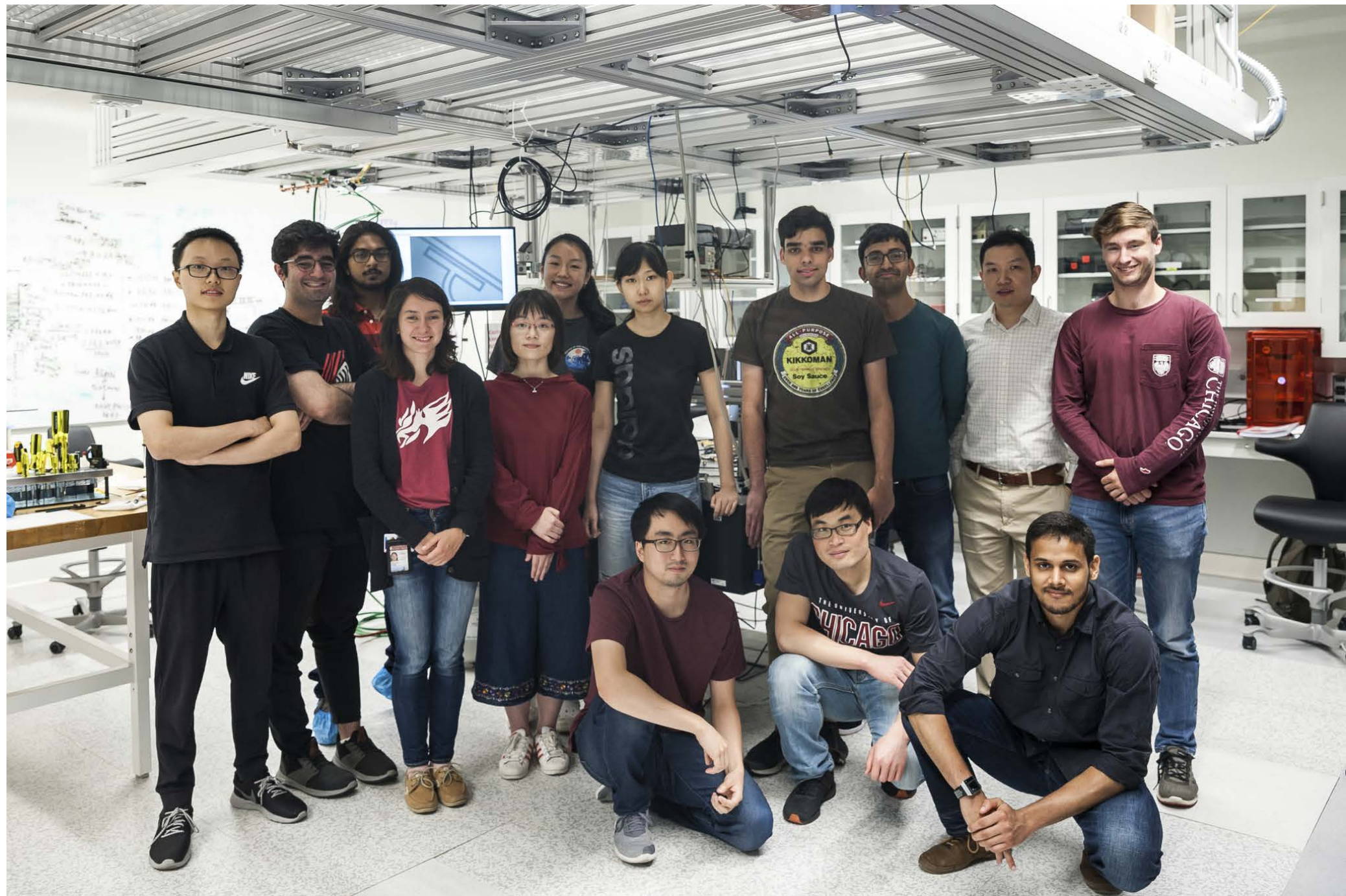


# Test board & IQ demodulator

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# Chicago



# New York





# Ann Arbor





# Seoul

